

APPLICATION OF NEW MODELING METHODS OF THE PRODUCTION OF NITROGEN OXIDES IN THE COMBUSTION MODE OF BIOMASS

MÁRIA ČARNOGURSKÁ, MIROSLAV PŘÍHODA¹, MARCEL KOŠKO

Technical Univerzity in Košice, Faculty of Mechanical Engineering, Košice, Slovakia

¹VŠB TU Ostrava, Faculty of Metallurgy and Materials Engineering, Ostrava, Czech Republic

e-mail: maria.carnogurska@tuke.sk

The process of elaboration and consequent verification of mathematical model of NO_x production during wood combustion based on the dimensional analysis theory is presented in this paper. The model is based on selected physical quantities which can be measured continually during the boiler operation. Primarily, the model was elaborated for boiler type VERNER V210 of 20 kW performances and its validity was also verified for the same construction type of boiler of lower performance (14 kW). Lump wood of lower calorific value of approximately $15 \text{ MJ}\cdot\text{kg}^{-1}$ was used as a fuel in the boilers. The results showed that the dimensional analysis can be applied to describe such a complex phenomenon as the NO_x production during wood combustion.

Key words: mathematical modelling, nitrogen oxides, dimensional analysis, wood combustion.

Primjena novih metoda modeliranja tvorbe dušikovih oksida u procesu izgaranja biomase. U ovom radu prikazan je postupak formulacije i naknadne provjere valjanosti matematičkog modela tvorbe NO_x tijekom izgaranja drvene mase na temelju teorije dimenzijske analize. Model se temelji na odabranim fizikalnim veličinama koje se mogu kontinuirano mjeriti tijekom rada kotla. Prije svega, model je formuliran za kotao tipa Verner V210 učina od 20 kW i njegova valjanost je također provjerena za isti konstrukcijski tip kotla nešto nižeg učina (14 kW). Komadi drveta niže ogrjevnosti od oko $15 \text{ MJ}\cdot\text{kg}^{-1}$ korišteni su kao gorivo u kotlovima. Rezultati su pokazali da se dimenzijska analiza kao metoda može primijeniti za opisivanje takovih kompleksnih pojava kao što je tvorba NO_x tijekom izgaranja drvene mase.

Ključne riječi: mathematical modelling, nitrogen oxides, dimensional analysis, wood combustion.

INTRODUCTION

For the purpose of obtaining heat the burning of wood, bark and wood waste are ranked among standard procedures for use or disposal of phytomass. While the use of phytomass for energy purposes was a priority in the past, its importance gradually declined in the power industry and wood became only a suitable additional fuel.

Formation of nitrogen oxides during dendromass combustion is particularly associated with nitrogen compounds contained in the fuel.

Their elimination in low power devices is quite complicated. In high performance devices their elimination is possible by a substoichiometric combustion and supplying the combustion air in several levels. For

elimination of thermal nitrogen oxides it is important to prevent formation of areas with high temperature and high excess air [10]. The issues of thermal lignin decomposition during combustion of wood at 400 °C are dealt with in e.g. [5], [6]. The description of nitrogen oxides concentration in the exhaust gases, generated during the low-temperature oxidation, depending on the amount of nitrogen contained in fuel, is dealt with in the work [8].

Currently there is a large number of small heat sources fired by dendromass on the Slovak market. It is possible to burn wood in the form of logs, chips, pellets, briquettes, etc. Small heat sources for combustion of wood, and various forms of its waste, must meet the requirements, set out by relevant European and Slovak standards, as well as the relevant health regulations. Among the basic parameters observed in small heat sources are such parameters as heat performance and the method of combustion process regulation.

Other monitored parameters are boiler efficiency, the requirements in terms of environmental impact and safety requirements. From the energy point of view it is necessary to ensure the most effective utilisation of the energy contained in the fuel. The quality of combustion in a confined space of the boiler depends mainly on the temperature of combustion, the method of separation of the various phases of burning, thoroughness of combustible gases mixing with oxygen at the required reaction temperature, excess air and manner of distribution of primary and secondary air [6].

