



International Journal of Engineering Business Management Special Issue: Innovations in Pharmaceutical Industry

A Weighing Algorithm for Checking Missing Components in a Pharmaceutical Line

Regular Paper

Alessandro Silvestri^{1.*}, Domenico Falcone¹, Cristina Cerbaso¹, Antonio Forcina¹

1 University of Cassino and Southern Lazio - Department of Civil and Mechanical Engineering * Corresponding author E-mail: silvestr@unicas.it

Received 23 Jun 2014; Accepted 22 Aug 2014

DOI: 10.5772/59022

© 2014 The Author(s). Licensee InTech. This is an open access article distributed under the terms of the Creative Commons Attribution License (http://creativecommons.org/licenses/by/3.0), which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

Abstract To meet the requirements and specifications coming from the surrounding society, the socio-economic progress involves the development of new products, new technologies, new organizational forms etc.

Companies are constantly looking for methods or procedures to improve production and income; but, the enterprise growth is strictly linked to the reliability of its internal processes. Internal failures can often cause loss of image.

The goal of the present work is the development of an algorithm able to optimize the production line of a pharmaceutical firm. In particular, the proposed weighing procedure allows both checking missing components in packaging and minimizing false rejects of packages by dynamic scales.

The main problem is the presence at the same time, in the same package, of different components with different variable weights. The consequence is uncertainty in recognizing the absence of one or more components.

Keywords Scale, Packaging, Reliability, Control, Measurement

1. Introduction

The routine verification of the package content is an important part of any company control activity. It is a consumer right to receive package complete of all expected components [1].

Different control (more or less automatic) systems are adopted by manufacturers to check the right fulfillment of packaged goods, 100% checked or sampled. Those controls permit to reduce the negative implications and potential high costs of customer complaints, claims and product recalls.

Different commercial and automatic tools and equipment are available:

- Vision Systems;
- X-ray Inspection Systems;
- Thermal Inspection Systems;
- Metal Detection Systems;
- Checkweigher Systems.

Vision Systems

A vision system is often adopted for checking damages or wrong pack information. It can also send images and results to be stored for future use, if required.

X-ray Inspection Systems

X-ray inspection system is mainly used for contamination detection, providing reliable information to alert when foreign bodies are contaminating products and packages.

Thermal Inspection Systems

Thermal inspection systems are mainly used in food industry and, in particular, for proper filling of frozen meal packages.

Metal Detection System

A metal detector recognizes the presence of metal bodies, contaminating products and packages.

Checkweigher Systems

Checkweigher systems help to improve the productivity and the efficiency of manufacturing through fast and accurate product inspection by dynamic and conveyor scales. It is generally located at the end of a production process, before of the automatic palletization area.

The above inspection equipment is often integrated in a unique control line (Figure 1).

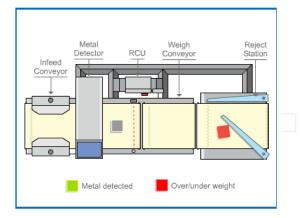


Figure 1. Example of integrated control line (metal detector, checkweigher, reject station)

Two different cases inside the package are possible:

- the same type of components, with the same average weight;
- different components, with different weights.

In the second case, the inspection activity is more complex, as well as the definition of a weighing procedure for checking missing components.

When a weighing procedure is adopted, two kinds of goals have to be achieved:

- on one hand, you have to be sure that all components are present in the package;
- on the other hand, you have to reduce the reject of correct packaged goods.

In the present paper a weighing algorithm to verify the presence of different components in pharmaceutical packages has been developed.

Each component is characterized by a natural weight variability, therefore tolerance limits are required (minimum and maximum accepted weight values for each component in the case).

2. State of the art

Measurement is everywhere, playing a vital role in all work sectors. Incorrect or inaccurate measurements can lead to wrong decisions and have serious consequences both in financial and human health. The weight determination of a product influences a vast range of activities and is the dominant factor in trading. Many chemical reference methods rely on gravimetric determinations. Health and safety and business costs should be vitally dependent on the accurate weight determination, an important source of measurement uncertainty in any analysis. For this purpose different types of scales are used: which are instruments for the weight evaluation of a sample (weighed object). They measure the force exerted by the sample on its support in the Earth gravitational field. Nowadays, mechanical scales are often replaced by electronic ones, which offer a better resolution and faster measurement [2].

The gravimetric test method uses weight measurement to determine the net quantity of contents of packaged goods [3,4], but the scales are also used to check the presence of all the components in a pack [5].

The packaging equipment is a fundamental component of a production line. They are automatic filling systems for any type of product. The whole production line and, in particular, packaging and palletizing systems [6], can be designed and optimized through simulation techniques [7-9]. After packaging and before palletizing, final control activities are generally finalized, to check defects and verify product correspondence to market orders and needs. In particular, the weight control is a traditional inspection activity of many firms, often carried out to assure a customer is paying for exact amount of product. For the above reason, the data collected by checkweighers are archived to be available for future verifications. Therefore, scales modern dynamic are equipped with communications ports to upload data to a host computer. Those data can also be used for monitoring production performances.

Some rules and standards for weight control have been defined ("Packers Rules" proposed by The European Average Weight System), even if, commonly, the "minimum weight" rule is applied (packs characterized by weight under a specified limit are rejected [10,11]).

The identification of missing components in a mixed packaged good is more complex, because of the weight variability of each subcomponent.

Empirical procedures are often adopted to solve this kind of problem.

3. The methodology

The objective of this work is to define an algorithm allowing the improvement of the product quality. In particular, we are interested in avoiding final products (packs containing several parts) with missing components and at the same time in decreasing false rejects. Anyway, the main rule is to prefer false rejects than final products with missing components.

The parameter taken into account for the scope is the product weight and the algorithm aims to provide the right control limits for the scales.

In order to determine the weight limits, the weight tolerances (mimimum and maximum values) of all the parts composing every product (identified with a code, as every part), have to be known.

Therefore, the total minimum and maximum weight of the product has to be calculated as follows :

component2_maximumweight + (2) componentn_maximumweight

The previous values can be chosen as weight limits for the scales, if the value:

lies outside the defined range (product_maximumweight – product_minimumweight). Instead, if the value lies inside the range, it is possible that the scale could consider as good a pack with a missing component.

Therefore, it is necessary to define a new algorithm able to determine more appropriate control limits.

The previous weight control limits definition is based on design tolerances and a subsequent verification of process capability for each component is required. Of course, the components variability is linked to the suppliers reliability and to the process performance.

The main idea of the developed procedure is to link the weight control limits to the variability of the components in each weighed product, instead of fixed design tolerances.

According to probability theory, (the central limit theorem – CLT) [13], given certain conditions, the arithmetic mean of a sufficiently large number of independent random variables, will be approximately normally distributed. The expected value (E.V.) will be the sum of the average values μ_i and its variance (S²) will be the sum of the variances σ^2_i :

$$\boldsymbol{E}.\boldsymbol{V}_{.} = \sum_{i} \boldsymbol{\mu}_{i} \tag{4}$$

$$S^2 = \sum_I \sigma_I^2 \tag{5}$$

Below the weighing procedure is going to be explained (see also flowchart in Annex 1).

In particular three main steps are defined.

Step 1: components variability monitoring

It is possible to cluster components in families with the same characteristics in terms of weight and to collect data in order to evaluate the average and variance values of each family, respecting the statistical significance for the number of samples needed.

After the evaluation of the statistical parameters of each family of components (μ ; σ); it is possible to calculate the expected value of the final product and its standard deviation (square root of the variance), through the equations (4) and (5).

