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# Optimization of Land Distribution in Land Consolidation

Rajica MIHAJLOVIĆ, Manojlo MILADINOVIĆ, Mladen ŠOŠKIĆ – Belgrade<sup>1</sup>

ABSTRACT. This paper describes the research on the application of single criterion and multi-criteria optimization of land mass redistribution. The mathematical modeling of the basic requirements for distribution and an example of solving multi-criteria weight models is presented here in the paper.

Keywords: land consolidation, optimization, land mass, mathematical model, redistribution, weight coefficient model.

## 1. Introduction

Technologically speaking, land mass redistribution consists of dimensioning and positioning land consolidation blocks in the land consolidation area, distribution of values (areas), ordering of new lots in a block and determination of their analytical elements (Mihajlović 2010).

This paper propose the way to select the block to which the land holding will be distributed using mathematical optimization methods. During the process we ought to determine the size, number and shape of the new lots.

In the last thirty years there has been an intensive work on this problem and many papers (Kik 1980, de Vos 1992, Gostović 1979, Grafarend et al. 1979, Kik 1992, Kropff 1977, Lemmen et al. 1986, Pelzer 1972, Hoisl 1984, Wurzl 1984, Miladinović et al. 1994, Mihajlović 1995, Avci 1999, Sonnenberg 1990, Cay et al. 2004, Cay et al. 2006, Cay et al. 2008, Rosman et al. 1998, Mihajlović 2010)

<sup>&</sup>lt;sup>1</sup>Rajica Mihajlović, PhD, Geod. Eng., Faculty of Civil Engineering, University of Belgrade, Blvd. kralja Aleksandra 73, RS-11000 Belgrade, Serbia, e-mail: rajica@grf.bg.ac.rs,

Prof. Manojlo Miladinović, PhD, Geod. Eng., Faculty of Civil Engineering, University of Belgrade, Blvd. kralja Aleksandra 73, RS-11000 Belgrade, Serbia, e-mail: manem@grf.bg.ac.rs,

Mladen Šoškić, M.Sc., Geod. Eng., Faculty of Civil Engineering, University of Belgrade, Blvd. kralja Aleksandra 73, RS-11000 Belgrade, Serbia, e-mail: mladens@grf.bg.ac.rs.

showed that the help of computers and proven methods of operational research can automate and improve the methodology for developing the proposition (project) of the land mass redistribution and so give significant advantage comparing to the methods applied so far.

The land consolidation model<sup>2</sup> defined in this paper is based on the experiences from already implemented land consolidations and on the regulations in Serbia that are similar to the regulations in most European countries.

## 2. Defining Land Mass Redistribution as an Optimization Model

The conditions for production on agricultural land depend on fertility, shape, orientation<sup>3</sup>, size and distance between a lot and the holder yard, water, paved road or market. Optimal conditions for production can be achieved using optimization methods for ordering and dimensioning the new lots. Taking into account the rules and experience of land mass redistribution (Mihajlović 2010) certain redistribution requirements can be defined and mathematically modeled in the following way:

### 1. New lots should have the largest possible area (value)

The request for the largest possible areas, i.e. new lots' values, can be defined with the objective function (1), for which the maximum will be demanded.

$$\max F = \sum_{i=1}^{n} \sum_{j=1}^{m} w_{ij} x_{ij}$$
(1)

where:

 $w_{ij}$  – is distribution coefficient (criteria) for *j*-th participant in *i*-th block

 $x_{ii}$  – is unknown lot value of *j*-th participant in *i*-th block,

 $w_{ij}$  coefficient can represent the value of the old land consolidation participants in newly designed blocks, the distance between blocks and holder yards, the minimal differences of soil quality in the old and the new situation or wishes of the participants.

### 2. Distance between new lots and holder yards should be minimal

The request to minimize distance between new lots and holder yards and maximize the value of new lots can be defined with the objective function (2) for which the maximum will be demanded in the optimization model.

$$\max F = \sum_{i=1}^{n} \sum_{j=1}^{m} \frac{x_{ij}}{d_{ij}},$$
(2)

<sup>&</sup>lt;sup>2</sup>Land mass includes all the land consolidation area.