Given the complexity of the exact description of the process of creating nitrogen oxides during different conditions

of wood combustion, it is not possible to develop a generally applicable model that would describe such production for various types of boilers, for various forms of fuel (sawdust, wood pieces, chips), and various types of wood (spruce, fir, beech, pine, etc.). The issue of burning wood and developing of a mathematical formula for production of nitrogen oxides is dealt with by several authors, e.g. [2], [8], [9]. These models are often very complicated. They are usually based on "chemistry" of wood conversion during its combustion and the determination of nitrogen oxides volume using them is rather difficult. Therefore even today the possible applications of new procedures and methods to describe the formation of nitrogen oxides while dendromass is being burnt are searched.

One of the possible tools, suitable for modeling of various processes, is the dimensional analysis, see [1,7], used primarily in the field of fluid mechanics and thermomechanics. The authors attempted to apply this theory to modeling of the nitrogen oxides formation during combustion of the wood in boilers with small output power. So far, there is no any work to describe this phenomenon employing the dimensional analysis.

The created model in this paper is based on the selected physical quantities, which are continuously measurable during operation of the combustion equipment. In the presented model the attention is paid mainly to the impact of particular operational parameters on the production of nitrogen oxides during combustion of a particular type of wood with a specific calorific value [3], [4], [11].

NITROGEN OXIDES PRODUCTION

It is documented that the wood nitrogen content is different and depends

mainly on tree species. The average nitrogen content in the wood of conifers is

approximately $N = 0.03 \%$, and in the hard wood of deciduous trees is up to $N = 0.15 \%$. The average presence of nitrogen in the bark of conifers is approximately $N = 0.40 \%$, and in the bark of deciduous trees up to $N = 0.72 \%$ [12]. During the combustion of wet wood and bark in grate furnaces of the heating units the nitrogen oxides are formed only through low-temperature oxidation of the part of nitrogen bound in the fuel. Their production is dependent upon the amount of nitrogen contained in the fuel and the portion of nitrogen in the fuel transformed into emissions. The fact that the nitrogen content in wood and bark of trees is not the same means that also the concentrations of nitrogen oxides in exhaust gasses from these trees are different.

The wood as a fuel is characterized by moderate high calorific value, a high portion of volatile combustible material and low ash content.

The methodology of the model development for description of the NO_x production during combustion of wood involves the correlation between the nitrogen contained in the wood and nitrogen oxides contained in the exhaust gasses only through the temperature of exhaust gasses at the exit from the boiler. It is supposed that this temperature is directly related to the temperature in the furnace. The type of wood

and the influence of nitrogen content in the wood may not be taken into account directly in the actual development of the model. This influence is reflected in the model through the in situ measured values of selected variables forming a model. The measured nitrogen oxides reflect the quality and the nature of the combustion process, the impact of the burnt trees and their corresponding nitrogen content in wood and bark. The influence of the combusting wood type, and thus the nitrogen content in the fuel, on the actual production of nitrogen oxides is expressed only by obtained constants A , B in the equation (17), which in the developed model will be for each type of wood and its calorific value different. These constants for the type of combusted dendromass must be obtained by an experiment.

The developed model for the determination of nitrogen oxides, presented later in this article, is of general validity, but the constants A and B contained in it apply only to combusted wood with particular nitrogen content in it as its current calorific value. Therefore, if the other type of wood is combusted than wood burned during the guarantee measurements for the VERNER boiler (dry beech wood logs of length about 34 cm), it is necessary to re-establish the constants A and B appearing in the equation (17) of the developed model.