At this point, a first variability range of the final product weight might be defined corresponding to the minimum and maximum weight control limits. In fact, if we consider one standard deviation σ away from the mean, we have about 68% of the values inside the range $\pm \sigma$; whereas if we consider two standard deviations, about 95% of the values lie inside the range $\pm 2\sigma$; and finally about 99.7% are within three standard deviations. This fact is known as the 68-95-99.7 rule, or the 3-sigma rule [14] (Figure 2).

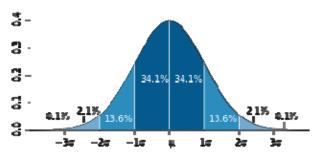


Figure 2. Number of standard deviations and percentages of data

Step 2: control limits definition

Because of the components variability, it can occur that the final product weight lies inside the range previously fixed ($\pm 3\sigma$), even in case of missing components.

In fact, according to the CLT, in the case of missing components, we obtain a reduction of the E.V. and of the standard deviation of the whole package weight (equations (4) and (5)), but if the consequent reduced weight value is still higher than the previous minimum control limit in the case of no missing component (e.g. in Figure 3), we are not sure of the absence of a component because of the weight variability of complete products (we can notice common areas for the curves of missing components and no missing component).



Figure 3. Statistical parameters modification due to missing components (A or B)

It is possible to evaluate the new E.V. and the new standard deviation in the case of the absence of each component. Consequently we obtain modified variability ranges of the final product weight (without each component), corresponding to new minimum and maximum weight control limits (E.V. $\pm 3\sigma$). Among these, it is interesting to consider the major modified maximum control limit (point K in the figure n. 4).

Step 3: control areas definition

Therefore, we can have four possibilities for the total package weight (Figure 4) :

- **Area A**: lower than minimum control limit in the case of no missing component (point J);
- Area B: between minimum control limit in the case of no missing component (point J) and major maximum control limit in the case of a missing component (point K);
- **Area C**: between the major maximum control limit in the case of a missing components (point K) and maximum control limit in the case of no missing component (point L);
- **Area D**: upper than maximum control limit in the case of no missing component (point L).

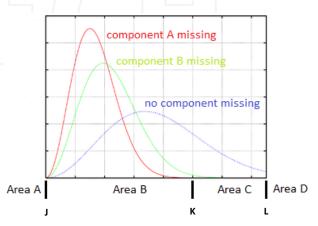


Figure 4. Four possibilities (Areas) for the total package weight

The above Areas correspond to four different events:

- Area A : we are sure that one or more components are missing, so we can reject the packages;
- Area B: we are not sure that the package is complete, so the choice could be a sampling procedure of inspection in order to verify the absence of missing components;
- Area C: we are sure that the package is complete and so the shipment to the costumer is possible;
- Area D: we are sure that double components are present, even if in the history of the production line, no similar case has been recorded, thanks to technical arrangements and because of space constraints inside the package.

4. Case Study

The developed weighing algorithm has been applied in the case of a pharmaceutical production line optimization. In fact, the analysed company wanted to speed and to standardize the procedure of verification of components by checking the final pack weight, primarily reducing false rejects.

4.1 Description and control of the blister packaging line scales

In order to apply the algorithm, first we are going to define the measurement tool and how it works.

The automatic balances control the whole production, rejecting the packs with a weight lower or higher than the imposed tolerance limits; subsequently the rejected packs are stored for the future integration of components (if possible) [12].

All the balances used in the department of solid oral products, are calibrated and periodically inspected according to a specific procedure.

Moreover, a frequent functionality control is carried out with during the use; this operation establishes, under specific conditions, the relationship between the values indicated by a measurement instrument and the corresponding known values of a sample.

In the considered balance (Thermo Fisher Scientific; Figure 5), the packs weight is calculated on the basis of the electrical signal emitted by a load cell located on the conveyor belt of the weighing plate.



Figure 5. Thermo Fisher Scientific balance

The package, sliding along the conveyor belt, reaches the weight reading light barrier placed entering the weighing plate. Through the light barrier signal and the speed measurement, the position of the pack is determined and the weight is calculated on the basis of the signal emitted by the load cell.

The error deviation is compared with the reference and the Versa Controller determines whether to accept or discard the package. The line of blister packaging consists of the following equipment:

Machine	Builder
STEMS OVERTURNING	TAIM
BLISTER MACHINE	Partena M90
VISION SYSTEM	Sea Vision HARLEQUIN
CASES MACHINE	Cmatic BA400 300L
BALANCE	Thermo Fisher
	Scientific
STICKER LABELLING	Bollinatrice IMA
MACHINE	Sensitive AP400 TE 3T
CASE PACKER	CAM
BALANCE	Mettler Toledo
STICKER LABELLING	Etipack Stick 4/8
MACHINE	
ELEVATOR	TCM
LEEVITION	TCIVI

Figure 6. Packaging line description

The balance appreciates the hundredth of a gram.

4.2 Weight limits determination

Hereinafter, we are using specific business terms, listed below with their definition:

- BOM: list and quantities of materials needed for the production process;
- Blister: container for tablets, consisting of a layer of PVC or Foil and a layer of easily pierceable aluminium;
- Insert: package leaflet for the patient;
- Case: box containing blister and insert;
- Primary packaging: blister filled with tablets;
- Secondary packaging: case filled with blisters and insert;
- False reject: a product that the automatic balance discards due to a breakdown or a mistake, but that is actually good to be inserted in the packaging boxes;
- Packaging Box: box containing individual packages of product.

The study to determine the balance weight limits has been conducted in the blister packaging line, that manages 187 different products.

In order to determine the weight limits, all the materials composing every component (identified with a code, as all material), with their weights and relative tolerances should be known.

The requested information of every component are:

- Tablet type, number of tablets in each case and weight tolerances;

- Aluminium, weight in g/m² (grams per square meter) with tolerances, sizes in mm² (square millimetres);
- PVC, weight in g/m², sizes in mm²;
- Foil, weight in g/m², sizes in mm²;
- Case, weight in g/m², sizes in mm²;
- Insert, weight in g/m², sizes in mm².

For tablets:

Hereinafter, we are only considering one kind of product (Product n. 1) and assuming three hypotheses:

- Absence of measurement errors;
- Supplier Qualification, characterized by capability indices cp and cpk >>1;
- Priority interest in avoiding missing components rather than false rejects.

BLP	TAB	tot	Active ingredient	Semifinished code	1 tablet minimum weight g	1 tablet maximum weight g	1 tablet minimum total weight in 1 blister g	1 tablet maximum total weight in 1 blister g
3	10	30	Product B	XXXXXX	0.2910	0.3090	2.9100	3.0900

Table 1. Product 1 - tablets weight

where:

BLP: number of blisters TAB: number of tablets per blister tot: total number of tablets in each case

The tablet minimum and maximum weights (tolerance range) are defined in the design phase.

The minimum and maximum total weight of one blister are obtained by multiplying the minimum and maximum weight of the tablet to the total number of tablets in each blister, adding the aluminium weight (used to coat the tablets), as follows:



Table 2. Product n. 1 - filled blister weight

Starting from the area of 1 blister (m^2) , the aluminium weight is given by:

 $\begin{array}{l} minimum(maximum) a luminium weight for 1 b lister = \\ minimum(maximum) a luminium weight (g/m²) \times \\ area of 1 b lister \end{array} (7) \\ \end{array}$

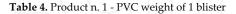
Consequently, it is possible to evaluate the aluminium tolerances (Table 3).