<sup>&</sup>lt;sup>3</sup> Position of the longer side of the lot according to the optimal planting zone.

where  $d_{ij}$  represents the distance between barycenter of *i*-th block and *j*-th holder's yard and can be determined using the designed road network.

### 3. New lots should have the most convenient shape

The request that a lot has the most convenient shape can be defined for the whole land consolidation area as the lower and upper limits for all lots (3), groups of block, individual block or even for each owner in each block.

$$x_{ij} \ge DL_i, \ x_{ij} \le GL_i, \ i = 1, 2, \dots, n, \ j = 1, 2, \dots, m$$
 (3)

where

 $DL_i$  – is the upper limit of new lots values in block *i*, and

 $GL_i$  – is the lower limit of new lots values in block *i*.

By defining the lower and the upper limits of new parcels and the project fixed table width we are directly determining their shape (a rectangle with the most appropriate aspect ratio).

### 4. The sum of new lots values should be equal to the sum of the old plots values

The request to give to each participant the value equal to the one they entered the land consolidation process with (decreased for the common area percentage, of course), is defined as the constrain function (4):

$$\sum_{i=1}^{n} x_{ij} = VP_{j}, \ j = 1, 2, \dots, m.$$
(4)

If in (2) would be requested that these values can be with  $\pm 10\%$  difference from the value that entered the land consolidation process, then there would be two groups of constraints that would represent the upper and the lower limit of the value assigned to the lot:

$$\sum_{i=1}^{n} x_{ij} = VP_{j}(0.9 + k)$$

$$\sum_{i=1}^{n} x_{ij} = VP_{j}(1.1 - k)$$

$$j = 1, 2, ..., m$$
(5)

where

 $VP_i$  - is the value of the *j*-th participant for redistribution,

- n is the number of land consolidation blocks,
- m is the number of participants whose holding is being distributed, and
- k is the common needs reduction coefficient.

### 5. Quality of old and new lots should have minimal difference

The request that the difference in the quality of the input land and redistributed lots be minimal can be defined with the following criteria function:

$$\max F = \sum_{i=1}^{n} \sum_{j=1}^{m} \frac{1}{|KP_j - KT_i|} x_{ij}$$
(6)

where

 $KP_{i}$  - is the ratio of the *j*-th owner's holding value and area, and

 $KT_i$  - is the ratio of the *i*-th block values and area.

The request set in (2) that the land distributed from redistribution's land mass can differ not more than  $\pm 20\%$  from the area inputed to redistribution's land mass could be roughly defined by two sets of constraints:

$$\sum_{i=1}^{n} \frac{1}{KT_{i}} x_{ij} \geq \frac{VP_{j}}{KP_{j}} (0.8+k), \quad (j = 1, 2, ..., m),$$

$$\sum_{i=1}^{n} \frac{1}{KT_{i}} x_{ij} \leq \frac{VP_{j}}{KP_{j}} (1.2-k), \quad (j = 1, 2, ..., m),$$
(7)

where k is the common needs reduction coefficient.

### 6. Same or smaller distance from the old and new lots to the holders yards

One solution to defining this request could be done with the objective function of the form (1) where the coefficient  $w_{ij}$  take the sum of the values of the old lots in newly designed blocks  $c_{ij}$  and for such objective function maximum is requested in the optimization model.

$$\max F = \sum_{i=1}^{n} \sum_{j=1}^{m} c_{ij} x_{ij}$$
(8)

Another possibility for defining the request for equal (or smaller) distances between old and new properties is to define the groups of constraints (9):

$$\sum_{i=1}^{n} PN_{ij} x_{ij} \ge \sum_{l=1}^{p} PS_{lj} v_{lj}, \ (j = 1, 2, \dots, m).$$
(9)

That is, if we take the reciprocal values of distance from holder's yards to the barycenter of new block and the defined sector of old state for the path parameters (Kik 1980) it will be:

$$\sum_{i=1}^{n} (1/d_{ij}) x_{ij} \ge \sum_{l=1}^{p} q(1/f_{lj}) v_{lj}, \quad (j = 1, 2, \dots, m),$$
(10)

