

# Drying Kinetics of Poplar (*Populus Deltoides*) Wood Particles by a Convective Thin Layer Dryer

## Kinetika konvektivnog sušenja tankog sloja iverja drva topole (*Populus Deltoides*)

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**ABSTRACT** • Drying of poplar wood (*Populus Deltoides*) particles was carried out at different drying conditions using a laboratory convective thin layer dryer. Drying curves were plotted and in order to analyze the drying behavior, the curves were fitted to different semi-theoretical drying kinetics models. The effective moisture diffusivity was also determined from the integrated Fick's second law equation and correlated with temperature using an Arrhenius-type model to calculate activation energy of diffusion. The results showed that Midilli et al. model was found to satisfactorily describe the drying characteristics of poplar wood particles dried at all temperatures and air flow velocities. In general, the drying rate increases with increasing air temperature and air flow velocity. A short constant drying rate period was observed and drying frequently took place at falling rate period in all cases. The effective moisture diffusivity of poplar wood particles increased from  $1.01E-10$  to  $2.53E-10$   $m^2 \cdot s^{-1}$  as the drying air temperature increased from 65 to 85 °C. The activation energy of diffusion for 1  $m \cdot s^{-1}$  and 1.5  $m \cdot s^{-1}$  air flow velocities were calculated as 27.8  $kJ \cdot mol^{-1}$  and 50.8  $kJ \cdot mol^{-1}$ , respectively.

**Key words:** Poplar wood particles, thin layer dryer, drying kinetics model, effective moisture diffusivity, activation energy

**SAŽETAK** • Pri različitim uvjetima sušenja provedeno je sušenje iverja drva topole (*Populus deltoides*) uporabom konvektivne sušionice za tanki sloj iverja. Iscrtane su krivulje sušenja, a da bi se analizirao proces sušenja, krivulje su prilagođene različitim teorijskim kinetičkim modelima sušenja. Određena je i efektivna difuznost vode u drvu prema Fickovu drugom zakonu te je primjenom Arrheniusova modela za izračun aktivacijske energije difuzije korelirana s temperaturom. Rezultati su pokazali da model Midillija i suradnika zadovoljavajuće opisuje obilježja sušenja iverja drva topole pri svim temperaturama i brzinama strujanja zraka. U načelu, brzina sušenja povećava se s povećanjem temperature zraka i brzine strujanja zraka. Zabilježeno je kratko razdoblje konstantne brzine sušenja, a sušenje se najčešće postiže u razdoblju pada brzine sušenja. Efektivna difuzivnost vode u iverju drva topole povećana je s  $1,01E-10$  na  $2,53E-10$   $m^2 \cdot s^{-1}$  s povećanjem temperature zraka sa 65 na 85 °C. Izračunana je aktivacijska energija difuzije za 1  $m \cdot s^{-1}$  i 1,5  $m \cdot s^{-1}$  brzine strujanja zraka i iznosi 27,8  $kJ \cdot mol^{-1}$  i 50,8  $kJ \cdot mol^{-1}$ .

**Ključne riječi:** iverje drva topole, sušionica tankog sloja iverja, modeli kinetike sušenja, efektivna difuznost vode u drvu, aktivacijska energija

<sup>1</sup> Authors are PhD candidate, full professor and assistant professor at Department of Wood and Paper Sciences and Technology, Faculty of Natural Resources, University of Tehran, Karaj, Iran.

<sup>1</sup> Autori su doktorand, profesor i docent Odjela za znanost i tehnologiju drva i papira, Fakultet prirodnih resursa, Sveučilište u Teheranu, Iran.

## 1 INTRODUCTION

### 1. UVOD

In many developing countries, deforestation and over harvesting from poorly managed forests have brought environmental awareness. As a result, focus was placed on studies dealing with the use of implanted wood resources instead of local forest resources for wood composites production. Therefore, fast growing wood resources such as poplar wood are getting more important as a raw material in particleboard and other wood based panel manufacturing.

Drying of wood particles is one of the main steps in a particleboard production process. Consumption of a high amount of energy, apart from environmental impacts, makes it one of the most energy intensive operations with a great importance in particleboard manufacturing. Hence reducing energy consumption, besides product quality, would be highly important for drying the raw materials used in industry.

Investigation of drying kinetics is one of the best methods to get sufficient information about drying performance. Experimental data from the drying curves can be used in simulation of wood particle drying to optimize the particleboard production process.

Thin layer drying equations are important tools in mathematical modeling of drying. They are practical and give sufficiently good results. To use thin layer drying equations, the drying rate curves have to be known. Thin layer drying generally means to dry sample particles or slices in one layer (Akpınar, 2006). The drying performance of hygroscopic materials can be characterized by measuring the changes in the moisture content as a function of time. Drying kinetics data for wood chips in a steam dryer have been determined by Fyhr and Rasmuson (1996). Ceylan (2008) investigated the drying characteristic of poplar and pine timbers in a heat pump dryer, but there is no information available on thin layer drying of poplar wood particles. Laboratory based modeling is needed to characterize the thin layer drying process of poplar wood particles, as full scale studies are both expensive and time consuming (Ghazanfari *et al.*, 2006). Therefore, the objectives of this study were to investigate the drying characteristics of poplar wood particles in a hot air convective thin layer dryer and fit the best model for the drying performance of poplar wood particles. In addition, the drying kinetics, moisture effective diffusivities, and activation energies of diffusion at different drying conditions will be computed.