Figure 1. Lump wood boiler of VERNER V210 type

Slika 1. Kotao tipa VERNER V210 za loženje komadima drveta

The VERNER's boilers (Fig. 1), of V210 type with output of 20 kW and of V140 type with output 14 kW, are hot water boilers fuelled by wood and are designed for efficient, comfortable and environmentally friendly heating of houses, residential units, operations and similar facilities with heat loss ranging

from 14 kW to 20 kW. Both boilers are based on the principle of two stage combustion, where there is fuel gasification followed by combustion of generated gases. Technical parameters of the two boilers are shown in the Table 1.

Table 1. Parameters of VERNER boilers

Tablica 1. Tehničke karakteristike VERNER kotlova

BOILER	V140	V210
Rated power (kW)	14	20
Efficiency (%)	90	90
Variability by continuous operation (kW)	7 - 14	10 - 20
Variability by shutdown mode of operation (kW)	2 - 7	3 - 10
Total weight (kg)	330	370
Height (without exhaust cover) (mm)	1230	1230
Width (mm)	580	580
Depth (mm)	825	925
Diameter of exhaust gasses hub (mm)	160	160
Volume of the feed chamber (l)	55	75
Fuel consumption at rated output (kg·h ⁻¹)	3.6 - 3.8	4.2 - 5.7
Minimum return temperature of water (°C)	55	55

BOILER	V140	V210
Exhaust gasses temperature at the exit (°C)	150	155
Water volume (l)	30	32
Calorific value (MJ·kg ⁻¹)	14.52	15.45
Exhaust gasses mass flow rate (kg·s ⁻¹)	0.01	0.015
Minimum operating thrust of the exhaust (Pa)	10	10
Emission class of the boiler	3	3
Range of outlet water temperature control (°C)	60 - 90	60 - 90
Fuel used during warranty period (dry wood)	diameter: up to 15 cm, length: up to 35 cm	
Other type of fuel:	wooden briquettes, sawdust, dry wood chips	
The maximum noise level (dB)	55	55

PROCEDURE STATEMENTS BY MATHEMATICAL MODEL

Among the relevant variables affecting the production of nitrogen oxides during combustion of wood in the analysed combusting equipment, based on the knowledge from specialized literature, the physical quantities accompanying the

combustion process have been chosen, which are measurable on the operated combustion equipment. These are following quantities, which should be expressed in the system of basic units for the application in the dimensional analysis:

- boiler performance P_k ($W \equiv \text{kg} \cdot \text{m}^2 \cdot \text{s}^{-3}$),
- the amount of combustion air Q_{vz} ($\text{m}^3 \cdot \text{s}^{-1}$),

- calorific value Q_u ($J \cdot kg^{-1} \equiv m^2 \cdot s^{-2}$),
- exhaust gasses temperature at the end of the boiler T_{sk} (K),
- combustion air temperature T_{vz} (K),
- nitrogen oxides NO_x ($kg \cdot m^{-3}$).

The complete physical equation expressing the dependence of selected relevant dimensional quantities with different dimensions, including the production of NO_x , has, in terms of dimensional analysis, the expression

$$f(P_k, Q_{vz}, Q_u, T_{sk}, T_{vz}, NO_x) = 0 \quad (1)$$

From the requirements of dimensional diversity implies that the variables in the equation may not stand alone, but in the form of product

$$\pi = (P_k^{x_1}, Q_{vz}^{x_2}, Q_u^{x_3}, T_{sk}^{x_4}, T_{vz}^{x_5}, NO_x^{x_6}) \quad (2)$$

The expression of dimensionless arguments is based on the dimensional matrix, which for basic units of selected quantities in the total number of columns $n = 6$ and rows $m = 4$ has the form

$$\begin{matrix} & P_k & Q_{vz} & Q_u & T_{sk} & T_{vz} & NO_x \\ m & \left\| \begin{matrix} 2 & 3 & 2 & 0 & 0 & -3 \end{matrix} \right\| \\ s & \left\| \begin{matrix} -3 & -1 & -2 & 0 & 0 & 0 \end{matrix} \right\| \\ kg & \left\| \begin{matrix} 1 & 0 & 0 & 0 & 0 & 1 \end{matrix} \right\| \\ K & \left\| \begin{matrix} 0 & 0 & 0 & 1 & 1 & 0 \end{matrix} \right\| \end{matrix} \quad (3)$$

