Introduction

Increased global industrialization has led to a steep rise in the demand for energy. The global demand for energy is expected to increase by about 1.6 % per annum from 2011 to 2030\(^1\). Fossil fuels are expected to remain the main energy source in the world, but in the meantime renewable energy sources (wind, solar, geothermal, bioenergy) are the world’s fastest-growing energy sources, increasing by 2.5 percent per year\(^2\). However, the reserves of fossil fuels are limited, and their large-scale use is associated with environmental deterioration\(^3,4\). The negative effects of using fossil fuels include acid rain, ozone layer depletion, and global climate change\(^5\). The increase in oil price and the growing interest in environmental issues have recently given a considerable impetus to the research for cleaner and renewable energy sources.

Biodiesel, which consists of long-chain Fatty Acid Methyl Esters (FAME) obtained from renewable lipids, such as those in vegetable oils or animal fat, can be used both as an alternative fuel and as an additive for petroleum diesel. As much as 70–80 % of the cost of biodiesel is associated with the cost of raw material. Using a low-cost raw material, such as crude oils, acid oils, waste oils or high FFA rice bran oil (RBO) to produce biodiesel is important in reducing the cost of biodiesel production\(^6\).

Nevertheless, the biggest challenge in using FFA feedstock is that, during transesterification, these feedstocks easily undergo the saponification reaction leading to soap formation. Saponification results in reduced biodiesel yields, hinders separation of the ester from glycerin and reduces the formation rate of FAME\(^7,8\). Therefore, alkaline catalysts cannot directly catalyze the transesterification of oils containing high FFA. For alkaline transesterification to take place, the FFA level in the oil should be below a desired level (ranging from less than 0.5 % to less than 3 %)\(^9\). As a result, a two-step process is usually employed to prepare biodiesel from high FFA feedstocks. In the first step, the raw material undergoes acid pretreatment before being subjected to alkali-catalyzed transesterification. The acid-catalyzed chemical reaction, also referred to as esterification, involves the reaction of FFAs and alcohol, yielding fatty acid alkyl ester and water\(^10\).

The reduction of free fatty acids (FFA) in rice bran oil (RBO) with methanol in the presence of sulfuric acid as a homogeneous catalyst was studied. The effects of catalyst concentration (0.15 to 1.0 wt%), reaction temperature (318 K to 333 K), and molar ratio of oil to methanol (1:5 to 1:30) on the conversion of FFA were investigated to optimize the conditions for maximum conversion of FFAs. A detailed kinetic study was carried out using second-order pseudo-homogeneous kinetic model. The kinetic parameters were obtained and activation energy was determined from the Arrhenius plot. The activation energy of 23.21 kJ mol\(^{-1}\) and pre-exponential factor of 32.65 L mol\(^{-1}\) min\(^{-1}\) was obtained under the optimum catalyst concentration of 0.5 wt %, stirring speed of 500 rpm and oil to methanol ratio 1:20.

Key words: biodiesel, esterification, high free fatty acid oil, homogeneous catalyst, kinetics
tion. Rice bran, the cuticle between the paddy husk and the rice grain and is obtained as a by-product of rice processing, is the main source of RBO. The annual world rice cultivation yields approximately 47 million tons of rice bran, from which about 9 million tons of RBO could be available for the production of biodiesel. Maximum production of rice is in Asian countries and the prospective biodiesel production from RBO in Asian countries is about 10 billion liters, which amounts to approximately 10 % of Asia’s diesel requirements. Rice bran contains 15–27 % oil, while crude RBO from fresh rice bran contains 6–8 % FFA. Due to the presence of active enzymes in rice bran, the FFA content in rice bran during storage increases by 1–7 % per day. The crude RBO can be refined to edible oil only if the FFA content in the oil is less than 10 %. It is not possible to extract RBO immediately after the milling of rice, due to which most of the high FFA rice bran remains underutilized.

Due to the huge availability of high FFA-RBO, the unavoidable need to remove FFA and the requirement of characterizing the kinetics of the reaction with a view to optimizing the reactor dimensions led us to undertake the present work. The influence of operational variables on the kinetics of the esterification of FFA in RBO using sulfuric acid as catalyst were studied. The reaction kinetics were developed based on pseudo-homogeneous, first-order in forward direction and second-order esterification of FFA.

Materials and methods

Materials

Raw high FFA-RBO was purchased from the solvent extraction unit located near Chandigarh (India), which was filtered with a 10 micron filter cloth. The acid value was determined to be 24 mg KOH g⁻¹ oil. The average molecular weight of RBO is calculated based on its FFA and TG content, assuming a molecular weight of 870 for TG and 282 for FFA¹. The chemicals used in esterification were methyl alcohol (99.0 % purity) and H₂SO₄ (98 % purity), which were purchased from SD Fine Chemicals (India). The reagents used in the free fatty acids determination included potassium hydroxide (KOH, 99.9 % purity), ethanol (99.9 % purity), diethyl ether and phenolphthalein indicator, which were also purchased from SD Fine Chemicals (India). All the chemicals and reagents were of analytical grade.

