Estimation of Added Resistance of a Ship in Regular Waves

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Editors


Uredništvo

Preliminary communication

Two methods of added resistance calculation are briefly presented, one developed by Faltinsen, and the other by Salvesen. Both are based on the Salvesen, Tuck and Faltinsen linear strip theory, as they use it to define the wave induced motions. The first one obtains the added resistance by direct pressure integration, while the second one involves the potential flow solution. Also, as a third method, an empirical approximation of the Salvesen method for the short wave lengths region is included.

The calculations of added resistance due to waves were performed according to the chosen methods for four different ships: two containerships, a bulk carrier and a ro-ro vessel. The results are presented graphically, with the comparison to experimental results for the available cases.

Keywords: added resistance, motion of a ship in waves, speed loss

1 Introduction

The capability to sustain speed in a seaway is one of the primary objectives in the design of marine vehicle. The added resistance of a ship in a seaway is becoming of great importance because of the increasing demand in transportation speed and voyage duration [1] as well as because of the increasing conscience of the need to reduce emissions from the ships [2].

The term “Added Resistance” is used to describe the phenomenon of energy loss because of generation of waves as a consequence of ship motions due to sea waves. To this purpose the ship resistance in calm water is increased by accounting for the effect of seaway. The ship speed, required power and propeller characteristics are usually estimated for still water conditions. But during its exploitation, the ship encounters different sea conditions and in many occasions the seaway influences the resistance and propulsion features. The added resistance of a ship in waves is generally explained by three effects: the so-called drifting force resulting from interference of incidence waves and waves generated by heaving and pitching; the damping force associated with heaving and pitching in calm water; the diffraction force due to the interference of waves and ship. These forces are related to the energy transmitted from the ship to the water and to wave generation. In general, it has been proved that
the drifting force is the most significant, while the diffraction
force would make the smallest contribution, more important for
short waves. The viscous effect due to the damping of the vertical
motions represents only a small part of this extra-induced loss
of energy.

Progress made in seakeeping, in both analytical methods and
experimental techniques, makes it possible to determine added
resistance with sufficient accuracy for design purposes. However,
the accuracy of added resistance calculation depends very much
on the accuracy of ship motion prediction, but this problem will
not be considered here. The same is valid for the effect of wind
loads on speed loss and the effects which lead to intentional
speed reduction based on the ship master’s judgment (such as
slamming, propeller racing, ventilation, excessive accelerations
and green water on the deck).

The phenomenon treated in the paper is the added resistance
of a ship advancing in regular waves, which causes involuntary
speed reduction. During voyage in wind and waves, the increase
of the resistance requires an adequate power increase in order
to maintain a certain cruising speed. The added resistance may
also have significant influence on ship’s performance in moderate
seas, especially for ships with blunt bow-forms. Therefore, a
preliminary estimation of added resistance considering a given
sea condition needs to be performed.

Different methods of added resistance estimation can be
chosen, starting from the simplest empirical ones to the most
recent computational methods [3]. Several theoretical methods
of added resistance estimation can be pointed out: Havelock [4],
Maruo [5], Joosen [6], Boese [7], Gerritsma and Beukelman
[8]. These methods have been evaluated by different authors
(Sstrom-Tejsen et al., [9]), and none of them seems to predict
the added resistance accurately over a wide range of ship forms
and speeds. Considering the disadvantages of each of these methods,
two other methods have been developed, in order to allow the
added resistance estimation for any ship type at any speed, and
at any heading.

One has been developed by Faltinsen [10], and the other by
Salvesen [11]. Both are based on the Salvesen, Tuck and Faltinsen
linear strip theory [12], as they use it to define the wave induced
motions. The first one obtains the added resistance by direct
pressure integration, while the second one involves the potential
flow solution. The idea of the paper is to briefly explain and
compare these two methods. The coefficients obtained by the
linear strip theory are used for the numerical calculation of the
required pressures and forces, and the added resistance due to
waves is expressed non-dimensionally. The results are presented
graphically, with the comparison to experimental results for the
available cases.