## 2 MATERIALS AND METHODS

### 2. MATERIJAL I METODE

#### 2.1 Raw material

##### 2.1.1. Sirovina

The poplar wood (*Populus Deltoides*) used in this study was supplied from research and educational forest, Khyroudkenar, Noshahr (longitude: 51° 31', Altitude: 36° 39', latitude: -20 m), managed by University of Tehran, Iran. The 20 years old tree trunks were

sliced and cut into long strands using an industrial slicer in Rokesh Choobi factory, Gazvin, Iran. The strands were cut into slice shape particles with approximate target dimensions of 1x20x30 mm using a laboratory clipper. The wood particles with the moisture content of around 0.2 kg water/kg dry material were wetted by distilled water to around 1.6 kg water/kg dry material and finally they were kept in sealed plastic bags and stored in a 0-4 °C refrigerator to reach equilibration of moisture content without deterioration, for 72 hours before drying.

#### 2.2 Drying procedure

##### 2.2. Postupak sušenja

The homogeneously moistened wood particles that had been stored in plastic bags, were placed and spread on three perforated trays, in one layer (about 20 g of dry wood particles on each tray), and put into hot air duct on digital balance, which was connected to a computer. Drying experiments were performed at hot air temperatures of 65, 75, and 85 °C with air flow velocities of 1 and 1.5 m·s<sup>-1</sup> in a laboratory-scale convective thin layer dryer. The initial weight of each sample was measured by an electronic digital balance (GF3000, ±0.02, A& D, Japan). The dryer was set to the selected drying temperatures and air flow velocities for about 30 min to achieve the steady-state conditions before the samples were placed in the duct. The temperatures were measured by means of LM35 sensor (LM35, ±1 °C, NSC, USA), the air flow velocities were measured using an anemometer (V- sensor, 405- VI, ±3 %, TESTO, UK) and the relative humidity of fresh air was measured using a humidity probe (RH-sensor, Capacitive, ± 3 %, PHILIPS, UK). The relative humidity of fresh air was constant (17 %) throughout the experiments. The weight losses of the samples were measured and automatically recorded at 10 second intervals until equilibrium moisture content (EMC) was achieved. Finally, the dried poplar wood particles were put into an oven at 103 ±2 °C for getting equilibrium moisture content. The initial moisture content and equilibrium moisture content were calculated using ASAE, 2001 equations:

#### 2.3 Mathematical modeling of drying and data analysis

##### 2.3. Matematičko modeliranje sušenja i analiza podataka

The form of Newton's law of cooling in heat transfer (equation 1) is often used to describe the moisture loss in thin layer drying (Brooker and Bakker-Arkema, 1974). Based on this law, the drying rate is proportional to the difference in moisture content between the material being dried and the equilibrium moisture content at the drying conditions as:

$$\frac{dM}{dT} = -k(M - M_e) \quad (1)$$

The solution of (1), assuming  $k$  is independent of  $M$  and  $M_e$ , is:

$$MR_{Newton} = \exp(-kt) \quad (2)$$

Where  $MR$  is the dimensionless moisture ratio given by:

$$MR = \frac{M - M_e}{M_0 - M_e} \quad (3)$$

In order to determine the moisture ratio as a function of drying time, drying curves obtained in this experiment were fitted with four different models of moisture ratio thin layer drying obtained from the literature (Table 1).

**Table 1** Mathematical models applied to the drying curves  
**Tablica 1.** Matematički modeli primijenjeni za krivulje sušenja

Model name <i>Naziv modela</i>	Model equation <i>Jednadžba modela</i>	Reference <i>Referenca</i>
Newton	$MR = \exp(-kt)$	O'Callaghan <i>et al.</i> , 1971
Page	$MR = \exp(-kt^n)$	Pang, 1949
Henderson & Pabis	$MR = a \exp(-kt)$	Guarte, 1996; Chninman, 1984
Midilli <i>et al.</i>	$MR = a \exp(-kt^n) + bt$	Midilli <i>et al.</i> , 2002

The goodness of fit of each model to the experimental data was evaluated from the coefficient of determination ( $R^2$ ), root mean square error ( $RMSE$ ), reduced chi-square ( $\chi^2$ ), and mean bias error ( $MBE$ ).  $R^2$  was used as the primary comparison criteria for selecting the best model to fit the four models to the experimental data. Also, a model is considered better than another if it has a lower value of the  $MBE$ ,  $RMSE$ , and  $\chi^2$ . The expressions for each of these parameters are stated as follows:

$$R^2 = \frac{\sum_{i=1}^N (M_{R_i} - M_{R_{pre,j}}) * (M_{R_i} - M_{R_{exp,j}})}{\sqrt{[(\sum_{i=1}^N (M_{R_i} - M_{R_{pre,j}})^2) * (\sum_{i=1}^N (M_{R_i} - M_{R_{exp,j}})^2)]}} \quad (4)$$

$$\chi^2 = \frac{\sum_{i=1}^N (M_{R_{exp,j}} - M_{R_{pre,j}})^2}{N - n} \quad (5)$$

$$RMSE = \left[ \frac{1}{N} \sum_{i=1}^N (M_{R_{pre,j}} - M_{R_{exp,j}}) \right]^{\frac{1}{2}} \quad (6)$$

$$MBE = \frac{1}{N} \sum_{i=1}^N (M_{R_{pre,j}} - M_{R_{exp,j}}) \quad (7)$$

The  $MBE$  provides information on the long term performance of the correlations by allowing a comparison of the actual deviation between predicted and measured values term by term. The ideal value of  $MBE$  is 'zero'.