Esterification

The esterification was carried out in a 500-mL water-jacketed flat-bottom glass batch reactor working with total reflux. An amount of 100 gm of RBO was preheated to the required temperature (varied from 318 K to 333 K). Varying quantities of sulfuric acid as catalyst (0.15 to 1.0 wt%) were mixed in methanol (oil to methanol molar ratio varying from 1:5 to 1:30) and the resulting mixture was allowed to react with the preheated oil. The reaction was carried out for 2 hours using a temperature-controlled magnetic stirrer having one-inch magnetic bead. Samples were collected at different time intervals (5, 15, 30, 50, 70, 90 and 120 min), washed with distilled water to remove residual acid and impurities, dried to remove residual water and tested for acid value.

All experiments were carried out at atmospheric pressure. The standard error obtained in the calculation of the acid value was ± 1–2 % for the duplicate set of reactions.

FFA analysis

The sample collected from the reaction was weighed and then dissolved in diethyl ether-ethanol solution. The mixture was titrated against standard KOH solution of known normality with phenolphthalein as an indicator. The acid value (AV) of the sample is defined as follows:

\[
\text{AV} = \frac{M_w \cdot c \cdot V}{m}
\]  

(1)

where \(M_w\) is the molecular weight of KOH, \(c\) is the molar concentration of KOH, \(V\) is the volume of KOH used in the titration process, and \(m\) is the sample weight. Once the acid value is determined, the FFA conversion can be calculated as follows:

\[
X = \left(1 - \frac{AV}{AV_0}\right)
\]  

(2)

where \(X\) is the FFA conversion and \(AV_0\) is the initial acid value before the esterification reaction.

Results and discussion

The esterification using H₂SO₄ as acid catalyst is

\[
\text{R}_1\text{COOH}+\text{CH}_3\text{-OH} \xrightarrow{H_2SO_4} \text{R}_1\text{-COO-CH}_3 + \text{H}_2\text{O}
\]  

(3)

In this work, \(R_1\) was a linear chain of 11–17 carbon atoms containing a variable number of unsaturations depending on the particular origin of the raw material, and \(R_2\) was a methyl radical. A parametric study was carried out to establish the optimum parameters for this reaction. The parameters included catalyst concentration, oil to methanol ratio, reaction temperature and time of reaction. The
parameters and the operating conditions of the experimental runs are summarized in Table 1. The presence or absence of mass transfer effect was established by carrying out experiments at different revolutions per minute (rpm).

**Effect of external mass transfer**

Methanol is meagerly soluble in rice bran oil; thus, it requires agitation in order to avoid mass transfer taking control over the process. Tests were conducted at variable agitation speeds from 200 to 600 rpm (at 0.5 wt% H$_2$SO$_4$, 1:20 oil to methanol ratio and 333 K). As shown in Figure 1, there was an increase in conversion when the stirrer speed was increased from 200 rpm to 500 rpm. However, above 500 rpm, it was observed that there had been no further increase in FFA conversion. This indicates the absence of external mass transfer limitations above 500 rpm. Therefore, a speed of 500 rpm was subsequently used to examine the influence of other parameters.

Figure 2 presents the FFA conversion with time at various molar ratios. There was an increase in conversion as oil to methanol ratio increased from 1:5 to 1:30. This shows that the esterification rate increases with the molar ratio. Similar trends were obtained in other research on esterification of nonanoic acid and lactic acid.$^{21,22}$ There was no significant increase in conversion when the molar ratio increased beyond 1:20. Although using excess methanol speeds up the reaction, it also increases the operating cost and reactor size.$^{23}$ Hence, 1:20 was taken as the optimum molar concentration for further study.