Minimu m weight g/m ²	Maxim um weight g/m ²	r	1 blister area m²		Min. aluminiu m weight 1blister g	m weight
56.7000	68.3000	61x70	0.0043	20µ	0.2421	0.2916

Table 3. Product n. 1 - aluminium weight of 1 blister

The same operations have been made to calculate PVC (or Foil) and insert weights (Tables 4 and 5).

Minimum weight PVC g/m ²	Maximum weight PVC g/m ²	sizes mm	1 blister area m ²	Minimum PVC weight 1blister g	Maximum PVC weight 1blister g
380.9500	421.0500	61x70	0.0043	1.6267	1.7979



Insert minimum weight g/m ²	Insert maximum weight insert g/m ²	sizes mm	area m²	Insert minimum total weight g	Insert maximum total weight insert g
38.0000	42.0000	130X810	0.1053	4.0014	4.4226

Table 5. Product n. 1 - insert weight

Regarding the case, its weight, not considering the closing flaps, is given by the product of its area and its specific weight (in g/m²):

```
minimum(maximum)Casetotalweight =
(casearea(withoutclosingflaps) × (8)
minimum(maximum)Caseweight)
```

Sizes mm	Case minimum weight g/m ²	Case maximum weight g/m ²	Case area m²		Maximum weight of 1 empty Case without flaps g
65X35X75	332.5000	367.5000	0.0218	7.2452	8.0078

 Table 6. Product n. 1 – empty case weight not considering closing flaps

Finally, we have also to consider the weight of the closing flaps, calculated as described below:

- from a case the flaps have been cut and weighed using a balance with a sensitivity up to one thousandth of a gram;
- subsequently, the percentage of the flaps weight has been calculated (15% of the whole case weight);
- this percentage has been used for all the products, being only slightly variable among the products, in order to evaluate the case total weight (Table 7).

Flaps	Flaps	Case	Case
minimum	maximum	minimum	maximum
weight g	weight g	weight g	weight g
0.9223	1.0194	8.1675	

Table 7. Product n. 1 - closing flaps weight and case total weight

The weight of the labels is overlooked because it is not appreciable by the balance.

Then:

Totalf'inalweight = filledblisterweight + insertweight + caseweight (9)

Where the final weight represents the total weight of the pack; the weight of the filled blisters is given by the weight of the aluminium added to the weight of the PVC or Foil and to the weight of the tablets in the blister, multiplied by the number of blisters in the case; the weights of insert and case have been previously calculated.

Ultimately, considering tolerances, the final minimum and maximum weights of the packaging will be as follows:



 Table 8. Product n. 1 – pack final weight considering weight tolerances

Different products can have same weight of materials, therefore they will have the same final pack weight. For that reason, a subdivision of products in families has been set according to the final weight. For each family, the determination of the weight limits for the dynamic balance is the same (total number of families obtained: 67).

Initially, it is possible to keep as weight limits for the balance the final minimum and maximum weight of the completely filled case, which is the weight obtained by adding the weight tolerances of each material composing the case. According to the weighing procedure, if:

is a value out of the range defined by the weight tolerances, the values in Table 8 could be set as weight limits for the dynamic balance.

The components considered to establish the lighter one are only the filled blisters and the insert; whereas the case is not considered, because it is impossible that a product reaches the balance without its case.

By comparing the weight of the insert and the filled blister, is possible to highlight the lighter component, to verify weight limits and evaluate the final maximum weight, through the equation (5) (Table 9).

Insert minimum weight g	Insert maximum weight g	1 filled blister minimum total weight g	1 filled blister maximum total weight g	Lighter component
4.0014	4.4226	4.7788	5.1795	Insert
4.0014	4.4226	3.8288	4.1295	Blister
4.8412	5.3508	4.6128	4.9455	Blister
4.0014	4.4226	3.8288	4.1295	Blister
1.7290	1.9110	4.6358	4.9652	Insert
3.4580	3.8220	6.0414	6.5389	Insert
3.4580	3.8220	4.7114	5.0689	Insert
3.4580	3.8220	4.7114	5.0689	Insert
3.4580	3.8220	4.6585	5.0066	Insert
3.4580	3.8220	4.7114	5.0689	Insert
3.4580	3.8220	4.7114	5.0689	Insert
3.4580	3.8220	4.7114	5.0689	Insert
3.4580	3.8220	4.7114	5.0689	Insert
5.5176	6.0984	4.3798	4.9957	Blister

Table 9. Comparison between the insert and the filled blister to identify the lighter component

For the first product, the lighter component is the insert and its minimum weight is 4.00 g. The maximum final weight, shown in Table 8, is 28,99 g.