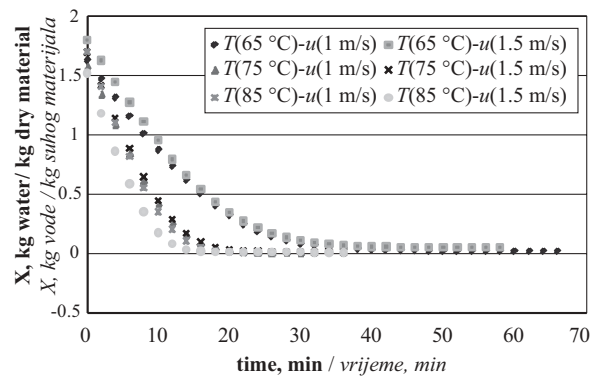
### 3 RESULTS AND DISCUSSION

#### 3. REZULTATI I RASPRAVA

##### 3.1 Experiments of drying kinetics

##### 3.1. Eksperimenti kinetike sušenja

Drying curves for the different temperatures and velocities of hot air in drying poplar wood particles are



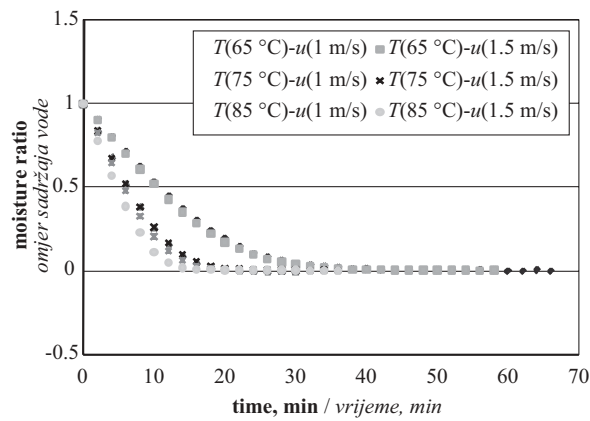
**Figure 1** Drying curves (moisture content vs. time) for poplar wood particles under different hot air drying conditions

**Slika 1.** Krivulje sušenja (sadržaj vode u ovisnosti o vremenu sušenja) za iverje drva topole pri različitim uvjetima sušenja vrućim zrakom

shown in Figures 1-4. Numerical differentiation of the experimental drying curve data was used to obtain the drying rate curves. Poplar wood particles with an average initial moisture content of around 1.6 kg water/kg dry material were dried to the final moisture content of about 0.008 kg water/kg dry material. It is evident from these curves that the moisture content continuously decreased with the drying time. The drying rate was higher for wood particles dried at higher temperatures than that of particles dried at lower temperatures for the same average moisture content.

The moisture ratio of samples reduced exponentially as the drying time increased. These curves show an increase of drying rate, given by the curve slope, with an increase in temperature (Figure 1). This is in agreement with the results of the previous studies (Mazza and Maguer, 1980; Lopez *et al.*, 2000). At higher temperatures, the relative humidity of the drying air was less than that of the drying air at lower temperatures. Hence, the difference in the partial vapor pressure between the surface of wood particles and the surrounding drying air at higher temperatures would be higher than the one at lower temperatures. Consequently, the moisture transfer rate is increased at higher temperature (Kaleemullah and Kailappan, 2005).

Figures 1 and 2 clearly show that the air temperature along with air velocity had a significant effect on the moisture content of the samples. Drying process is not only more rapid at higher temperatures but also faster at higher velocities (Figure 3). During the experiments of hot air drying, the time to reach the final moisture content for the samples was found to be between 27 and 67 min at different drying conditions. An increase in the air temperature and air velocity resulted in an increase in the drying rate and consequently a decrease in the drying time. Previous studies have reported similar trends (Ertekin and Yaldiz, 2004; Fritzell *et al.*, 2009; Ghazanfari *et al.*, 2006). As can be seen, drying rate at the initial stage of the drying period is rather low, which may be due to the activation energy and increase of the temperature of wood water content. At