2 Added resistance estimation

2.1 The linear strip theory

The Salvesen, Tuck and Faltinsen linear strip theory is
common to both methods as a tool to find the wave induced
motion.

The theory assumes the ship to have a slender hull form
with lateral symmetry. The ship is advancing at a constant mean
forward speed \( U \) in sinusoidal waves with an arbitrary heading.
The translatory displacements in the \( x, y \), and \( z \) directions are \( \eta \)
(surge), \( \eta \) (sway) and \( \eta \) (heave), and the angular displacement of
rotational motion about the \( x, y \), and \( z \) axes are \( \eta \) (roll), \( \eta \) (pitch)
and \( \eta \) (yaw) respectively, as shown in Figure 1.

Figure 1 Ship motions

The responses are assumed to be linear and harmonic. The
viscous effects are disregarded, so the fluid motions can be
assumed as irrotational and the problem can be formulated within
the potential flow theory.

The velocity potential for an incident wave, according to
gravity theory, is:

\[
\Phi(x,y,z,t) = \phi_0(x,y,z)e^{-i\omega t},
\]

where \( \omega \) is the encounter frequency, which is related to the wave
frequency \( \omega \) by:

\[
\omega = \omega_e + kU \cos \beta.
\]
free surface, the \( z \) axis is positioned vertically upwards through the centre of gravity of the ship, while the \( x \) axis is in the direction of forward motion.

In the linear strip theory, considering the coordinate system, the spatial incident wave potential can be defined as:

\[
\phi_i = \frac{ig\zeta}{\omega} e^{-i(k(x \cos \beta + y \sin \beta) + \zeta)}
\]

(3)

where \( \zeta \) is the wave amplitude.

Considering the theory, for a slender ship with lateral symmetry, the two linear coupled equations that govern the heave and pitch motions in the frequency domain are:

\[
\sum_{k=\pm 3, 5} \alpha^2 (M_{jk} + A_{jk}) + i\omega B_{jk} + C_{jk} \eta_j = F_j, \text{ for } j = 3 \text{ and } 5.
\]

(4)

The exciting force and moment can be expressed as:

\[
F_j = F_j^I + F_j^D
\]

(5)

The term \( F_j^I \) represents Froude-Krilov force and moment, and \( F_j^D \) represents the diffraction force and moment.

### 2.2 Linear wave induced motions and loads

The time-dependent potential can be divided into three parts:

\[
\phi_0(x, y, z) = \phi_j + \phi_y + \phi_\delta,
\]

(6)

where \( \phi_j \) is the incident wave potential, \( \phi_y \) is the velocity potential due to forced motions in six degrees of freedom, and \( \phi_\delta \) is the diffraction potential of the restrained ship.

According to Faltinsen’s method, after the analysis of each term, the time-dependent velocity potential can be written as:

\[
\phi_\delta e^{-i\omega t} = \phi_j + \phi_y(t) + \phi_\delta = \frac{1}{i \omega} \eta_j + \frac{1}{i \omega} \eta_j + \phi_\delta
\]

(7)

In equation (7) the components \( \eta_j \) and \( \phi_\delta \) are:

\[
\eta_j = \omega \cdot \zeta_0 \sin \beta \cdot e^{izn + ik \cos \beta - \omega n t}
\]

(8)

\[
\phi_\delta = -i \omega \cdot \zeta_0 \cdot e^{izn + ik \cos \beta - \omega n t}
\]

(9)

In the equations (8) and (9) \( z_0 \) is an average vertical cross-sectional coordinate, which can be chosen as \(-T/2\), where \( T \) is the local draught.