### where

- $PN_{ij}$  is the parameter of the path between *j*-th owner's yard and *i*-th block,
- $PS_{lj}\,$  is the parameter of the path between  $j\mbox{-}th$  owner's yard and  $l\mbox{-}th$  old state sector,
- $f_{li}$  is the distance between *j*-th participant's yard and *l*-th old state sector,
- $v_{li}$  is the value of *j*-th participant's holding from the old state in *l*-th sector,
- p is the total number of sectors in the old state,
- $x_{ii}$  is the unknown values of *j*-th participant's lot in *i*-th block,
- $d_{ii}$  is the distance between *j*-th participant's yard and *i*-th block, and
- q is the coefficient of proportionality which defines the functional difference between old and new path network.

### 7. Respect wishes of the land consolidation participants for the land grouping

Participants' wishes can be taken separately for the location (block) of the future lot and for the size (value) of that lot or for the location and size of a future lot at the same time. Thus, for example, the wish coefficient may take: for the first wish -100 points, for the second -80 points, 60 points for third and so on.

Another solution is that the participant declare in which block he wants to get a lot, to give a number of alternatives and the sizes of the lot and possible variations from the given size (range). Based on the wishes defined this way, we could adopt the following limits:

$$\begin{split} x_{ij} &\geq DZ_{ij}, \text{ za } DZ_{ij} > 0; \quad x_{ij} \leq GZ_{ij}, \text{ za } GZ > 0, \\ x_{ij} &= 0, \text{ za } DZ_{ij} = GZ_{ij} = 0, \ (i = 1, 2, \dots, n; \ j = 1, 2, \dots, m) \end{split}$$

where

 $DZ_{ij}$  – is the lower limit for *j*-th participant's wish to get a lot in *i*-th block, and  $GZ_{ij}$  – is the upper limit for *j*-th participant's wish to get a lot in *i*-th block. The land mass redistribution based on the principle of wishes is given in Hupfeld (1971) and Mihajlović (2010).

# 8. The sum of new lots values distributed in one block should be equal to the value of that block

The criterion that the sum of values distributed to a block should be equal to the value of that block can be represented as a group of constraints whose general formula is:

$$\sum_{j=1}^{m} x_{ij} = VT_i, \ (i = 1, 2, \dots, n).$$
(12)

where  $GZ_i$  is the value of the reallocation blocks.

Certain deviation of the sum of new lots values from the block value could also be allowed for these requirements (e.g.  $\pm 10\%$ ). In that case, the constraints (12) would give two sets of constraints:

$$\sum_{j=1}^{m} x_{ij} \ge 0.9 \cdot VT_i, \ (i = 1, 2, ..., n), \quad \sum_{j=1}^{m} x_{ij} \le 1.1 \cdot VT_i, \ (i = 1, 2, ..., n),$$
(13)

### 9. The maximum and minimum for the number of lots per each owner

The maximum number for the number of lots per each owner can be written as:

$$\sum_{i=1}^{n} k_{ij} \le MG_{j}, \ (j = 1, 2, \dots, m)$$
(14)

Similarly, the minimum number of lots of an owner can be defined as:

$$\sum_{i=1}^{n} k_{ij} \ge MD_{j}, \ (j = 1, 2, \dots, m)$$
(15)

where

 $k_{lj}$  – is the binary variable (0 or 1) (i = 1,2,...,n; j = 1,2,...,m),

 $MG_j$  – is the maximal number of distributed lots to *j*-th owner, and

 $MD_j$  – is the minimal number of distributed lots to *j*-th owner.

The defined constraints have to do with the shape of new lots, so when defining number of lots in the block one must keep that in mind. This could be introduced as the restrictions when using binary integer programming or mixed programming. The defined constraints could be used as constraints when applying binary integer programming (BIP) or mixed programming.

### 10. The maximum and minimum for the number of lots per each block

The maximum for the number of lots per each block can be constrained with equations:

$$\sum_{j=1}^{m} k_{ij} \le NG_i, \ (i = 1, 2, \dots, n)$$
(16)

While the minimum number of lots per each block is defined with the group of constraints:

$$\sum_{j=1}^{m} k_{ij} \ge ND_i, \ (i = 1, 2, \dots, n)$$
(17)

where

 $k_{ij}$  — is binary variable (0 or 1) (i = 1, 2, ..., n; j = 1, 2, ..., m),  $NG_{ij}$  — is maximal number of distributed lots in *i*-th block, and  $ND_{ij}$  — is minimal number of distributed lots in *i*-th block. This group of constraints is also only applicable in case of binary or mixed programming, as the previous one.