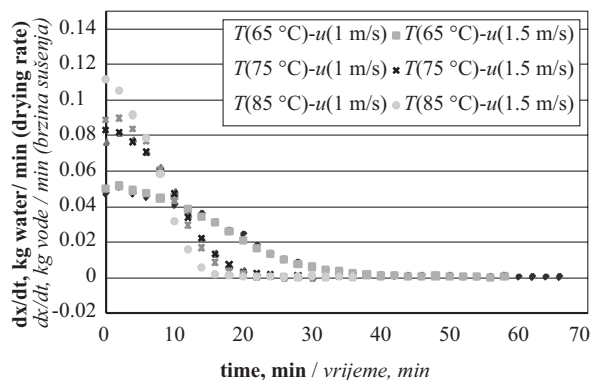


**Figure 2** Drying curves (moisture ratio vs. time) for poplar wood particles under different hot air drying conditions  
**Slika 2.** Krivulje sušenja (sadržaj vode u ovisnosti o vremenu sušenja) za iverje drva topole pri različitim uvjetima sušenja vrućim zrakom

the beginning, when the moisture content was high, the drying rate was very high, and as the moisture content approached the equilibrium moisture content, the drying rate was very low (Figure 2). This is in good agreement with the results of Kaleemullah and Kailappan (2005), Lopez *et al.* (2000) and Mazza and Maguer (1980).

Drying rate vs. average moisture content curves (Krischer curves) for wood particles at different drying air temperatures are shown in Figure 4. To eliminate the scattering of curves, each drying rate curve was smoothed using a second-order polynomial (Kemp *et al.*, 2001).

Generally, the product is dried at a constant rate, and for hygroscopic products, after a falling rate period, the decrease stops and the equilibrium is established. As shown in Figure 4, all drying periods can be observed in the curves for poplar wood particles made by Krischer. At the early stage of drying, known as the induction period, the wet solid temperature rises to a constant (equilibrium) value (Montazer-Rahmati and Amini-Horri, 2001) then, a short constant rate period begins. In the constant rate period of drying, external conditions such as temperature, air flow velocity, rela-



**Figure 3** Drying rate curves for poplar wood particles under different hot air drying conditions  
**Slika 3.** Krivulje brzine sušenja iverja drva topole pri različitim uvjetima sušenja vrućim zrakom

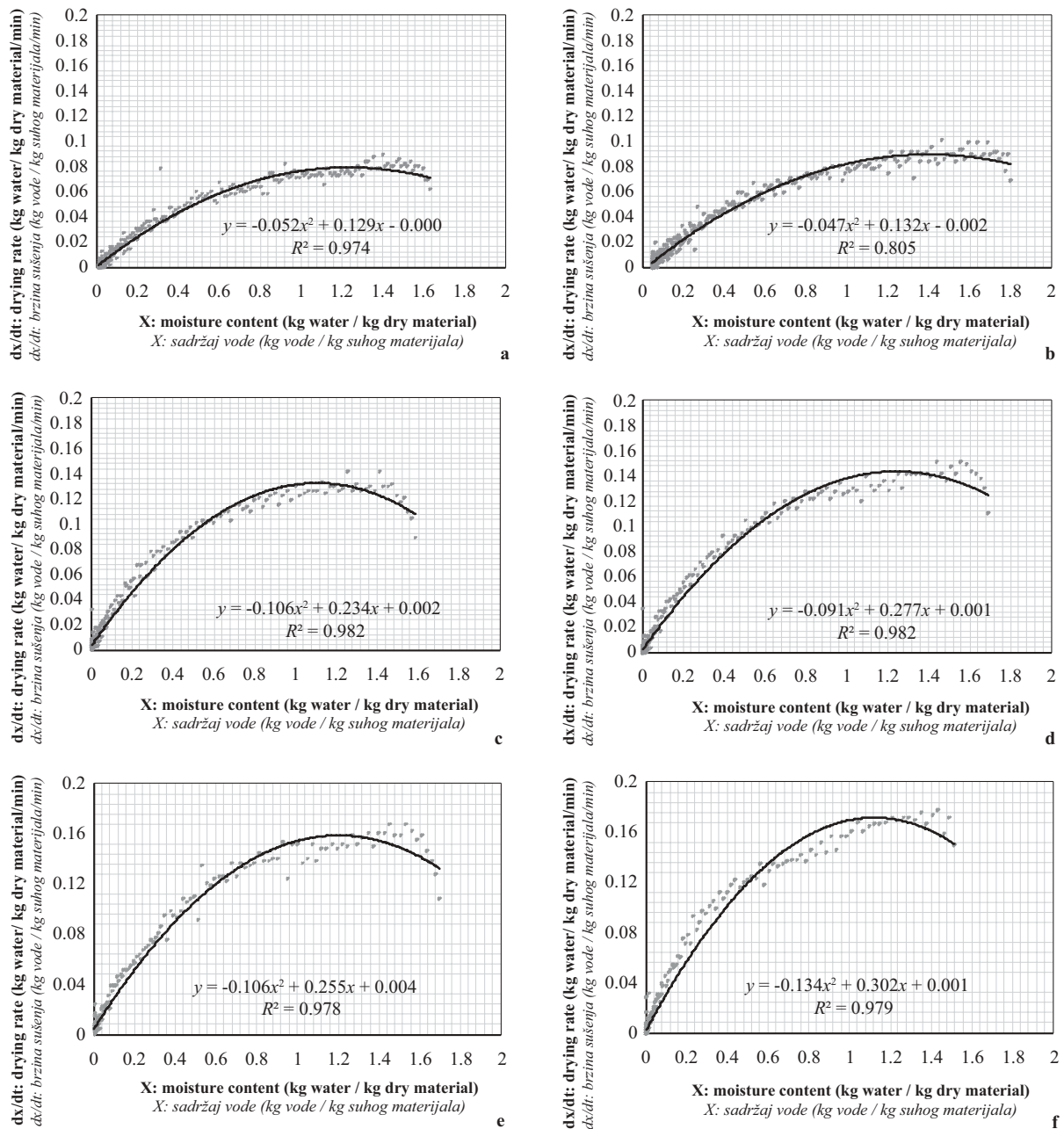
tive humidity of the medium and physical form of the wood particles control the drying process and the surface diffusion is the dominant diffusion mechanism. Toward the end of the constant rate period, moisture has to be transported from the inside of the solid material to the surface by capillary forces and the drying rate may still be constant until the moisture content has reached the critical moisture content, and the surface film of the moisture has been so reduced that dry spots appear on the surface. Then the first falling rate period or unsaturated surface drying begins. Since, however, the rate is computed with respect to the overall solid surface area, the drying rate falls even though the rate per unit of wet solid surface area remains constant (Menon, 1995). In this drying period, liquid diffusion is the dominant diffusion mechanism due to moisture concentration difference and internal conditions such as moisture content, temperature, and wood particles structure. When the surface film of the liquid is entirely evaporated, the subsequent falling rate period begins. In the second falling rate period of drying, vapor diffusion is the dominant diffusion mechanism as moisture concentration difference and internal conditions are still very important (Husain *et al.*, 1972).