$$28,99 - 4,00 = 24,99g \tag{11}$$

without missing components 169 50.44 1 26.51 57 18.35 11.4 39.16 170 47.43 3 15.18 59 15.45 111.4 39.16 177 50.44 4 19.39 60 23.54 116 40.48 172 50.44 5 9.70 61 15.45 117 40.48 172 50.44 6 11.45 62 18.97 118 40.48 177 50.44 7 8.73 63 15.95 119 41.81 176 38.79 9 14.93 65 23.96 121 41.70 177 41.81 10 9.98 66 17.14 122 41.81 178 50.44 12 15.05 60 17.14 125 39.16 187 44.81 14 15.05 77 40.28 130 41.70 185 50.44		Absolute	security	minimun	n weight	t va <mark>lue of</mark>	a good p	ack
2 19.39 58 1967 114 39.16 170 47.43 3 15.18 59 15.45 115 40.48 171 50.44 4 19.39 60 23.54 116 40.48 172 50.44 5 9.70 61 15.45 118 40.48 174 50.44 7 8.73 63 15.95 119 41.81 175 39.16 8 9.98 66 20.95 122 41.70 177 41.81 10 9.98 66 21.01 123 41.81 170 50.44 12 15.05 66 17.14 125 39.16 181 50.44 14 150.5 70 18.86 122 41.81 184 50.44 14 150.5 77 40.28 133 57.54 122 17.44 188 50.44 19 8.98 74 40.28 </th <th></th> <th></th> <th>with</th> <th>out missi</th> <th>ng com</th> <th>ponents</th> <th></th> <th></th>			with	out missi	ng com	ponents		
3 15.18 59 1545 115 40.48 171 50.44 4 19.39 60 23.54 116 40.48 172 50.44 5 9.70 61 15.45 117 40.48 173 50.44 6 11.45 62 18.97 119 41.81 175 39.16 8 9.98 64 20.95 122 60.18 176 38.79 9 14.93 65 23.96 122 41.70 177 41.81 10 9.98 66 21.01 122 41.70 178 73.73 11 15.05 77 40.28 120 41.70 182 41.81 15 15.05 77 40.28 133 57.54 122 41.70 185 50.44 19 8.98 75 18.99 133 57.54 122 41.70 185 41.70 165 50.44	1	26.51	57	18.35	113	38.79	169	50.44
4 19.39 60 23.54 116 40.48 172 50.44 5 9.70 61 15.45 117 40.48 173 50.44 7 8.73 63 15.95 119 41.81 175 39.16 8 9.98 66 20.95 122 41.70 177 41.81 10 9.98 66 21.01 122 41.70 177 41.81 12 15.05 67 18.97 123 41.81 179 50.44 13 15.05 69 17.14 122 41.70 178 73.73 14 15.05 71 40.28 127 43.70 183 50.44 15 15.05 76 23.85 130 41.70 186 60.44 19 8.98 75 130 130 41.70 186 60.44 19 8.98 75 130 130 41.70 126 60.44 20 15.05 76 23.85 133<	2	19.39	58	19.67	114	39.16	170	47.43
5 9.70 61 15.45 117 40.48 173 50.44 6 11.45 62 18.97 118 40.48 174 50.44 7 8.73 63 15.95 120 60.18 176 38.79 9 14.93 65 23.96 121 41.70 178 73.73 11 15.05 66 21.01 122 41.70 178 73.73 12 15.05 66 17.14 122 41.81 179 50.44 13 15.05 71 40.28 122 41.70 183 50.44 14 15.05 76 23.85 130 41.70 183 50.44 19 8.98 75 18.99 131 30.16 186 50.44 19 8.98 76 23.85 132 60.07 186 50.44 19 8.98 76 13.9 135 41.70 186 50.44 19 8.98 76 13.83 132 60.07 136 137 140.48 20 15.05 76 23.85 133 57.54 146 141 <t< th=""><th>3</th><th>15.18</th><th>59</th><th>15.45</th><th>115</th><th>40.48</th><th>171</th><th>50.44</th></t<>	3	15.18	59	15.45	115	40.48	171	50.44
5 9.70 61 15.45 117 40.48 173 50.44 6 11.45 62 18.97 118 40.48 174 50.44 7 8.73 63 15.95 120 60.18 176 38.79 9 14.93 65 23.96 121 41.70 178 73.73 11 15.05 66 21.01 122 41.70 178 73.73 12 15.05 66 17.14 122 41.81 179 50.44 13 15.05 71 40.28 122 41.70 183 50.44 14 15.05 76 23.85 130 41.70 183 50.44 19 8.98 75 18.99 131 30.16 186 50.44 19 8.98 76 23.85 132 60.07 186 50.44 19 8.98 76 13.9 135 41.70 186 50.44 19 8.98 76 13.83 132 60.07 136 137 140.48 20 15.05 76 23.85 133 57.54 146 141 <t< th=""><th>4</th><th>19.39</th><th>60</th><th>23.54</th><th>116</th><th>40.48</th><th>172</th><th>50.44</th></t<>	4	19.39	60	23.54	116	40.48	172	50.44
6 11.45 62 18.97 118 40.48 174 50.44 7 8.73 63 15.95 119 41.81 175 39.16 9 14.93 65 23.96 120 60.18 177 41.81 10 9.98 66 21.01 122 41.70 178 73.73 11 15.05 68 17.14 125 39.16 180 46.40 13 15.05 70 18.86 122 41.70 178 50.44 14 15.05 71 40.28 122 41.70 183 50.44 15 15.05 77 40.28 130 41.70 183 50.44 19 8.98 75 18.99 129 41.70 185 50.44 19 8.98 75 133 57.54 133 57.54 134 41.70 22 17.48 78 36.77 138 41.70 135 41.70 24 15.05 77 40.28 136 38.79 145 44.84 24 15.05 77 40.28 138 41.70 125 44.14	5	9.70	61	15.45	117	40.48	· · · · · · · · · · · · · · · · · · ·	50.44
7 8.73 63 15.95 119 41.81 175 39.16 8 9.98 64 20.95 120 60.18 176 38.79 9 14.93 65 23.96 121 41.70 177 41.81 10 9.98 66 21.01 122 41.70 178 39.16 11 15.05 68 17.14 122 41.81 180 46.40 13 15.05 70 18.86 126 41.70 182 50.44 16 14.54 72 23.85 128 41.81 182 50.44 16 14.54 72 23.85 129 41.70 185 50.44 17 17.60 73 18.99 131 39.16 187 47.43 20 15.05 76 23.85 133 57.54 133 57.54 21 15.05 77 40.28 133 57.54 141 186 140 21 15.05 77 40.28 135 41.70 125 141 161 22 17.78 83 20.04 139 51.81 142 <t< th=""><th></th><th>11.45</th><th></th><th>18.97</th><th></th><th>40.48</th><th></th><th>50.44</th></t<>		11.45		18.97		40.48		50.44
8 9.98 64 20.95 120 60.18 176 38.79 9 14.93 65 23.96 121 41.70 177 41.81 10 9.98 66 21.01 122 41.81 178 73.73 11 15.05 68 17.14 122 41.81 180 464.40 13 15.05 70 18.86 126 41.70 132 41.81 15 15.05 71 40.28 127 43.70 183 50.44 16 14.54 72 23.85 132 60.07 186 50.44 17 17.60 73 18.99 131 39.16 187 41.80 18 14.93 74 40.28 133 57.54 187 41.70 186 50.44 19 8.98 75 13.99 135 41.70 187 41.81 147 187 41.81 187 <th></th> <th></th> <th></th> <th></th> <th></th> <th></th> <th></th> <th></th>								
9 14.93 65 23.96 121 41.70 177 41.81 10 9.98 66 21.01 122 41.70 178 73.73 11 15.05 67 18.97 123 41.81 179 50.44 12 15.05 68 17.14 122 39.16 181 50.44 13 15.05 70 18.86 125 39.16 182 41.81 15 15.05 71 40.28 122 43.70 183 50.44 16 14.54 72 23.85 128 41.81 184 41.81 17 17.60 73 18.99 129 41.70 186 50.44 19 8.98 75 18.99 133 57.54 120 160.57 60.42 133 57.54 24 150.5 77 40.28 133 57.54 24 160.14 24 25 17.78 81 40.28 137 40.88 24 26 17.99 82 40.28								
10 9.98 66 21.01 122 41.70 178 73.73 11 15.05 67 18.97 123 41.81 179 50.44 12 15.05 69 17.14 125 39.16 181 50.44 14 15.05 70 18.86 125 41.70 183 50.44 15 15.05 70 18.86 126 41.70 183 50.44 16 14.54 72 23.85 128 41.81 184 41.81 17 17.60 73 18.99 129 41.70 185 50.44 18 14.93 74 40.28 130 41.70 186 50.44 19 8.98 75 18.99 133 57.54 122 17.48 78 36.77 133 41.70 126 127 17.87 81 40.28 135 38.79 126 147 41.81 126 147 141 38.79 126 147 141.81 126					-			
11 15.05 67 18.97 123 41.81 179 50.44 12 15.05 68 17.14 124 41.81 180 46.40 13 15.05 69 17.14 125 39.16 181 50.44 14 15.05 70 18.86 127 43.70 183 50.44 16 14.54 72 23.85 128 41.81 184 41.81 17 17.60 73 18.99 131 39.16 187 47.43 20 15.05 76 23.85 132 60.07 2 2 17.40 186 50.44 19 8.98 75 18.99 131 39.16 187 47.43 20 15.05 76 23.85 132 60.07 2 2 17.43 83 17.0 186 50.44 17.0 185 141.70 2 2 17.9 82 40.28 135 38.79 2 2 17.78 81 40.28 137 <th></th> <th></th> <th></th> <th></th> <th></th> <th></th> <th></th> <th></th>								
12 15.05 68 17.14 124 41.81 180 46.40 13 15.05 70 18.86 125 39.16 181 50.44 14 15.05 71 40.28 125 41.81 182 41.81 16 14.54 72 23.85 128 41.81 184 41.81 17 17.60 73 18.99 131 39.16 187 47.43 20 15.05 76 23.85 132 60.07 2 2 7.44.33 2 2 17.87 8.99 131 39.16 187 47.43 20 15.05 76 23.85 132 60.07 2 2 17.43 78 36.75 133 35.754 2 2 17.8 81 40.28 135 38.79 2 2 2 17.8 32.0.04 135 38.79 2 2 2 141 38.79 34 141 33.79 34 34.14 2 34.141 34.14 34.14						-	179	
13 15.05 69 17.14 125 39.16 181 50.44 14 15.05 70 18.86 126 41.70 183 50.44 15 15.05 71 40.28 127 43.70 183 50.44 16 14.54 72 23.85 128 41.81 184 41.81 17 17.60 73 18.99 129 41.70 186 50.44 19 8.98 75 18.99 131 39.16 187 47.43 20 15.05 77 40.28 133 57.54 2 2 21 15.05 77 40.28 133 57.54 2 2 2 17.87 83 20.04 136 38.79 2 2 2 17.87 83 20.04 138 41.70 2 2 2 17.87 83 20.04 138 41.70 2 2 2 18.35 39.99 142 60.18 2 2 2 2 2	·····†				1			