## 3. Optimization Models of Land Mass Redistribution

Mathematical models can be defined as single criterion or as multi-criteria optimization models by combining certain mathematically modeled requirements from Chapter 2.

### 3.1. Single Criterion Optimization Model

Considering the general formulation of linear programming mathematical model (Mihajlović 2010) adapted to solving with simplex method and mathematically modeled requirements for grouping lots and land mass redistribution in Chapter 2, the following mathematical model could be set as:

Objective function

$$\max F = \sum_{i=1}^{n} \sum_{j=1}^{m} w_{ij} x_{ij}$$
(18)

with constraints

$$\sum_{j=1}^{m} x_{ij} = VT_i, \ i = 1, 2, \dots, n, \ \sum_{i=1}^{n} x_{ij} = VP_j, \ j = 1, 2, \dots, m$$

$$DL \le x_{ij} \le GL, \ i = 1, 2, \dots, n; \ j = 1, 2, \dots, m.$$
(19)

Therefore, we seek the maximum value of objective function F which is the product of distribution coefficients  $w_{ii}$  and the unknown values of new lots  $x_{ii}$ .

Coefficient  $w_{ij}$  and unknowns  $x_{ij}$  in the objective function can represent the following properties:

- 1) the sum of the old lots of redistribution participants that fall into the newly designed blocks  $w_{ij} = c_{ij}$ ,
- 2) the reciprocal of distance between land consolidation blocks and holders' yards  $w_{ij} = d_{ij}^{-1}$ ,
- 3) the reciprocal of the absolute difference between the ratio of lots (holdings) values and area which participants entered the land consolidation process with and ratio of reallocation blocks values and area  $w_{ii} = |KP_i KT_i|^{-1}$ , and
- 4) wishes of land consolidation participants in percents (points) according to priorities  $(w_{ij} = z_{ij})$ ; for instance:  $z_{ij}$  could take 100 for the primary desire, 80 for the first alternative, 60 for the second alternative, etc.

The groups of constraint can be defined by combining the equations defined in Section 2. Inequality sign may be used in place of equality sign. Then it can be allowed to distribute lower or higher value of new lots for a defined percentage (e.g. 10%) to a block and to compensate in money. The system of inequality constraints can be extended to new groups of equalities or inequalities. The first group of constraint equalities (19) can be replaced with two new groups of constraints:

$$\sum_{i=1}^{n} x_{ij} \ge VP_{j}(0.9+k), \ (j=1,2,\ldots,m), \ \sum_{i=1}^{n} x_{ij} \ge VP_{j}(1.1-k), \ (j=1,2,\ldots,m),$$
(20)

The second group of constraints (19) can also be replaced with two new equalities:

$$\sum_{j=1}^{m} x_{ij} \ge 0.9 \cdot VT_i, \ (i = 1, 2, ..., n), \quad \sum_{j=1}^{m} x_{ij} \le 1.1 \cdot VT_i, \ (i = 1, 2, ..., n),$$
(21)

### 3.2. Multi-criteria Optimization Model

Multi-criteria programming allows introducing more objective criteria functions. Considering mathematical modeling of the land mass redistribution that is presented in Chapter 2 it is evident that the multi-criteria programming can include a greater number of defined requirements simultaneously, thus allowing objective optimization of land mass redistribution. For instance, the four objective functions in multi-criteria model taken from Chapter 2 can be defined by:

$$\max F_{1} = \sum_{i=1}^{n} \sum_{j=1}^{m} c_{ij} x_{ij}, \quad \max F_{2} = \sum_{i=1}^{n} \sum_{j=1}^{m} d_{ij}^{-1} x_{ij},$$

$$\max F_{3} = \sum_{i=1}^{n} \sum_{j=1}^{m} |KP_{j} - KT_{i}|^{-1} x_{ij}, \quad \max F_{4} = \sum_{i=1}^{n} \sum_{j=1}^{m} z_{ij} x_{ij}$$
(22)