Referring to the curves, the critical point is approximately 1.4 kg water/kg dry material. This high critical moisture content is attributed to the hygroscopicity of wood substance. As mentioned above, wood particles did not show a distinct constant rate period throughout the drying process (Figure 4) and drying mostly took place in the falling rate period. Pang *et al.* (1997), Husain *et al.* (1972) and Fritzel *et al.* (2009) show in their investigations that there was a constant rate period during the drying of veneer and wood fibers. Bakshi and Singh (1980) state that although biological materials have high moisture content, generally no constant rate period is seen in the drying processes. Similar results have been presented by Chandy *et al.* (1992), Freire *et al.* (2001), Kaleemullah and Kailappan (2005) and Vijayaraj *et al.* (2007). Although materials are generally dried without a constant rate period, Erbay and Icier (2010) state that sometimes there is an overall constant rate period at the initial stages of drying. The short constant rate period that can be seen at the beginning of the drying process may be attributed to evaporation of superficial water, retained on the surface of wood particles after removing the excessive water, making the sample surfaces wet during this period.

### 3.2 Fitting of the drying curves

#### 3.2. Prilagodba krivulja sušenja

So far, numerous models have been proposed to describe the behavior of thin layer drying kinetics. In this study, four different models were fitted to the experimental drying curve data at different drying conditions (Table 1). The results of the statistical analysis and the estimated values of the parameters for these models have been listed in Table 2. The results show that all the four models gave a good fit to the experimental data with a value greater than 0.96 for  $R^2$ . Among the models, the Midilli *et al.* model showed the



**Figure 4** Krischer curves for poplar wood particles drying. a)  $T=65\text{ }^{\circ}\text{C}$ ,  $u=1\text{ m}\cdot\text{s}^{-1}$ ; b)  $T=65\text{ }^{\circ}\text{C}$ ,  $u=1.5\text{ m}\cdot\text{s}^{-1}$ ; c)  $T=75\text{ }^{\circ}\text{C}$ ,  $u=1\text{ m}\cdot\text{s}^{-1}$ ; d)  $T=75\text{ }^{\circ}\text{C}$ ,  $u=1.5\text{ m}\cdot\text{s}^{-1}$ ; e)  $T=85\text{ }^{\circ}\text{C}$ ,  $u=1\text{ m}\cdot\text{s}^{-1}$ ; f)  $T=85\text{ }^{\circ}\text{C}$ ,  $u=1.5\text{ m}\cdot\text{s}^{-1}$

**Slika 4.** Krischerove krivulje sušenja iverja drva topole: a)  $T=65\text{ }^{\circ}\text{C}$ ,  $u=1\text{ m}\cdot\text{s}^{-1}$ ; b)  $T=65\text{ }^{\circ}\text{C}$ ,  $u=1,5\text{ m}\cdot\text{s}^{-1}$ ; c)  $T=75\text{ }^{\circ}\text{C}$ ,  $u=1\text{ m}\cdot\text{s}^{-1}$ ; d)  $T=75\text{ }^{\circ}\text{C}$ ,  $u=1,5\text{ m}\cdot\text{s}^{-1}$ ; e)  $T=85\text{ }^{\circ}\text{C}$ ,  $u=1\text{ m}\cdot\text{s}^{-1}$ ; f)  $T=85\text{ }^{\circ}\text{C}$ ,  $u=1,5\text{ m}\cdot\text{s}^{-1}$

best fit ( $R^2 > 0.99$ ) followed by the Page, Henderson & Pabis and Newton models. Also, the values for  $RMSE$ ,  $\chi^2$  and  $MBE$  attained from the Midilli *et al.* model were less than the values from other models generally followed by the Page, Henderson & Pabis and Newton models. Therefore, the Midilli *et al.* model was considered the best model to represent the behavior of thin layer drying of poplar wood particles within the experimental range of this study (Table 2).