14 15.05 70 18.86 126 41.70 182 41.81 15 15.05 71 40.28 127 43.70 183 50.44 16 14.54 72 23.85 126 41.81 184 41.81 17 17.60 73 18.99 130 41.70 185 50.44 18 14.93 74 40.28 130 41.70 186 50.44 19 8.98 75 18.99 131 39.16 187 47.43 20 15.05 76 23.85 132 60.75 18.9 133 57.54 21 15.05 80 40.28 136 38.79 142 1.01 187 22 17.78 81 40.28 136 38.79 1.02 1.02 1.02 22 17.78 81 40.28 136 41.70 1.02 1.02 1.02 23 9.70 79 40.28 136 41.70 1.02 1.02 1.02 24 15.05 80 40.28 137 40.48 1.02 1.02 24 17.87 84 16.16 <th>·····è·</th> <th></th> <th></th> <th></th> <th>\$</th> <th>-</th> <th>{ }·····</th> <th></th>	·····è·				\$	-	{ }·····	
15 15.05 71 40.28 127 43.70 183 50.44 16 14.54 72 23.85 128 41.81 184 41.81 17 17.60 73 18.99 130 41.70 185 50.44 18 14.93 74 40.28 130 41.70 186 50.44 19 8.98 75 18.99 131 39.16 187 47.43 20 15.05 76 23.85 132 60.07 20.16 <td< th=""><th></th><th></th><th></th><th></th><th></th><th></th><th>1</th><th></th></td<>							1	
16 14.54 72 23.85 128 41.81 184 41.81 17 17.60 73 18.99 129 41.70 185 50.44 18 14.93 74 40.28 130 41.70 186 50.44 19 8.98 75 18.99 131 39.16 187 47.43 20 15.05 76 23.85 132 60.07 24 78 36.77 134 41.70 23 9.70 79 40.39 135 41.70 2 2 2 17.87 80 40.28 136 38.79 24 15.05 80 40.28 136 41.70 2 2 2 27 17.87 83 20.04 139 41.81 2 2 26 17.99 82 40.28 138 41.70 2 2 28 17.87 84 16.16 140 41.81 2 2 30 19.69 86 15.82 143 34.14 34.14 32 22.23 88 16.08 144 34.14 33 18.35 91 19.69 <th></th> <th></th> <th></th> <th></th> <th>-</th> <th></th> <th></th> <th>-</th>					-			-
17 17.60 73 18.99 129 41.70 185 50.44 18 14.93 74 40.28 130 41.70 186 50.44 19 8.98 75 18.99 131 39.16 187 47.43 20 15.05 76 23.85 132 60.07 187 47.43 22 17.48 78 36.77 134 41.70 2 2 7.7 40.28 133 57.54 2 2 17.87 80 40.28 136 38.79 2								
18 14.93 74 40.28 130 41.70 186 50.44 19 8.98 75 18.99 131 39.16 187 47.43 20 15.05 77 40.28 133 57.54 132 60.07 21 15.05 77 40.28 133 57.54 132 60.07 23 9.70 79 40.39 135 41.70 24 15.05 80 40.28 136 38.79 25 17.78 81 40.28 137 40.48 26 27 77 83 20.04 139 41.81 26 22.34 141 38.79 26 22.34 141 38.79 26 22.23 84 16.16 140 41.81 26 22.34 141 38.79 26 22.23 88 16.08 144 34.14 34.14 32 22.23 88 16.08 144 34.14<								-
19 8.98 75 18.99 131 39.16 187 47.43 20 15.05 76 23.85 132 60.07 2 21 15.05 77 40.28 133 57.54 2 1 23 9.70 79 40.39 135 41.70 2 1 1.00 1.0							********	
20 15.05 76 23.85 132 60.07 21 15.05 77 40.28 133 57.54 22 17.48 78 36.77 134 41.70 23 9.70 79 40.39 135 41.70 24 15.05 80 40.28 136 38.79 25 17.78 81 40.28 137 40.48 26 17.99 82 40.28 138 41.70 27 17.87 83 20.04 139 41.81 28 17.87 84 16.16 140 41.81 29 9.90 85 22.34 141 38.79 30 19.69 86 15.82 142 60.18 31 15.82 87 15.82 143 34.14 32 22.23 88 16.08 144 34.14 33 18.35 90 19.67 146 50.44 34 18.35 90 19.67 146 50								
21 15.05 77 40.28 133 57.54 22 17.48 78 36.77 134 41.70 23 9.70 79 40.39 135 41.70 24 15.05 80 40.28 136 38.79 25 17.78 81 40.28 137 40.48 26 17.99 82 40.28 138 41.70 27 17.87 83 20.04 139 41.81 28 17.87 84 16.16 140 41.81 29 9.90 85 22.34 141 38.79 30 19.69 86 15.82 142 60.18 31 15.82 87 15.82 143 34.14 32 22.23 88 16.08 144 34.14 33 18.35 90 19.67 146 50.44 34 18.35 90 19.67 146 50.44 35 18.35 91 19.69 147 41							187	47.43
22 17.48 78 36.77 134 41.70 23 9.70 79 40.39 135 41.70 24 15.05 80 40.28 136 38.79 25 17.78 81 40.28 137 40.48 26 17.99 82 40.28 138 41.70 27 17.87 83 20.04 139 41.81 28 17.87 84 16.16 140 41.81 29 9.90 85 22.34 141 38.79 30 19.69 86 15.82 142 60.18 31 15.82 87 15.82 143 34.14 32 22.23 88 16.08 144 34.14 33 18.35 90 19.67 146 50.44 34 18.35 90 19.67 148 50.44 35 18.35 91 19.69 147 41.81 36 22.23 92 19.32 148 50					2			
23 9.70 79 40.39 135 41.70 24 15.05 80 40.28 136 38.79 25 17.78 81 40.28 137 40.48 26 17.99 82 40.28 138 41.70 27 17.87 83 20.04 139 41.81 28 17.87 84 16.16 140 41.81 29 9.90 85 22.34 141 38.79 30 19.69 86 15.82 142 60.18 31 15.82 87 15.82 143 34.14 32 22.23 88 16.08 144 34.14 33 18.35 90 19.67 146 50.44 35 18.35 91 19.69 147 41.81 36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50				{				
24 15.05 80 40.28 136 38.79 25 17.78 81 40.28 137 40.48 26 17.99 82 40.28 138 41.70 27 17.87 83 20.04 139 41.81 28 17.87 84 16.16 140 41.81 29 9.90 85 22.34 141 38.79 30 19.69 86 15.82 142 60.18 31 15.82 87 15.82 143 34.14 32 22.23 88 16.08 144 34.14 33 18.35 90 19.67 146 50.44 34 18.35 91 19.69 147 41.81 36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50.44 41 19.32 97 22.68 151 4								
25 17.78 81 40.28 137 40.48 26 17.99 82 40.28 138 41.70 27 17.87 83 20.04 139 41.81 28 17.87 84 16.16 140 41.81 29 9.90 85 22.34 141 38.79 30 19.69 86 15.82 142 60.18 31 15.82 87 15.82 143 34.14 32 22.23 88 16.08 144 34.14 33 18.35 90 19.67 146 50.44 34 18.35 91 19.69 147 41.81 36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50.44 39 21.01 96 18.81 152 50.44 41 19.32 97 22.68 154 7	23	9.70	79	40.39		41.70		
26 17.99 82 40.28 138 41.70 27 17.87 83 20.04 139 41.81 28 17.87 84 16.16 140 41.81 29 9.90 85 22.34 141 38.79 30 19.69 86 15.82 142 60.18 31 15.82 87 15.82 143 34.14 32 22.23 88 16.08 144 34.14 33 18.35 89 15.79 145 47.43 34 18.35 90 19.67 146 50.44 35 18.35 91 19.69 147 41.81 36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50.44 41 19.32 97 22.68 151 40.48 42 21.01 98 22.68 155 7	24	15.05	80	40.28	136	38.79		
27 17.87 83 20.04 139 41.81 28 17.87 84 16.16 140 41.81 29 9.90 85 22.34 141 38.79 30 19.69 86 15.82 142 60.18 31 15.82 87 15.82 143 34.14 32 22.23 88 16.08 144 34.14 33 18.35 90 19.67 145 47.43 34 18.35 90 19.67 146 50.44 35 18.35 91 19.69 147 41.81 36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50.44 39 21.01 96 18.81 152 50.44 41 19.32 97 22.68 153 50.33 42 21.01 98 22.68 154 7	25	17.78	81	40.28	137	40.48		
28 17.87 84 16.16 140 41.81 29 9.90 85 22.34 141 38.79 30 19.69 86 15.82 142 60.18 31 15.82 88 16.08 144 34.14 32 22.23 88 16.08 144 34.14 33 18.35 89 15.79 145 47.43 34 18.35 90 19.67 146 50.44 35 18.35 91 19.69 147 41.81 36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50.44 40 21.01 96 18.81 152 50.44 41 19.32 97 22.68 154 73.73 42 21.01 98 22.68 154 73.73 44 22.68 100 20.95 156	26	17.99	82	40.28	138	41.70		
29 9.90 85 22.34 141 38.79 30 19.69 86 15.82 142 60.18 31 15.82 87 15.82 143 34.14 32 22.23 88 16.08 144 34.14 33 18.35 89 15.79 145 47.43 34 18.35 90 19.67 146 50.44 35 18.35 91 19.69 147 41.81 36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50.44 39 21.01 95 22.68 151 40.48 40 21.01 96 18.81 152 50.44 41 19.32 97 22.68 154 73.73 42 21.01 98 22.68 154 73.73 44 22.68 100 20.95 156	27	17.87	83	20.04	139	41.81		
30 19.69 86 15.82 142 60.18 31 15.82 143 34.14 32 22.23 88 16.08 144 34.14 33 18.35 89 15.79 145 47.43 34 18.35 90 19.67 146 50.44 35 18.35 91 19.69 147 41.81 36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50.44 39 21.01 95 22.68 151 40.48 40 21.01 96 18.81 152 50.44 41 19.32 97 22.68 154 73.73 42 21.01 98 22.68 154 73.73 44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 50.33 <	28	17.87	84	16.16	140	41.81		
31 15.82 87 15.82 143 34.14 32 22.23 88 16.08 144 34.14 33 18.35 89 15.79 145 47.43 34 18.35 90 19.67 146 50.44 35 18.35 91 19.69 147 41.81 36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50.44 39 21.01 95 22.68 151 40.48 40 21.01 96 18.81 152 50.44 41 19.32 97 22.68 154 73.73 42 21.01 98 22.68 154 73.73 43 22.23 99 19.10 155 73.73 44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 <t< th=""><th>29</th><th>9.90</th><th>85</th><th>22.34</th><th>141</th><th>38.79</th><th></th><th></th></t<>	29	9.90	85	22.34	141	38.79		
32 22.23 88 16.08 144 34.14 33 18.35 89 15.79 145 47.43 34 18.35 90 19.67 146 50.44 35 18.35 91 19.69 147 41.81 36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50.44 39 21.01 95 22.68 151 40.48 40 21.01 96 18.81 152 50.44 41 19.32 97 22.68 154 73.73 42 21.01 98 22.68 154 73.73 43 22.23 99 19.10 155 73.73 44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 50.33 46 22.23 102 55.98 158 <	30	19.69	86	15.82	142	60.18		