The matrix rows are not linearly dependent, so that the rank of the matrix is $h = m = 4$. With the number of relevant quantities $n = 6$ the total number of created arguments will be

$$i = n - m,$$

i.e. 2 dimensionless arguments π . In their determination we proceed so the rectangular dimensional matrix [3], the relationship (3), is split into two parts. One part is a square matrix – the **A** matrix in the relation (4), and the second part is the complementary matrix (matrix **D**). The selection of columns from the equation (3) for the square matrix **A** should be such that its determinant is nonzero. Also the selection of the vector of unknown quantities x_i (matrix **B** and **E**) should be adapted to the selection of columns. This procedure is expressed by equation (4) and (5).

$$\mathbf{A} \cdot \mathbf{B} = (-1) \cdot \mathbf{D} \cdot \mathbf{E} \quad (4)$$

$$\left\| \begin{matrix} 2 & 3 & 2 & 0 \\ -3 & -1 & -2 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{matrix} \right\| \cdot \left\| \begin{matrix} x_1 \\ x_2 \\ x_3 \\ x_5 \end{matrix} \right\| = (-1) \cdot \left\| \begin{matrix} 0 & -3 \\ 0 & 0 \\ 0 & 1 \\ 1 & 0 \end{matrix} \right\| \cdot \left\| \begin{matrix} x_4 \\ x_6 \end{matrix} \right\| \quad (5)$$

The value of matrix **A** determinant is $\Delta_A = -4$. The selection of the excess unknowns x_4 and x_6 from the equation (5) will be carried out twice, whereby both selections must be linearly independent

	x_4	x_6
1st selection	0	1
2nd selection	1	0

The matrix of independent selections is always square and in the above expression represents identity matrix in the form

$$\begin{vmatrix} 0 & 1 \\ 1 & 0 \end{vmatrix} \quad (6)$$

It may also be chosen otherwise, but its determinant should always be nonzero ($\Delta \neq 0$). The determinant of the matrix (6) has a value of $\Delta = -1$, thus the condition solvability of the task is fulfilled.

The obtained system of linear equations from the relation (5) is in the form

$$\begin{aligned} 2 \cdot x_1 + 3 \cdot x_2 + 2 \cdot x_3 &= 3 \cdot x_6 \\ -3 \cdot x_1 - x_2 - 2 \cdot x_3 &= 0 \\ x_1 &= -x_6 \\ x_5 &= -x_4 \end{aligned} \quad (7)$$

By the solution of the system of linear equations we obtain two independent criteria π_1 and π_2 , and minus sign at the relevant unknown quantity x_i in the expression of arguments according to (8) means that the corresponding quantity in the criterion of similarity occurs in the denominator. The plus sign expresses the quantity in the numerator.

	x_1	x_2	x_3	x_4	x_5	x_6	
π_1	-1	1	1	0	0	1	(8)
π_2	0	0	0	1	-1	0	

Complex dimensionless arguments arising from (8) are in the form

$$\pi_1 = \frac{Q_{vz} \cdot Q_u \cdot NO_x}{P_k} \quad (9)$$

$$\pi_2 = \frac{T_{sk}}{T_{vz}} \quad (10)$$

The general dimensionless description of the function expressing the production of nitrogen oxides during combustion of wood may be given in the form

$$\psi(\pi_1, \pi_2) = 0 \quad (11)$$

The dimensionless argument π_1 contains variable NO_x , so this argument may be expressed as a function of an argument π_2

$$\pi_1 = \varphi(\pi_2) \quad (12)$$

The function (12) will be expressed as a system of one-parameter curves. Its shape is determined by calculation of π_2 value from values obtained during measurement (Table 2), and this value is entered as an independent variable. The argument π_1 , thus also the NO_x , is subsequently expressed as the dependently variable function of the π_2 function.