To account for the effect of the drying variables on the Midilli *et al.* model constants  $k$ ,  $a$ ,  $b$  and coefficient  $n$ , the predicted values were correlated as a function of drying air temperature and air flow velocity using multiple regression analysis (Eqs. 9-11). Based on this analysis, the Midilli *et al.* model constants and

coefficient were expressed in terms of drying air temperature  $T$  ( $^{\circ}\text{C}$ ) and air flow velocity  $u$  ( $\text{m}\cdot\text{s}^{-1}$ ) as:

$$MR = a \cdot \exp(-kt^n) + b \cdot t \quad (8)$$

$$k = -0.11569 + 0.001718 \cdot T + 0.014 \cdot u \quad (9)$$

$$a = 0.9699 - 2.5 \cdot 10^{-5} - 0.00622 \cdot u \quad (10)$$

$$n = 1.3798 + 0.002458 \cdot T - 0.0522 \cdot u \quad (11)$$

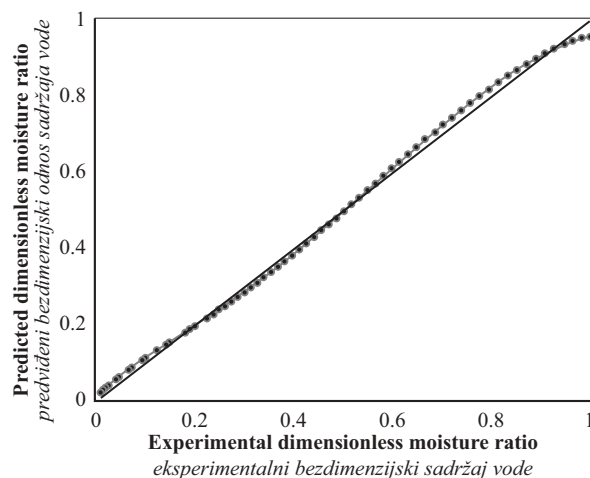
$$b = -0.00077 + 7.99 \cdot 10^{-6} \cdot T + 0.000016 \cdot u \quad (12)$$

These functions can be used to estimate the moisture ratio of poplar wood particles with a high accuracy and are valid for the above mentioned conditions.

**Table 2.** Statistical analysis for the four models at different drying conditions**Tablica 2.** Statistička analiza za četiri modela kinetike sušenja pri različitim uvjetima sušenja

Drying condition Uvjeti sušenja		Model Model	Model parameter Parametri modela	$R^2$	RMSE	$\chi^2$	MBE
$T, ^\circ\text{C}$	$u, \text{m}\cdot\text{s}^{-1}$						
65	1	Newton	$k=0.078$	0.977	0.04263	0.001822	0.006951
		Page	$k=0.028, n=1.373$	0.999	0.010607	0.000113	0.001124
		Henderson & Pabis	$a=1.119, k=0.086$	0.986	0.033157	0.001105	0.010399
		Midilli <i>et al.</i>	$a=0.961, k=0.021, n=1.46,$ $b=3.39\text{E-}5$	0.999	0.00765	5.91E-05	0.00138
65	1.5	Newton	$k=0.081$	0.977	0.043715	0.001917	0.007439
		Page	$k=0.03, n=1.364$	0.999	0.00963	9.33E-05	0.002838
		Henderson & Pabis	$a=1.117, k=0.089$	0.986	0.033799	0.001149	0.011824
		Midilli <i>et al.</i>	$a=0.964, k=0.023, n=1.436,$ $b=7.2\text{E-}5$	1	0.007277	5.36E-05	0.003065
75	1	Newton	$k=0.133$	0.967	0.054237	0.002957	0.009375
		Page	$k=0.049, n=1.449$	0.998	0.054237	0.002973	0.00491
		Henderson & Pabis	$a=1.136, k=0.149$	0.98	0.042116	0.001793	0.014393
		Midilli <i>et al.</i>	$a=0.965, k=0.04, n=1.522, b=0.0$	0.999	0.008869	8.03E-05	0.002949
75	1.5	Newton	$k=0.135$	0.974	0.045899	0.002116	0.009049
		Page	$k=0.055, n=1.405$	0.998	0.011272	0.000128	0.004173
		Henderson & Pabis	$a=1.123, k=0.15$	0.984	0.036185	0.001321	0.011928
		Midilli <i>et al.</i>	$a=0.959, k=0.043, n=1.497,$ $b=9.6\text{E-}5$	0.999	0.007993	6.50E-05	0.00018
85	1	Newton	$k=0.149$	0.967	0.054877	0.00303	0.008771
		Page	$k=0.059, n=1.438$	0.998	0.01267	0.000163	0.005302
		Henderson & Pabis	$a=1.132, k=0.166$	0.998	0.042968	0.001869	0.014854
		Midilli <i>et al.</i>	$a=0.965, k=0.049, n=1.505, b=0.0$	0.999	0.009844	9.94E-05	0.003714
85	1.5	Newton	$k=0.181$	0.975	0.041127	0.001699	0.007482
		Page	$k=0.081, n=1.413$	0.998	0.012093	0.000148	0.004051
		Henderson & Pabis	$a=1.121, k=0.20$	0.984	0.033194	0.001112	0.009962
		Midilli <i>et al.</i>	$a=0.952, k=0.062, n=1.528,$ $b=5.45\text{E-}5$	0.999	0.0092	8.62E-05	0.000312