32 22.23 88 16.08 144 34.14 33 18.35 89 15.79 145 47.43 34 18.35 90 19.67 146 50.44 35 18.35 91 19.69 147 41.81 36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50.44 39 21.01 95 22.68 151 40.48 40 21.01 96 18.81 152 50.44 41 19.32 97 22.68 154 73.73 42 21.01 98 22.68 154 73.73 44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 50.33 46 22.23 102 55.98 158 73.73 47 22.68 104 51.73 160	31	15.82	87	15.82	143	34.14		
33 18.35 89 15.79 145 47.43 34 18.35 90 19.67 146 50.44 35 18.35 91 19.69 147 41.81 36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50.44 39 21.01 95 22.68 151 40.48 40 21.01 96 18.81 152 50.44 41 19.32 97 22.68 153 50.33 42 21.01 98 22.68 154 73.73 43 22.23 99 19.10 155 73.73 44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 50.33 46 22.23 102 55.98 158 73.73 47 22.68 103 51.73 160	32	22.23	88	16.08		34.14		
34 18.35 90 19.67 146 50.44 35 18.35 91 19.69 147 41.81 36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50.44 39 21.01 95 22.68 151 40.48 40 21.01 96 18.81 152 50.44 41 19.32 97 22.68 153 50.33 42 21.01 98 22.68 154 73.73 43 22.23 99 19.10 155 73.73 44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 50.33 46 22.23 102 55.98 158 73.73 47 22.68 103 51.73 160 50.33 49 18.81 105 40.46 161	33	18.35	89	15.79		47.43		
36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50.44 39 21.01 95 22.68 151 40.48 40 21.01 96 18.81 152 50.44 41 19.32 97 22.68 153 50.33 42 21.01 98 22.68 154 73.73 43 22.23 99 19.10 155 73.73 44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 50.33 46 22.23 102 55.98 158 73.73 47 22.68 103 51.73 160 50.33 49 18.81 105 40.46 161 63.82 50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163	34	18.35	90	19.67		50.44		
36 22.23 92 19.32 148 50.44 37 22.23 93 18.99 149 73.84 38 22.23 94 15.86 150 50.44 39 21.01 95 22.68 151 40.48 40 21.01 96 18.81 152 50.44 41 19.32 97 22.68 153 50.33 42 21.01 98 22.68 154 73.73 43 22.23 99 19.10 155 73.73 44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 50.33 46 22.23 102 55.98 158 73.73 47 22.68 103 51.73 160 50.33 49 18.81 105 40.46 161 63.82 50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163	35	18.35	91	19.69	147	41.81		
38 22.23 94 15.86 150 50.44 39 21.01 95 22.68 151 40.48 40 21.01 96 18.81 152 50.44 41 19.32 97 22.68 153 50.33 42 21.01 98 22.68 154 73.73 43 22.23 99 19.10 155 73.73 44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 50.33 46 22.23 102 55.98 158 73.73 47 22.68 103 51.73 160 50.33 49 18.81 105 40.46 161 63.82 50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163 39.16 52 19.69 108 41.70 164 57.54 53 19.69 109 41.70 165	36	22.23	92	19.32		50.44		
38 22.23 94 15.86 150 50.44 39 21.01 95 22.68 151 40.48 40 21.01 96 18.81 152 50.44 41 19.32 97 22.68 153 50.33 42 21.01 98 22.68 154 73.73 43 22.23 99 19.10 155 73.73 44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 50.33 46 22.23 102 55.98 158 73.73 47 22.68 103 51.73 160 50.33 49 18.81 105 40.46 161 63.82 50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163 39.16 52 19.69 108 41.70 164 57.54 53 19.67 110 60.07 166	37	22.23	93	18.99	149	73.84		
39 21.01 95 22.68 151 40.48 40 21.01 96 18.81 152 50.44 41 19.32 97 22.68 153 50.33 42 21.01 98 22.68 154 73.73 43 22.23 99 19.10 155 73.73 44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 50.33 46 22.23 102 55.98 158 73.73 47 22.68 103 51.73 160 50.33 49 18.81 105 40.46 161 63.82 50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163 39.16 52 19.69 108 41.70 164 57.54 53 19.67 100 60.07 166 50.44 55 21.01 111 41.70 167	·····	22.23	94	15.86		50.44		
40 21.01 96 18.81 152 50.44 41 19.32 97 22.68 153 50.33 42 21.01 98 22.68 154 73.73 43 22.23 99 19.10 155 73.73 44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 50.33 46 22.23 102 55.98 158 73.73 47 22.68 103 51.73 160 50.33 49 18.81 105 40.46 161 63.82 50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163 39.16 52 19.69 108 41.70 164 57.54 53 19.69 109 41.70 165 47.43 54 19.67 110 60.07 166 50.44 55 21.01 111 41.70 167								
41 19.32 97 22.68 153 50.33 42 21.01 98 22.68 154 73.73 43 22.23 99 19.10 155 73.73 44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 50.33 46 22.23 102 55.98 158 73.73 47 22.68 103 51.73 159 94.21 48 22.23 104 51.73 160 50.33 49 18.81 105 40.46 161 63.82 50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163 39.16 52 19.69 108 41.70 165 47.43 53 19.67 110 60.07 166 50.44 55 21.01 111 41.70 167 73.84	1				1			
42 21.01 98 22.68 154 73.73 43 22.23 99 19.10 155 73.73 44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 50.33 46 22.23 102 55.98 158 73.73 47 22.68 103 51.73 159 94.21 48 22.23 104 51.73 160 50.33 49 18.81 105 40.46 161 63.82 50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163 39.16 52 19.69 108 41.70 164 57.54 53 19.69 109 41.70 165 47.43 54 19.67 110 60.07 166 50.44 55 21.01 111 41.70 167 73.84								
43 22.23 99 19.10 155 73.73								
44 22.68 100 20.95 156 50.33 45 22.68 101 15.05 157 50.33 46 22.23 102 55.98 158 73.73 47 22.68 103 51.73 159 94.21 48 22.23 104 51.73 160 50.33 49 18.81 105 40.46 161 63.82 50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163 39.16 52 19.69 108 41.70 164 57.54 53 19.67 110 60.07 166 50.44 55 21.01 111 41.70 167 73.84								
45 22.68 101 15.05 157 50.33 46 22.23 102 55.98 158 73.73 47 22.68 103 51.73 159 94.21 48 22.23 104 51.73 160 50.33 49 18.81 105 40.46 161 63.82 50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163 39.16 52 19.69 108 41.70 164 57.54 53 19.67 110 60.07 166 50.44 55 21.01 111 41.70 167 73.84								
46 22.23 102 55.98 158 73.73 47 22.68 103 51.73 159 94.21 48 22.23 104 51.73 160 50.33 49 18.81 105 40.46 161 63.82 50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163 39.16 52 19.69 108 41.70 164 57.54 53 19.69 109 41.70 165 47.43 54 19.67 110 60.07 166 50.44 55 21.01 111 41.70 167 73.84								
47 22.68 103 51.73 159 94.21 48 22.23 104 51.73 160 50.33 49 18.81 105 40.46 161 63.82 50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163 39.16 52 19.69 108 41.70 164 57.54 53 19.69 109 41.70 165 47.43 54 19.67 110 60.07 166 50.44 55 21.01 111 41.70 167 73.84					f			
48 22.23 104 51.73 160 50.33 49 18.81 105 40.46 161 63.82 50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163 39.16 52 19.69 108 41.70 164 57.54 53 19.69 109 41.70 165 47.43 54 19.67 110 60.07 166 50.44 55 21.01 111 41.70 167 73.84					P			
49 18.81 105 40.46 161 63.82 50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163 39.16 52 19.69 108 41.70 164 57.54 53 19.69 109 41.70 165 47.43 54 19.67 110 60.07 166 50.44 55 21.01 111 41.70 167 73.84					1			
50 18.35 106 34.90 162 73.73 51 22.23 107 39.16 163 39.16 52 19.69 108 41.70 164 57.54 53 19.69 109 41.70 165 47.43 54 19.67 110 60.07 166 50.44 55 21.01 111 41.70 167 73.84					-			
51 22.23 107 39.16 163 39.16 52 19.69 108 41.70 164 57.54 53 19.69 109 41.70 165 47.43 54 19.67 110 60.07 166 50.44 55 21.01 111 41.70 167 73.84								
52 19.69 108 41.70 164 57.54 53 19.69 109 41.70 165 47.43 54 19.67 110 60.07 166 50.44 55 21.01 111 41.70 167 73.84								
53 19.69 109 41.70 165 47.43 54 19.67 110 60.07 166 50.44 55 21.01 111 41.70 167 73.84								
54 19.67 110 60.07 166 50.44 55 21.01 111 41.70 167 73.84								
55 21.01 111 41.70 167 73.84								
56 22.68 112 41.70 168 50.44	55	21.01	111		167			
	56	22.68	112	41.70	168	50.44		