**Effect of catalyst concentration**

The amount of acid catalyst used in the process also affects the FFA conversion. Experiments were carried out by changing the catalyst (H$_2$SO$_4$) amount in the range of 0.15–1.0 (wt%) at a temperature of 333 K, 1:20 oil to methanol molar ratio and at stirrer speed of 500 rpm. The increase in FFA conversion is shown in Figure 3. Conversion increases with increased catalyst quantity up to 0.5 % of the catalyst. Below 0.5 % concentration, the final acid value of oil remains above 4, which is higher and

### Table 1 – Variation of parameters for the esterification of FFA in RBO

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Studied values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Catalyst concentration (wt%)</td>
<td>0.15, 0.25, 0.5, 1.0</td>
</tr>
<tr>
<td>Oil to methanol molar ratio</td>
<td>1:5, 1:10, 1:20, 1:30</td>
</tr>
<tr>
<td>Temperature (K)</td>
<td>318, 323, 328, 333</td>
</tr>
<tr>
<td>Reaction time (min)</td>
<td>15, 30, 50, 70, 90, 120</td>
</tr>
</tbody>
</table>

**Effect of oil to methanol molar ratio**

Oil to methanol molar ratio is an important parameter that affects the yield of the biodiesel. The esterification reaction between the FFA and methanol follows reversible kinetics. To obtain a higher equilibrium conversion, the backward reaction can be minimized with the use of excess methanol.$^{20}$
transesterification cannot be done. From Figure 3, it is evident that the conversion of FFA becomes almost constant as the catalyst concentration is increased beyond 0.5%. The optimum catalyst concentration was taken as 0.5%.

Effect of temperature of reaction

Once the oil to methanol ratio of 1:20 and catalyst concentration of 0.5 wt% were adopted as optimal, the influence of temperature was examined. As shown in Figure 4, reaction temperature evidently influences esterification. The maximum FFA conversion was obtained at 333 K. A higher temperature obviously increased the rate further, but required using a pressure above atmospheric level. The reaction temperature above boiling point of methanol (338 K) cannot be used since at higher temperature, it tends to lose methanol.

Kinetic model

The esterification reaction was a reversible reaction, the rate of which under the operating conditions used was controlled by the chemical reaction, as there is no external mass transfer above 500 rpm. The chemical reaction occurred in the oil phase.

With the above consideration, the rate of reaction for this esterification reaction

\[ \text{RBO(A)} + \text{Methanol(B)} \rightleftharpoons \text{Ester(C)} + \text{Water(D)} \] (4)

is

\[ -\frac{dC_A}{dt} = k_1 C_B C_A - k_2 C_C C_D \] (5)

where \( C_A \) denotes the concentration of FFA in RBO, \( C_B \), \( C_C \) and \( C_D \) are the concentrations of methanol, ester and water respectively; and \( k_1 \) and \( k_2 \) are the kinetic constants for the forward and reverse reaction, respectively.

Since the methanol to oil ratio was very high, it was assumed that \( C_B \) is almost constant. Eq. (5) can be written as:

\[ -\frac{dC_A}{dt} = C_A \frac{dX_A}{dt} = k_1 \left[ C_B (C_A - C_A x_A) - \frac{C_A x_A C_A x_A}{K_e} \right] \] (6)

where equilibrium conversion, \( K_e = k_1 / k_2 \).

This reaction is pseudo-homogeneous, first-order in forward direction and second-order in reverse direction. A general expression for this esterification reaction is

\[ \frac{2 \sqrt{K_e} \tanh^{-1} \left[ \frac{2 C_A x_A + C_B K_e}{\sqrt{C_B (4 C_A + C_B K_e)^2}} \right]}{\sqrt{C_B (4 C_A + C_B K_e)}} = k_1 t \] (7)

This can be simplified to

\[ Y = k_1 t \] (8)

where

\[ Y = \frac{2 \sqrt{K_e} \tanh^{-1} \left[ \frac{2 C_A x_A + C_B K_e}{\sqrt{C_B (4 C_A + C_B K_e)^2}} \right]}{\sqrt{C_B (4 C_A + C_B K_e)}} \]

The rate constant for the forward reaction \( (k_1) \) was obtained by plotting \( Y \) of Eq. (8) vs. time (t). Table 2 contains the calculated rate constants for different reaction temperatures. The value of rate constants obtained are close to the values reported by other researchers.

The influence of temperature on specific reaction rate was determined by fitting \( k_1 \) to the Arrhenius equation,

\[ k = k_0 \cdot e^{\frac{E}{RT}} \] (9)

using plot of –ln \( k_1 \) as a function of reciprocal temperature, \( T \) (Figure 5), \( k_0 \) is pre-exponential factor, \( E \) is activation energy and \( R \) is ideal gas constant [J mol\(^{-1}\) K\(^{-1}\)].
Table 2 – Reaction rate constants at 0.5 wt% catalyst and oil to methanol ratio of 1:20

<table>
<thead>
<tr>
<th>Temperature (K)</th>
<th>$k_1$ (L mol$^{-1}$ min$^{-1}$)</th>
<th>$K_e$</th>
</tr>
</thead>
<tbody>
<tr>
<td>318</td>
<td>0.00510</td>
<td>0.115852</td>
</tr>
<tr>
<td>323</td>
<td>0.00570</td>
<td>0.130634</td>
</tr>
<tr>
<td>328</td>
<td>0.00640</td>
<td>0.168740</td>
</tr>
<tr>
<td>333</td>
<td>0.00762</td>
<td>0.233390</td>
</tr>
</tbody>
</table>