The accuracy of the established model was evaluated by comparing the computed moisture ratios with the observed values as shown in Figure 5. The close agreement between the measured and the predicted moisture contents gives confidence in applying the mo-



**Figure 5** Experimental moisture ratio vs. predicted moisture ratio from Midilli *et al.* model for constant  $T=85^\circ\text{C}$ ,  $u=1.5\text{ m}\cdot\text{s}^{-1}$

**Slika 5.** Eksperimentalni sadržaj vode u odnosu na predviđeni omjer sadržaja vode prema modelu Midillija i suradnika za konstante  $T=85^\circ\text{C}$ ,  $u=1,5\text{ m}\cdot\text{s}^{-1}$

del to examine the influence of wood particles variables and drying conditions on the drying rate.

### 3.3 Calculation of effective moisture diffusivity and activation energy of diffusion

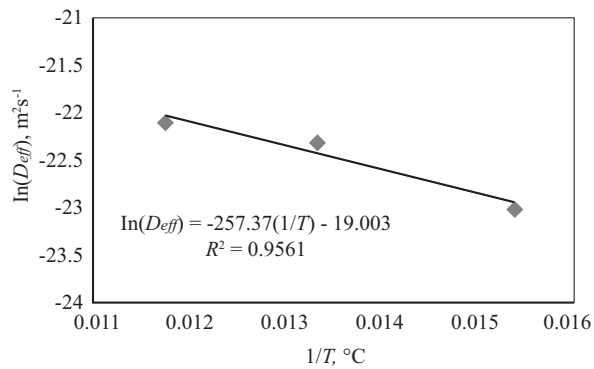
#### 3.3. Izračun efektivne difuznosti vode u drvu i aktivacijske energije difuzije

In describing a drying process during the falling rate period, the concept of effective moisture diffusivity ( $D_{eff}$ ) has been accepted as the basic mechanism of moisture movement inside the drying material (Reyes *et al.* 2004). As mentioned in the previous sections, the drying of wood particles mostly occurs in the falling rate period and liquid diffusion controls the process. Fick's second law of diffusion can be used to model the drying behavior of wood particles. The following analytical solution for diffusion in an infinite planar slab was given by Akpinar, 2006:

$$MR = \frac{M}{M_o} = \frac{8}{\pi^2} \sum_{n=1}^{\infty} \frac{1}{(2n-1)^2} \exp\left[-\frac{(2n-1)^2 \pi^2 Dt}{4L^2}\right] \quad (13)$$

Only the first term of equation (6) is used for long drying times (Lopez *et al.*, 2000), hence:

$$MR = \frac{8}{\pi^2} \exp\left[-\frac{\pi^2 Dt}{4L^2}\right] \quad (14)$$



**Figure 6** Relationship between the effective moisture diffusivity ( $D_{eff}$ ) and the reciprocal of absolute temperature ( $1/T$ )

**Slika 6.** Odnos između efektivne difuznosti vode u drvu ( $D_{eff}$ ) i recipročne vrijednosti apsolutne temperatura ( $1/T$ )

From equation (7), a plot of  $\ln(MR)$  versus time gives a straight line with a slope of  $k_o$  given by:

$$k_o = \frac{\pi^2 D}{4L^2} \quad (15)$$

The activation energy of diffusion was calculated using an Arrhenius type equation (Akpinar *et al.*, 2003; Lopez *et al.*, 2000):

$$D = D_o \exp\left[-\frac{E_a}{RT_a}\right] \quad (16)$$

Where  $E_a$  is the energy of activation ( $\text{kJ}\cdot\text{mol}^{-1}$ ),  $R$  is universal gas constant ( $8.3143 \text{ kJ}\cdot\text{mol}^{-1} \text{ K}$ ),  $T_a$  is absolute air temperature ( $\text{K}$ ), and  $D_o$  is the pre-exponential factor of the Arrhenius equation ( $\text{m}^2\cdot\text{s}^{-1}$ ). The activation energy can be determined from the slope of the Arrhenius plot,  $\ln(D)$  versus  $1/T_a$ . From Equation (9), a plot of  $\ln(D)$  versus  $1/T_a$  gives a straight line whose slope is  $k_1$ , given by:

$$k_1 = \frac{E_a}{R} \quad (17)$$

In the above equations, isothermal assumption was used and  $T$  is the ambient air temperature of the dryer duct.