Table 10. Absolute security minimum weight value of a good pack without missing components

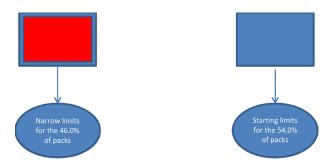
The value resulting is less than the final minimum weight that is 26,51 g, so it gets out of range. Therefore, the verification is successful and the values in Table 8, for the first product can be chosen as the weight limits for the balance.

So, the secure value for a good case without missing components is 26,51 g.

In Table 10 we have indicated with continuous red borders the products, whose weight value, obtained by subtracting the minimum weight of the lighter component to the maximum final weight, is within the range.

In this case, the balance could consider as good a pack with a missing component.

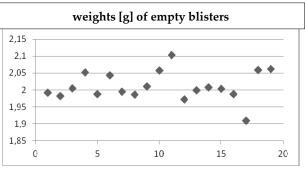
In particular, we can consider limits values such as in Table 8, for 54,01% of the products; while for 45,99% of cases (indicated with red borders in Table 10), it is necessary to use the new algorithm developed to determine new weight control limits (Figure 7).





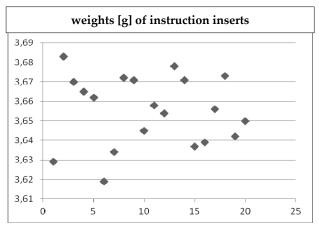
The starting point is the creation of families, as made previously, characterized by the same components weight. Subsequently, it is necessary to collect data in order to evaluate the average and the variance of each family, respecting the statistical significance (number of samples needed).

For example, in Figures 8 and 9, collected weights values, respectively of blisters and instruction inserts (two of the components in packages), are showed.



Units (empty blisters)

Figure 8. Example of data collection of weights of empty blisters



Units (instruction inserts)

Figure 9. Example of data collection of weights of instruction inserts

Then, it is possible to calculate the average and standard deviation (square root of variance) values (Table 11).