The forming of a mathematical model starts from the fact that the distribution coefficients in criteria function (22)  $(w_{ij} = c_{ij}, w_{ij} = d_{ij}^{-1}, w_{ij} = |KP_j - KT_i|^{-1}$  or  $w_{ij} = z_{ij}$ ) are not in the same measurement units and thus must be normalized like in (23) and (24).

$$g_{kij} = \frac{w_{kij}}{\sum_{j=1}^{m} w_{kij}}, \quad i = 1, \dots, n, \quad k = 1, \dots, p$$
(23)

Normalized objective function has the following form:

$$\max F_k = \sum_{i=1}^n \sum_{j=1}^m g_{kij} x_{ij}, \text{ za } k = 1, 2, \dots, p = 4;$$
(24)

The final objective function is reduced to single criterion function:

$$\max G = \sum_{i=1}^{n} \sum_{j=1}^{m} q_k g_{kij} x_{ij}, \text{ za } k = 1, 2, \dots, 4;$$
(25)

where  $q_k$  is weight coefficient of each function.

Limits, with such defined objective functions, can be made by combining the equations defined in Section 2. For instance, they may be:

$$\sum_{i=1}^{n} x_{ij} = VP_{j}, \text{ za } i = 1, 2, ..., n; \quad \sum_{j=1}^{m} x_{ij} \ge VT_{i} \cdot P1_{i}, \text{ za } i = 1, 2, ..., n$$
$$\sum_{j=1}^{m} x_{ij} \le VT_{i} \cdot P2_{i}, \text{ za } i = 1, 2, ..., n$$
(26)

 $x_{ij} \leq GL, \text{ za } i=1, 2, \dots, n; \ j=1, 2, \dots, m, \ x_{ij} \geq DL, \ \text{za } i=1, 2, \dots, n; \ j=1, 2, \dots, m,$ 

where

 $VT_i \cdot P1_i$  is the upper limit of the sum of new lots that fall in the block *i*,

 $VT_i \cdot P2_i$  is the lower limit of the sum of new lots that fall in block *i*.

For the coefficients P1 and P2 deviations percentage (e.g. 2%) could be taken to the discretion of (the designers) but their value does not exceed  $\pm 10\%$ .

Thus a mathematical model can further customized to specificity of the methods defined to solve multi-criteria optimization problems such as interactive methods for solving like the STEM (STEP Method) method, weight coefficients method, the criteria functions space bound methods or the goal programming (Mihajlović 2010).

## 4. Example of the Application of Optimization Models in the Land Mass Redistribution

A mathematical model from (19) is tested on land consolidation area of 106.9727 ha with 261 lots before land consolidation that were belonging to 16 participants with an average 0.4098 ha.

Figure 1 shows the lots before and after the land consolidation obtained by applying multi-criteria weight coefficients method with four objective functions with the same weight of 0.25.

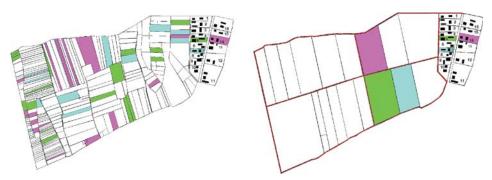


Fig. 1. Lots before and after optimized land consolidation.

	Properties of holdings before land consolidation						
Holder	Number of lots in old state	Total area of lots (ha)	Total value of lots	Average value of lots	Ratio value over area		
1	17	43069.8	30523.3	1795.5	0.70859		
2	19	79095.0	60700.8	3194.8	0.69206		
3	11	21051.1	16035.4	1457.0	0.73462		
4	15	66331.5	50778.2	3385.2	0.66960		
5	19	71010.3	52609.1	2768.9	0.65574		
6	21	67658.9	50813.4	2419.7	0.78170		
7	13	64811.3	51444.8	3957.3	0.63951		
8	19	64906.4	48365.1	2545.5	0.72841		
9	21	89291.7	70351.2	3350.1	0.76747		
10	16	78213.8	54128.1	3383.0	0.76277		
11	16	68124.7	49930.5	3120.7	0.76731		
12	12	43407.8	29089.4	2424.1	0.74102		
13	10	101876.8	66882.8	6688.3	0.75112		
14	19	82061.8	64148.0	3376.2	0.79392		
15	18	75006.4	47966.7	2664.8	0.74519		
16	15	53809.3	39183.1	2612.2	0.78784		
Total	261	1069726.6	7829499	2999.8	0.73192		

Table 1. Data on holdings of the participants in the old state of consolidation.