Specifically, the expression of equation (12) may be expected e.g. in the form of a power function

$$\pi_1 = A \cdot \pi_2^B \quad (1) \quad (13)$$

which will be transformed by logarithmic calculation into the equation of a line

$$\log \pi_1 = \log A + B \cdot \log \pi_2 \quad (14)$$

The calculation of the intercept A in relation (14), indicating the distance of the intersection of the regression line on co-ordinate π_1 from the zero point, and the regression coefficient B , indicating the slope

of regression line, may be made by the least squares method, and also directly by

utilization of the Microsoft Excel program.

RESULTS OF THE DEVELOPED MODEL APPLICATION

For the purpose of mathematical model development and its verification the VERNER company has provided the data about the individual physical quantities (Table 2). These are average values obtained from continuous measurements at two operating conditions of the boiler. The

measurements have been carried out twice at the nominal power (about 20 000 W); once at about half of the output power. The measurements have been carried out by an external company (Strojírenský zkušební ústav, s.p. Brno).

Table 2. Measured values of relevant quantities and calculated value of NO_x according to the relation (17) for the V210 boiler

Tablica 2. Izmjerene vrijednosti relevantnih veličina i izračunate vrijednosti NO_x prema izrazu (17) za kotao V210

P_k (W)	Q_{vz} ($m^3 \cdot s^{-1}$)	Q_u ($J \cdot kg^{-1}$)	T_{sk} (K)	T_{vz} (K)	$NO_{x \text{ nam}}$ ($kg \cdot m^{-3}$)	$NO_{x \text{ vyp}}$ ($kg \cdot m^{-3}$)	<i>difference</i> (%)
20050	0.0097	15450000	394.75	296.65	0.00024235	0.00022490	7.20
20010	0.0101	15450000	397.15	296.85	0.00020538	0.00022026	-7.24
10870	0.0057	15450000	365.15	296.85	0.00015814	0.00015890	-0.48

In the Table 3 are shown the calculated values of dimensionless arguments π_1 , π_2 in accordance with relations (9) and (10) and their logarithms are determined, what is necessary for the analytical procedure of calculating the regression coefficient and intercept.

Based on the measured quantities, it is possible to express the actual course of the function $\log \pi_1 = \varphi(\log \pi_2)$ as well as the course of dependency of dimensionless arguments themselves directly in the logarithmic coordinates (Fig. 2).

From the dependence expressed in logarithmic coordinates, the intercept A and the regression coefficient B follow directly. Their values are $A = 0.00063236$, $B = 3.1490$.

Such defined constants in the developed model are valid only for combustion of dry beech wood with the calorific value $15.45 \text{ MJ} \cdot \text{kg}^{-1}$. In the case of combustion of wood with different calorific value, the different values of individual quantities acting in the model would be obtained during measurement.

Also other values of dimensionless arguments π_1, π_2 would be obtained and production of nitrogen oxides would be described by the relationship (18), in which the change of combusted fuel and production of nitrogen oxides would be reflected by the new values of intercept constant A and the regression coefficient B .