Component	μ	σ
Empty blisters	2.09	0.048
Instruction inserts	3.64	0.018

 Table 11. Averages and variances of empty blisters and instruction inserts

Considering the variability of each component, and applying the equations (4) and (5), it is possible to evaluate the weight minimum and maximum control limits for the considered family of filled packs (E.V. $\pm 3\sigma$) (e.g. in Table 12).



 Table 12. Family n.1 – control limits in the case of no missing component

At this point, it is necessary to verify the control limits modification because of a missing component (family average and standard deviation values reduction). By subtracting one component, component by component, new sets of control limits are obtained. By choosing the major maximum control limit in the case of one missing component, the definition of the suggested three weight control limits, and consequently of the below four control areas (discussed in the paragraph n. 3), is possible (Figure 10):

Point J: 51.02 g (minimum control limit in the case of no missing component)

Point K: 55.98 g (major maximum control limit in the case of missing components)

Point L: 58.48 g (maximum control limit in the case of no missing component)

AREA A: package weight <51.02 g AREA B: 51.02g ≤ package weight ≤ 55.98 g; AREA C: 55.98g < package weight ≤ 58.48 g; AREA D: package weight > 58.48g.

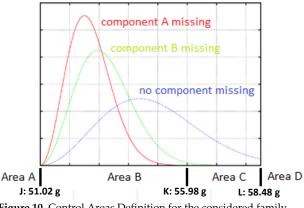


Figure 10. Control Areas Definition for the considered family

By applying the control limits suggested by the new algorithm and by monitoring the weight of packaged goods during a daily production, only two packages were rejected in AREA A (very low percentage, about 0,4%); about fifty percentage in AREA B required an inspection activity (sampling procedure definition); fifty percentage in AREA C were considered as correct packages; no one was found in AREA D (Figure 11).

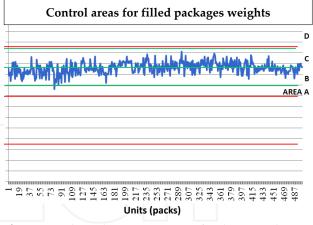


Figure 11. Daily production monitoring of packages weights

5. Conclusions

A checkweigher is an automatic or manual machine for checking the weight of packaged goods. It is used to ensure that the weight of a product is within specified limits. Packages outside the tolerance range are rejected and taken out of line through an automatic system.

The definition of the above tolerance and control limits is not so easy in the case of a significant weight variability and number of components. In the present paper a weighing algorithm has been developed to verify the content of pharmaceutical packages of different components. The basic idea is to link the weight check of filled packages to the control of the weight of each assembled component. Therefore the adoption of statistical approaches and tools has been necessary.

The proposed weighing procedure allows:

- to avoid missing components in the package;
- to alert double components in the package;
- to suggest the need of inspection sampling procedure;
- to send correct filled packages to the palletizing machinery.

In the future the algorithm will be tested in other production lines, inside and outside the pharmaceutical field.

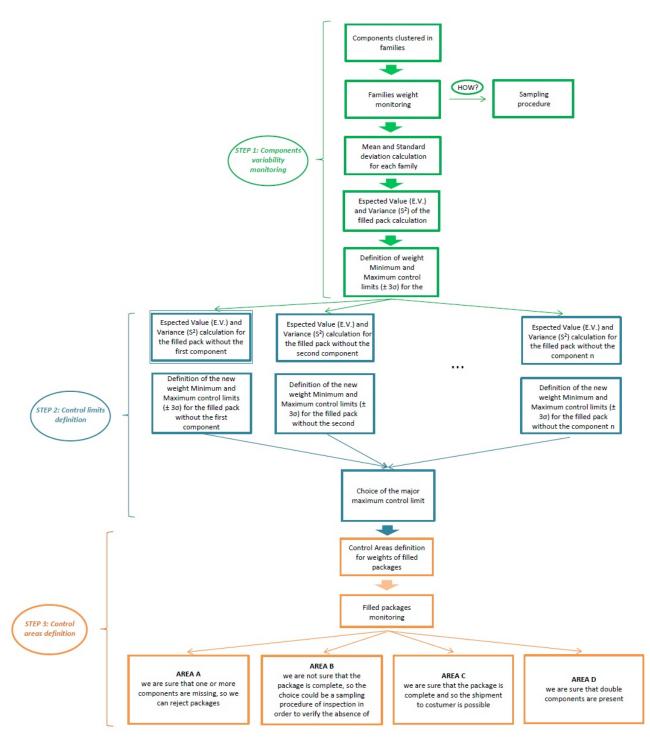
6. References

- Caputo A C, Pelagagge P M, Salini P, (2010) Genetic algorithm for optimal selection of feeding policies in assembly systems. Proc. 8th International Conference on Manufacturing Research ICMR10, Durham University, UK, in Vitanov V I, Harrison D, Advances in Manufacturing Technology XXIV, pp. 199- 204, ISBN 9781905866519.
- [2] Valcu A, Baicu S (2012) Analysis of the results obtained in the calibration of electronic analytical balances. Mass Laboratory, National Institute of Metrology (INM), Bucharest, Romania.
- [3] Crown L, Sefcik D, Warfield L (2013) Checking the net contents of packaged goods. National Institute of Standards and Technology, Handbook 133, Checking the Net Contents of Packaged Goods.
- [4] Das P, (2005) Developing control measures to reduce variation in weight of packed cement bags. Quality Engineering : Volume 17, Issue 4, pp. 609-614.
- [5] Dutheil C (2014) Inspecting pills and capsules. Issue 584, pp. 29-30.
- [6] Falcone D, Duraccio V, Silvestri A, Di Bona G (2005) Technical and economical analysis of the layout of a palletization plant through simulation techniques. Summer Computer Simulation Conference 2005, Part of the 2005 Summer Simulation Multiconference, SummerSim pp. 387 – 391.

- [7] Falcone D, Silvestri A, Forcina A, Pacitto A (2011) Modeling and simulation of an assembly line: A new approach for assignment and optimization of activities of operators. 10th International Conference on Modeling and Applied Simulation, MAS 2011, Held at the International Mediterranean and Latin American Modeling Multiconference, I3M 2011 pp. 202 – 206.
- [8] Falcone D, Silvestri A, Di Bona G, Forcina A, Pacitto A (2010) Study and modelling of very flexible lines through simulation. Proceedings of the 2010 Spring Simulation Multiconference - Emerging M and S Applications in Industry and Academia Symposium, EAIA pp. 11 – 16.
- [9] Falcone D, Forcina A, Di Bona G, Duraccio V, Silvestri A, Cerbaso C. (2013) Technical and economic verification of the convenience in reengineering a production line using simulation techniques. 25th European Modeling and Simulation Symposium, EMSS 2013 pp. 327 – 332.
- [10] National Weights and Measure Laboratory (2006) The Weights and Measures (Packaged Goods) Regulations. The National Archives, URN 07/1343.
- [11] Yam, K L (2009) Encyclopedia of Packaging Technology. John Wiley & Sons, ISBN 978-0-470-08704-6.
- [12] Compagno L, D'Urso D, Trapani N (2012) Designing an optimal shape warehouse. APMS 2012 International Conference, 24-26 September, Rhodes Island.
- [13] Hazewinkel, M., (2001) Central limit theorem. Encyclopedia of Mathematics, Springer, ISBN 978-1-55608-010-4.
- [14] Hazewinkel, M., (2001), Norma Distribution. Encyclopedia of Mathematics, Springer, ISBN 978-1-55608-010-4.



Annex 1



Flow diagram describing the new developed algorithm