A satisfactory linear coefficient of 0.983 was obtained. The slope of the straight line in Figure 5 can be applied to calculate the activation energy. The activation energy for the forward reaction was 23.21 kJ mol$^{-1}$ and pre-exponential factor 32.65 L mol$^{-1}$ min$^{-1}$. This value is comparable to the activation energy in the range of 20.7 to 45.9 kJ mol$^{-1}$ when calculated by first-order reaction kinetics$^{27-29}$. For heterogeneous catalysts, the activation energy for esterification of different oils is generally higher$^{23,25,26,30}$. By applying the Arrhenius equation to the values of slope and intercept of graphs, the temperature dependency of the constants can be correlated by the following equations:

$$k_1 = \exp \left[ \frac{3.486 - 2792}{T} \right]$$  \hspace{1cm} (10)$$

and

$$K_e = \exp \left[ \frac{13.72 - 5071}{T} \right]$$  \hspace{1cm} (11)$$

**Reaction enthalpy, entropy and free energy**

Assuming constant reaction enthalpy within the operating temperature range, the reaction enthalpy $\Delta H_r$ and entropy $\Delta S_r$ can be estimated by setting the experimental values of eqs. 10 and 11 into the following equation:

$$\ln K_e = \frac{\Delta H_r}{RT} + \frac{\Delta S_r}{R}$$  \hspace{1cm} (12)$$

The reaction enthalpy $\Delta H_r$ and entropy $\Delta S_r$ are found to be 42.16 kJ mol$^{-1}$ and 0.114 kJ mol$^{-1}$ K$^{-1}$. Furthermore, the liquid phase reaction free energy change at 333 K can be calculated to be $\Delta G_r = \Delta H_r - T \Delta S_r = 4.198$ kJ mol$^{-1}$ and the value of $\Delta G_r$ explains the reason for non-spontaneity and it is in good agreement with the reported literature$^{31,32}$.

**Model prediction**

For all calculated values of $k_1$, good linear correlation in the range of 0.97 to 0.999 was obtained. Hence, the proposed kinetic model is appropriate for this reaction. Similar trends were obtained in the esterification of acetic acid also$^{33}$. The goodness-of-fit of the experimental data to this kinetic model was assessed by comparing the experimental FFA conversion with the theoretical prediction of Eq. (8). As can be observed in Figure 6, the errors between the experimental and the predicted data were within ±10 %, which demonstrated the validity of the kinetic model adopted.

**Conclusion**

The effects of catalyst concentration, temperature, agitation and methanol to oil molar ratio on FFA esterification in 12 % FFA rice bran oil with methanol, using sulfuric acid as homogeneous catalyst, were studied. Maximum FFA conversion of 85 % was obtained with the optimum catalyst concentration 0.5 wt%, oil to methanol molar ratio 1:20, agitation speed 500 rpm and at a temperature 333 K in 90 minutes. A pseudo-homogeneous second-order reversible model was demonstrated to justify the experimental data and the activation energy was 23.21 kJ mol$^{-1}$. This model was provided a satisfactory interpretation of the experimental results.
ACKNOWLEDGMENT

We gratefully acknowledge the experimental support from Energy Research Centre, Panjab University, Chandigarh (India).

Notations

A – Rice bran oil
B – Methanol
c – Molar concentration of KOH
C – Ester
C_T – Concentration of RBO, mol L⁻¹
C_F – Concentration of methanol, mol L⁻¹
C_E – Concentration of ester, mol L⁻¹
C_W – Concentration of water, mol L⁻¹
D – Water
E – Activation energy
ΔG_r – Reaction free energy change, kJ mol⁻¹
ΔH_r – Reaction enthalpy, kJ mol⁻¹
k_f – Forward reaction rate constant, kJ mol⁻¹
k_r – Backward reaction rate constant, kJ mol⁻¹
K_c – Equilibrium constant
k_o – Pre-exponential factor, L mol⁻¹ min⁻¹
m – Weight of sample, g
M_w – Molecular weight
R – Ideal gas constant, kJ mol⁻¹ K⁻¹
ΔS_r – Reaction entropy, kJ mol⁻¹ K⁻¹
τ – Time, min
T – Temperature, K
V – Volume, L
X – Conversion

Abbreviations

AV – Acid Value
FAME – Fatty Acid Methyl Ester
FFA – Free Fatty Acid
RBO – Rice Bran Oil
TG – Triacylglycerol

References