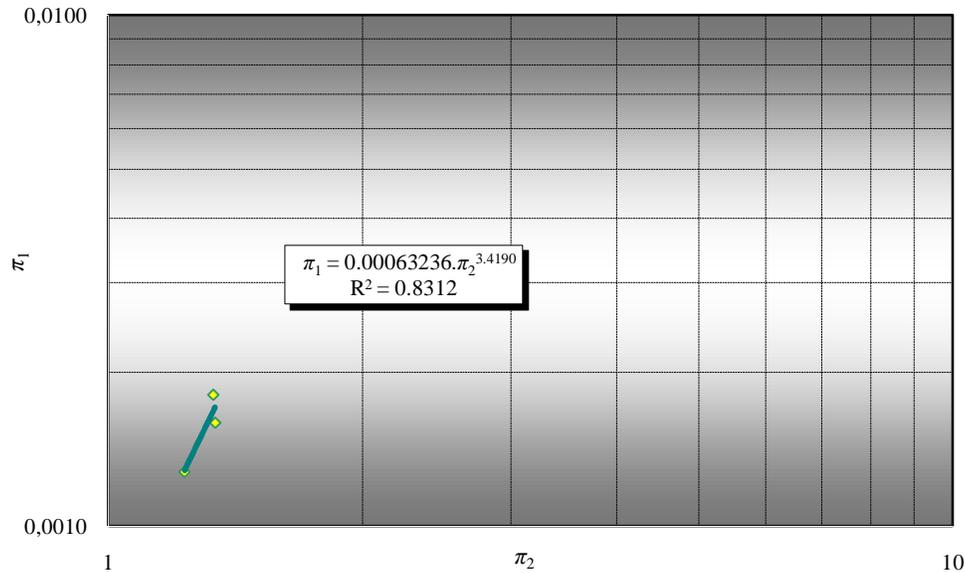


Figure 2. Intercept constant A and the regression coefficient B

Slika 2. Konstanta presjeka A i koeficijent regresije B

Table 3. Values of dimensionless arguments for linear regression

Tablica 3. Vrijednosti bezdimenzijskih argumenata za linearnu regresiju

π_2	π_1	$\log \pi_1$	$\log \pi_2$	$\log \pi_1 \cdot \log \pi_2$	$\log^2 \pi_2$
(1)	(1)	(1)	(1)	(1)	(1)
1.3307E+00	1.8089E-03	-2.7424	0.1241	-0.3403	0.0154
1.3379E+00	1.5952E-03	-2.7972	0.1264	-0.3536	0.0160
1.2301E+00	1.2775E-03	-2.8936	0.0899	-0.2602	0.0081
		-8.4332	0.3404	-0.9541	0.0395
		$\sum y$	$\sum x$	$\sum x \cdot y$	$\sum x^2$

If the experiment for obtaining of the new constants A and B at the combustion of different quality and type of wood will not be carried out, and the original values of constants will be used, a greater variation in nitrogen oxides expressions in terms of the developed model, comparing to the real situation, should be expected. Also such case of model application will be analysed in this article.

The formation of nitrogen oxides during combustion of wood may be described on the basis of relation (13) for the analysed boiler by the model developed using the dimensional analysis, by the dependency of relevant dimensional quantities as follows

$$\frac{Q_{vz} \cdot Q_u \cdot NO_x}{P_k} = A \cdot \left(\frac{T_{sk}}{T_{vz}} \right)^B \quad (15)$$

The functional dependence of NO_x production on the selected quantities expressed from the relation (15) will be expressed as

$$NO_x = A \cdot P_k \cdot T_{sk}^B \cdot Q_{vz}^{-1} \cdot Q_u^{-1} \cdot T_{vz}^{-B} \quad (\text{kg} \cdot \text{m}^{-3}) \quad (16)$$

By the substitution of actual values of the regression coefficient and intercept constants in the expression (16) we obtain

$$NO_x = 63236 \cdot 10^{-8} \cdot \left(\frac{P_k}{Q_{vz} \cdot Q_u} \right) \cdot \left(\frac{T_{sk}}{T_{vz}} \right)^{3.4190} \quad (\text{kg} \cdot \text{m}^{-3}) \quad (17)$$

or

$$NO_x = C \cdot \left(\frac{P_k}{Q_{vz} \cdot Q_u} \right)^m \cdot \left(\frac{T_{sk}}{T_{vz}} \right)^n \quad (\text{kg} \cdot \text{m}^{-3}) \quad (18)$$

VERIFICATION OF THE DEVELOPED MATHEMATICAL MODEL FOR THE VERNER V140 BOILER

The developed model of nitrogen oxides production was verified also for the low power VERNER V140 boiler. Also with this type of boiler the average values of measured quantities necessary for the relation (18) have been obtained for two rated outputs and for about half of boiler's output by the company "Strojírenský zkušební ústav, s. p. Brno".