The dynamic first order pressure at a fixed submerged point can be expressed as:

\[
p = -\rho \frac{\partial \phi_\delta}{\partial t} + U \frac{\partial \phi_\delta}{\partial x}
\]

(10)

and the dynamic elevation \( \zeta \) can be written as:

\[
\zeta = \frac{1}{\rho g}
\]

(11)

### 2.3 Added resistance by pressure integration method

The pressure can be rewritten with the complete Bernoulli’s equation, and a Taylor expansion of the pressure about the mean position of the ship can be made [10]. Since the wetted surface changes according to the wave amplitude, sink and trim, the pressure \( \rho \) on the ship corrected to second order in wave amplitude may then be written as:

\[
p_i = -\rho g z + \rho \frac{\partial \phi}{\partial t} + \rho \frac{\partial \phi^*}{\partial x} + \rho \frac{\partial \phi^*}{\partial y} + \rho \frac{\partial \phi^*}{\partial z} + \rho \frac{\partial \phi^*}{\partial \theta} + \rho \frac{\partial \phi^*}{\partial \phi}
\]

(12)

In this equation \( \phi \) indicates the wave elevation calculated by the linear theory, and the bar over the expressions means time-averaged values.

\( S_\text{w} \) is the average wetted surface of the body.

### 2.4 The Salvesen method

From the previous considerations, Salvesen’s formula for added resistance has been used as the basic tool of calculation:

\[
R = -\frac{i}{2} k \cos \beta \sum_{j=3, 5} \zeta_j \left( F_{j}^I + F_{j}^D \right) + R_z
\]

(14)

In this equation, \( F_{j}^I \) is the complex conjugate of the Froude-Krilov part of the exciting force and moment, and \( F_{j}^D \) is the same as the diffraction part of the exciting force \( F_{j}^D \), except that in \( F_{j}^D \), the complex conjugate of the incident wave potential, \( \phi_\delta^* \), appears instead of \( \phi_\delta \).

The conjugates of the Froude-Krilov exciting forces are:

\[
F_{j}^I = i \rho \omega \int_S N_j \phi_\delta^* dS \quad F_{j}^D = -i \rho \omega \int_S x N_j \phi_\delta^* dS
\]

(15)

The term \( F_{j}^D \) is closely related to the diffraction force and moment \( F_{j}^D \), and is given by:

\[
\hat{F}_{j}^D = \frac{1}{\zeta} \hat{h}_j(x) dx \quad \hat{F}_{j}^D = -\left( \frac{1}{\zeta} \frac{\partial \hat{h}_j(x)}{\partial x} \right) dx
\]

(16)
Furthermore, the term of “short waves region” can be somehow undefined, since it depends on the ship length. So, according to the ship’s geometry and speed, the expression \( R = b \) can be applied for \( L / \lambda > 1.5 \) and give convincing results.

### 3 Comparison of the results

The calculations using both methods have been done for four ships: the ITTC containership \( S-175 \) \((L_p = 175 \text{ m}, B = 25 \text{ m}, T = 9.5 \text{ m}, C_B = 0.60)\), another containership, the M/V ADEE \((L_p = 117.6 \text{ m}, B = 20.2 \text{ m}, T = 8.3 \text{ m}, C_B = 0.653)\), the Grimaldi Ro-Ro vessel \((L_p = 195.6 \text{ m}, B = 32.25 \text{ m}, T = 9.4 \text{ m}, C_B = 0.73)\) and the bulk carrier \( Stara Planina \) \((L_p = 177 \text{ m}, B = 30 \text{ m}, T = 11.8 \text{ m}, C_B = 0.82)\). The calculations were performed for the following Froude numbers: 0.15, 0.20, 0.25 and 0.30. But to keep the paper’s clarity, only the results for the Froude number 0.20 are presented. Theoretical results obtained by the treated methods for the ITTC containership \( S-175 \) are presented in Figure 3, and a comparison with the available experimental values is also given. The results for the M/V ADEE are reported in Figure 4, for the Ro-Ro in Figure 5, and for the bulk carrier in Figure 6.

All the results are presented non-dimensionally, so the value \( R_{AW} \) represents the added resistance due to waves, reduced to a non-dimensional form by the following equation:

\[
\frac{R_{AW}}{\rho \cdot g \cdot \frac{C_B^2}{\pi} \cdot B^2 / L}
\]  

\( R_{AW} \) is the added resistance and \( \rho \), \( g \) and \( C_B \) are the density of water, the acceleration due to gravity and the sectional draught, respectively.