Table 1 shows the basic data on each participant's holding in the state before, and in Table 2 after, land consolidation as a result of the multi-criteria optimization weight coefficients method with four objective function (22), i.e. (25) with the same weight 0.25.

Calculation of the new lots values in land consolidation blocks was done using the MATLAB script named *VKRaspodelaTK* (Nikolić 1994) based on the mathematical model presented in (Vujošević et al. 1996, Martić 1978, Wagner 1975, Opricović 1998). Arrangement of new plots in one land consolidation block is done with script *Nadela* of *OPKOM* script library (Mihajlović 2010).

By analyzing the distribution criteria  $w_{ij}$  it can be seen that the (18) criteria 1)  $(w_{ij}=c_{ij})$  and 4)  $(w_{ij}=z_{ij})$  initially limit the distribution of new lots only to blocks where there are old lots in possession of a participant or where there is a defined desire, while criteria 2)  $(w_{ij}=d_{ij}^{-1})$  and 3)  $(w_{ij}=|KP_j-KT_i|^{-1})$  include the entire land consolidation area (every block).

Based on the results shown in Table 2, 19 new lots were obtained with an average value of 40817.7 a and enlargement coefficient of 13.7 times.

Holder number		Land consolidation blocks				
		T1	T2	T3	T4	
1	objective func. ceof. g	0.66	0.39	0.55	0.66	
	value of lot x				30087.7	
2	objective func. ceof. g	0.65	0.37	0.74	0.85	
	value of lot x				54074.9	
3	objective func. ceof. g	0.78	0.51	0.51	0.52	
	value of lot x	48665.5				
	objective func. ceof. g	0.55	0.29	1.05	1.10	
4	value of lot x				29103.6	
	objective func. ceof. g	0.27	0.35	6.22	1.45	
5	value of lot x			66795.9		
6	objective func. ceof. g	0.87	0.90	1.23	0.40	
	value of lot x	63505.1				
7	objective func. ceof. g	0.30	0.28	12.32	2.76	
	value of lot x			48444.4		
8	objective func. ceof. g	0.46	0.46	1.83	0.55	
	value of lot <i>x</i>			6725.2	31488.6	
	objective func. ceof. g	0.75	1.00	0.00	0.49	
9	value of lot x	6489.8	53582.8			
10	objective func. ceof. g	0.64	0.89	0.00	0.42	
	value of lot x				15321.9	
11	objective func. ceof. g	0.72	0.95	0.42	0.48	
	value of lot x	41467.1			6220.6	
12	objective func. ceof. g	0.54	0.74	0.54	0.53	
	value of lot x				50968.4	
13	objective func. ceof. g	1.10	0.92	0.47	0.36	
	value of lot x	51048.9				
14	objective func. ceof. g	1.61	2.12	0.00	0.28	
	value of lot <i>x</i>		51828.6			
15	objective func. ceof. g	1.13	0.91	0.50	0.37	
	value of lot <i>x</i>	48645.9				
16	objective func. ceof. g	1.54	1.95	0.40	0.29	
	value of lot <i>x</i>		71015.0			

Table 2. The distribution of new lots values in blocks using the weight coefficients method with four of the objective function with the same weights 0.25.

## 5. Concluding Remarks

Solving the land mass redistribution model is in most cases the large-scale problem and requires a professional software without software-hardware limitations. This is achieved to a large extent with software solutions from this work and from (Mihajlović 2010) which led to a solid basis for further works and improvements. According to the performed analysis it can be concluded that the weight coefficients method provides very useful results making it easier for decision maker by providing objective and optimal results.

Based on the research and obtained solutions from this work we can conclude that a real basis is created for further research and improvements of theoretical, technological and practical achievements.