The verification of the model was carried out in practice by substituting different values for the existing V140 boiler into relation (18), where the values of constants C , m and n were the same as in the case of the V210 boiler. The measured and calculated values for nitrogen oxides for the boiler with lower output power are in the Table 4.

where the individual constants are represented by following values:

$$C = 63236 \cdot 10^{-8}, \quad m = 1.0, \quad n = 3.4190.$$

The criterion equation for production of nitrogen oxides may be expressed in the simplest terms as follows

$$NO_x = C \cdot K^m \cdot P^n \quad (\text{kg} \cdot \text{m}^{-3}) \quad (19)$$

where individual constants are represented by the values:

$$C = 63236 \cdot 10^{-8}, \quad K = P_k / Q_{vz} \cdot Q_u, \\ P = T_{sk} / T_{vz}, \quad m = 1.0, \quad n = 3.4190.$$

The relationship (18) is a mathematical model of NO_x production during combustion of the wood in low power boilers of the same or similar design as the design of the VERNER boilers.

The difference between measured and calculated values in accordance with the mentioned relation for the VERNER V210 boiler (Table 4) may be explained by the fact that during the selection of relevant quantities certainly not all effects, on which the production of nitrogen oxides during combustion of wood depends, were taken into account.

However the priority in the development of the model has been focused on the quantities easily measurable, therefore it is reasonable to expect a greater deviation between the measured quantities of nitrogen oxides and the calculated values according to relation (18).

Table 4. Measured values of relevant Calculated Quantities and value of NO_x according to the relation (18) for V140 boiler

Tablica 4. Izmjerene vrijednosti relevantnih izračunatih veličina i vrijednosti NO_x prema izrazu (18) za kotao V140

P_k	Q_{vz}	Q_u	T_{sk}	T_{vz}	$NO_{x\ nam}$	$NO_{x\ vyp}$	odchylka
(W)	($m^3 \cdot s^{-1}$)	($J \cdot kg^{-1}$)	(K)	(K)	($kg \cdot m^{-3}$)	($kg \cdot m^{-3}$)	(%)
13210	0.0065	14520000	384.45	295.55	0.00021154	0.00021833	-3.21
13530	0.0067	14520000	386.55	297.25	0.00020743	0.00021577	-4.02
6930	0.0038	14520000	376.25	298.15	0.00019306	0.00017802	7.79

DISCUSSION

The mathematical model developed with utilization of the dimensional analysis proved the possibility of utilization of this method for determining of the nitrogen oxides produced volume during the combustion of wood in the equipment of low power. The Tables 2 and 4 show that the difference between the determination of nitrogen oxides production by direct measurements on the V210 boiler and

employing of a mathematical model, ranges from -7.24 % to 7.20 %, and for the V140 boiler from -4.02 % to 7.79 %.

The difference between measured and calculated values may be explained also by the fact that during the selection of relevant quantities certainly not all effects, on which the production of NO_x during combustion of wood depends, were taken into account.

CONCLUSION

At the development of the mathematical model with utilization of the dimensional analysis the precise knowledge of the physical nature of the researched phenomenon is essential and it necessary to take into account all relevant quantities on which the phenomenon depends. Among the relevant quantities in combustion of wood, except for the temperature of exhaust gasses at the end of the boiler, also e.g. the temperature of flame should be included.

The continuous measurement of the flame temperature in the combustion zone is rather difficult in the field operation;

therefore the inclusion of this relevant quantity in the development of a mathematical model has been omitted. It was assumed that this temperature is related to a final temperature of exhaust gases.

Omitting of the flame temperature among relevant quantities represents a certain level of error in description of the nitrogen oxides production and this deficiency substantially contributes to the difference between the nitrogen oxides production calculated in accordance with the model developed - relationship (18) and direct measurement.

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