The numerical results show that:

\[
\begin{align*}
R = a & \quad \text{for } L / \lambda \leq 1 \\
R = a + b & \quad \text{for } 1 < L / \lambda \leq 2 \\
R = b & \quad \text{for } L / \lambda > 2
\end{align*}
\]  

where:

\[
\begin{align*}
a &= \frac{1}{2} \frac{2 \alpha_0 U}{g} \left(1 + \frac{2 \beta U}{g} \right) \int L_1 \sin^3 \theta \, d\eta \\
b &= \frac{1}{2} \frac{2 \alpha_0 U}{g} \left(1 + \frac{2 \beta U}{g} \right) \int \sin^2 \theta \, d\eta \\
\end{align*}
\]
therefore it is corrected by the approximated formula. This can be particularly noticed for the M/V ADEE results, where the discrepancy in the shorter waves region is still present despite the applied correction. For $L/\lambda$ greater than 1.5 some inconsistencies can be noticed in the experimental results, as well in the results obtained by the Salvesen method, which seems to give significant changes of added resistance for a slight change of wave frequency in the mentioned range. For the first three considered ships the results follow the same trend, and the peak values differ within ±15 %, considering a mean value. But for the bulk carrier the results are quite inconsistent, and the cause of this inconsistency might be the form of the hull, which cannot be considered as slender. It has to be pointed out that for all the calculations the ship’s geometry has been described quite roughly, with a modest

![Graph 1](image1)

**Figure 3**  Added resistance for S-175, $Fr = 0.20$

**Slika 3**  Dodatni otpor za S-175, $Fr = 0.20$

![Graph 2](image2)

**Figure 4**  Added resistance for M/V ADEE, $Fr = 0.20$

**Slika 4**  Dodatni otpor za M/V ADEE, $Fr = 0.20$

![Graph 3](image3)

**Figure 5**  Added resistance for Ro-Ro, $Fr = 0.20$

**Slika 5**  Dodatni otpor za Ro-Ro, $Fr = 0.20$

![Graph 4](image4)

**Figure 6**  Added resistance for Bulk Carrier, $Fr = 0.20$

**Slika 6**  Dodatni otpor za Bulk Carrier, $Fr = 0.20$
number of points, and the shape of the stem and stern are not taken into consideration. Therefore, complete precision cannot be expected, but the shape of the curves and the peak values can be taken as accurate enough.

4 Conclusion

A comparison of two methods for added resistance in regular waves has been presented: the Faltinsen method and the Salvesen method. Both methods are well known and widely used, with the exception of the approximation for lower wave lengths in the Salvesen method. Since the Salvesen method seems to overestimate the added resistance in the shorter waves region, this approximation has been applied as an attempt to improve its accuracy.

Since the basic theory of the methods is still being applied, a short overview of both is presented. The calculations are numerical, computed by codes written in Fortran and Matlab. Two containerships have been chosen for the calculations: the SI75 and the M/V ADEE, as well as a bulk carrier and a Ro-Ro ship. The results are non-dimensional, and their absolute values of added resistance can be calculated. When available, a comparison with experimental results is also given. Both methods seem to predict the added resistance in head seas with similar accuracy in the longer waves region, except for the bulk carrier. This is not surprising because it is not a slender hull form, which is one of the basic assumptions of the theory. Therefore the results may be difficult to interpret. Also, the non-dimensional values of added resistance cannot illustrate their influence on total resistance in terms of total loss of speed or increase of power. A percentage value, considering the ship resistance in still water, would allow the prediction of the increase of power required to maintain the ship speed in the given conditions. The comparison between the required power for a ship advancing in still water and in a seaway is actually one of the basic targets of seakeeping calculations.

However, for a preliminary estimation of added resistance in regular waves any of the treated methods can be successfully used, since each of them provides the relevant data on the expected increase of resistance and on the conditions in which it occurs.

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References