### References

- Avci, M. (1999): A new approach orientated to new reallotment model based on block priority method in land consolidation, Turkish Journal of Agriculture and Forestry, 23, 451–457.
- Cay, T. et al. (2004): Algorithm developing for land consolidation software XX, ISPRS Congress, III, Turkey, 666–671.
- Cay, T. et al. (2006): Optimization in Land Consolidation, XXIII FIG Congress Munich, Germany.
- Cay, T. et al. (2008): A New Land Reallocation Model for Land Consolidation, FIG Working Week, Stockholm, Sweden.
- de Vos, W. H. (1992): Allocation in Land Consolidation Projects in The Netherlands with the Aid of an Automated System, Surveying and Mapping, Vol. 42, No. 4.
- Gostović, M. (1979): Model raspodele komasacione mase, Geodetski list, 10–12, 319–335.
- Grafarend, E. et al. (1979): Optimierung geodäticher Meroperationen, Teil III Optimierung der Flurbereinigung, Sammlung Wichman Neue Flge, Band II, Part II, Wichman Verlang Karlsruhe, 437–461.
- Kik, R. (1980): Reallotment of Farm Lands by Computer, Research Digest 1980, Icw, Wageningen, 179–181.
- Kik, R. (1992): Reallotment research in land improvement projects, Wageningen.
- Kropff, H. (1977): Ein Optimierungsansatz zur Automatisierung von Zuteilungsplanen in der Flurbereinigung, Schriftenreihe für Flurbereiningung, Heft 65, Landwirtschaftsverlag Münster – Hiltrup, West Germany.
- Lemmen, C. H. J. et al. (1986): A model for allocation and adjustment of lots in land consolidation, New development in the Netherlands, Federation Internationale des Geometres, XVIII International Congress, Toronto, Canada, Invited Paper 706.5, 326–341.
- Martić, Lj. (1978): Višekriterijumsko programiranje, Informator, Zagreb.
- Mihajlović, R. (1995): Primenom linearnih metoda operacionih istraživanja kod raspodele komasacione mase, magistarski rad, Građevinski fakultet, Univerzitet u Beogradu, Beograd.

- Mihajlović, R. (2010): Optimizacija raspodele komasacione mase kod uređenja zemljišne teritorije komasacijom, doktorska disertacija, Građevinski fakultet, Univerzitet u Beogradu, Beograd.
- Miladinović, M. et al. (1994): Raspodela komasacione mase primenom metoda linearnog programiranja, YU-SYM-OP-IS'94, Kotor.
- Nikolić, I. (1994): MATLAB Users Guide, MathWorks, Inc.
- Opricović, S. (1998): Višekriterjumska optimizacija sistema u građevinarstvu, Građevinski fakultet, Beograd.
- Pelzer, H. (1972): Zur Berechnung optimaler Zuteilungspläne bei der Flurbereinigung, Vermessungstechnische Rundschau, Heft 9.
- Rosman, F. B. et al. (1998): New Method for the Design of the Re-allocation Plan in Land Consolidation Projects, Federation Internationale des Geometres, XXI Congress, Brighton, UK, 232–245.
- Sonnenberg, J. K. B. (1990): Acquisition, disposal and allocation of land for non-agricultural purposes by land consolidation, Federation Internationale des Geometres, XIX International Congress, Helsinki, Finland, Invited Paper 705.1, 186–188.
- Vujošević, M. et al. (1996): Metode optimizacije mrežni lokacijski i višekriterijumski modeli, Dopis, Beograd.
- Wagner, H. M. (1975): Principles of Operation Research, with applications to Managerial Decisions, Second Edition, London.

## Optimizacija raspodjele komasacijske mase

SAŻETAK. U radu su prikazana istraživanja vezana za primjenu jednokriterijske i višekriterijske optimizacije kod raspodjele komasacijske mase. Izvedeno je matematičko modeliranje osnovnih zahtjeva raspodjele i prikazan je primjer rješavanja višekriterijskog modela metodom težinskih koeficijenata.

Ključne riječi: komasacija, optimizacija, komasacijska masa, matematički model, raspodjela, metoda težinskih koeficijenata.

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