The effective moisture diffusivity  $D_{eff}$  of poplar wood particles increased from  $1.01\text{E}-10$  to  $2.53\text{E}-10 \text{ m}^2\cdot\text{s}^{-1}$  as the drying air temperature increased from  $65$  to  $85 \text{ }^\circ\text{C}$ , and increased from  $1.69\text{E}-10$  to  $2.03\text{E}-10 \text{ m}^2\cdot\text{s}^{-1}$  as the air flow velocity increased from  $1$  to  $1.5 \text{ m}\cdot\text{s}^{-1}$ . As can be deduced, the effect of hot air temperature on effective moisture diffusivity is higher than that of air flow rate. The plot depicting the relationship between  $\ln(D_{eff})$  and  $1/T$  was found to be a straight line in the range of temperatures investigated, indicating Arrhenius dependence (Figure 6). The activation energy of diffusion  $E_a$  for  $1 \text{ m}\cdot\text{s}^{-1}$  and  $1.5 \text{ m}\cdot\text{s}^{-1}$  air velocity were also calculated as  $27.8 \text{ kJ}\cdot\text{mol}^{-1}$  and  $50.8 \text{ kJ}\cdot\text{mol}^{-1}$ , respectively.

## 4 CONCLUSION

### 4. ZAKLJUČAK

At the end of this study, the following conclusions can be drawn:

The Midilli *et al.* model is quite suitable for predicting the drying curve behavior of poplar wood particles in the temperature range of  $65\text{--}85 \text{ }^\circ\text{C}$ .

Constant drying rate period is very short in any of the experiments and the drying process of the poplar wood particles is mostly carried out at the falling rate period.

Effective moisture diffusivity of poplar wood particles increases with increasing air temperature and air flow velocity in the range of  $1.01\text{E}-10$  to  $2.53\text{E}-10 \text{ m}^2\cdot\text{s}^{-1}$ .

The activation energy of diffusion for  $1 \text{ m}\cdot\text{s}^{-1}$  and  $1.5 \text{ m}\cdot\text{s}^{-1}$  air flow velocities were calculated as  $27.8 \text{ kJ}\cdot\text{mol}^{-1}$  and  $50.8 \text{ kJ}\cdot\text{mol}^{-1}$ , respectively.

## 5 NOMENCLATURE

### 5. OPIS ZNAKOVA

$a, n, b$	Dimensionless drying constants in drying models / <i>bezdimezionalne konstante u modelima sušenja</i>
$k$	Drying velocity constant in drying models ( $\text{min}^{-1}$ ) / <i>konstanta brzine sušenja u modelima sušenja</i>
$L$	Particles half thickness (m) / <i>polovica debljine iverja</i>
$M$	Moisture content at any time (% dry basis) (kg water/kg dry material) / <i>trenutačni sadržaj vode (% u odnosu prema suhome materijalu) (kg vode / kg suhog materijala)</i>
$MBE$	Mean bias error / <i>srednja pogreška</i>
$MR$	Moisture ratio / <i>omjer sadržaja vode</i>
$R$	Universal gas constant ( $8.3143 \text{ kJ mol}^{-1}\cdot\text{K}^{-1}$ ) / <i>opća plinska konstanta</i>
$N$	Total number of observation / <i>ukupni broj zapažanja</i>
$n$	Number of constants / <i>broj konstanti</i>
$n$	Number of terms / <i>broj uvjeta</i>
$R^2$	Coefficient of determination / <i>koeficijent determinacije</i>
$RH$	Relative humidity in drying chamber / <i>relativna vlažnost zraka u sušionici</i>
$RMSE$	Root mean square error / <i>korijen srednje kvadratne pogreške</i>
$D$	Diffusivity ( $\text{m}^2\cdot\text{s}^{-1}$ ) / <i>difuznost</i>
$E$	Energy ( $\text{kJ}\cdot\text{mol}^{-1}$ ) / <i>energija</i>
$T$	Temperature ( $^\circ\text{C}$ ) ( $^\circ\text{K}$ ) / <i>temperatura</i>
$t$	Time (min) / <i>vrijeme</i>
$u$	Air flow velocity ( $\text{m}\cdot\text{s}^{-1}$ ) / <i>brzina strujanja zraka</i>
$x$	Moisture content (kg water / kg dry material) / <i>sadržaj vode u drvu (kg/vode / kg suhog materijala)</i>
	<i>Greek symbols</i>
$\chi^2$	Reduced chi-square / <i>reducirani Hi-kvadrat</i>
	<i>Subscripts</i>
$0$	Initial / <i>početno stanje</i>
$i$	$i$ th order / <i>i-ti red</i>
$crit$	Critical / <i>kritično</i>
$e$	Equilibrium / <i>ravnoteža</i>
$exp$	Experimental / <i>eksperimentalni</i>
$a$	Activation / <i>aktivacija</i>
$a$	Air / <i>zrak</i>
$eff$	Effective / <i>efektivno</i>
$m$	Mean / <i>prosječno</i>
$pre$	Predicted / <i>predviđeno</i>

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**Corresponding address:**

Prof. HAMID ZAREA HOSSEINABADI, Ph.D.

Department of Wood and Paper Sciences

and Technology

Faculty of Natural Resources

University of Tehran

P.O Box: 31585 4314

Karaj, IRAN

E-mail: hzareah@ut.ac.ir, zare.hamid@gmail.com