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Computational Study on Mössbauer Isomer Shifts of Some Organic-neptunium (IV) Complexes

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– This paper is dedicated to dr. Svetozar Musić on the occasion of his $70^{ ext{th}}$ birthday –

Abstract: Relativistic DFT calculations are applied to some organo-neptunium (IV) complexes, $Cp_3Np^{IV}X$ ($Cp = \eta^{5}-C_5H_5$; $X = BH_4$, Cl, OtBu, Ph, *n*Bu), in order to understand their bonding properties between Np and the ligands. We employ scalar-relativistic ZORA Hamiltonian with all-electron basis set (SARC). The calculated electron densities at Np nucleus position in the complexes at B2PLYP / SARC theory strongly correlate to the experimental Mössbauer isomer shifts of ²³⁷Np system. The result of bond overlap population analysis indicates that the bonding strength decreases in order of X = BH₄, Cl, OtBu, Ph and *n*Bu. The tendency depends on the degree of the covalent interaction between Np 5*f*-electron and X ligand. It is suggested that it is important to estimate the bonding contribution of 5*f*-orbital to understand the electronic state for organo-actinide complexes.

Keywords: actinide chemistry, Mössbauer isomer shifts, relativistic DFT approach, bond overlap population.

INTRODUCTION

A CTINIDE chemistry includes some fundamental and applicative interests. For example, the organoactinide complexes, such as $[Cp_2Th^{IV}X_2]$ ($Cp = \eta^{5}-C_5H_5$; X = alkyl, *etc.*), have been investigated as a candidate for the catalyst for the hydroelementation to unsaturated carboncarbon bond.^[1,2] Moreover, the chemical separation of minor-actinides, including Am and Cm, from lanthanides is an important and challenging quest, leading to the disposal of high-level radioactive waste.^[3,4] In both fundamental and applicative cases, it is one of the most interesting tasks to understand how 5*f*-electron behaves toward the bonding state in actinide compounds.

Density functional theory (DFT) has been employed as a useful tool to describe the electronic states for actinide compounds.^[5–7] Kaltsoyannis *et al.* performed the relativistic DFT calculation for An^{III}Cp₃ and An^{IV}Cp₄ (An = Th–Cm) to discuss the bonding properties of An ions by means of various population analyses.^[8,9] We have reported that allelectron relativistic DFT results strongly correlate to the experimental ²³⁷Np Mössbauer isomer shifts, which are quantitative parameters relative to Np ions.^[10] We have also suggested that the bonding types of *f*-electron to a metal-ligand bond, which include bonding, non-bonding and anti-bonding, correlate to their stability.^[11]

We aim to investigate the bonding state in actinide complexes to give a new insight to the bonding behavior of 5*f*-electron. The present study focuses on the bonding properties of some tris-(cyclopentadienyl) neptunium (IV) complexes, $Cp_3Np^{IV}X$. DFT study on their electronic and bonding states had never been reported, although their experimental values of ²³⁷Np Mössbauer isomer shifts are available.^[12] Here we discuss the contribution of 5*f*-electron to the bonding interaction in these complexes by relating the calculated electron density and molecular orbital (MO) population to the ²³⁷Np Mössbauer experiments. We believe that this study contributes to understanding the bonding property in 5*f*-block chemistry.

COMPUTATIONAL DETAILS

Mössbauer isomer shift (δ), which is a quantitative indicator of the bonding strength of a Mössbauer element,



has a linear correlation with the electron density at a Mössbauer nucleus position (ρ_0) :^[13]

$$\delta = a \left(\rho_0 - b \right) \tag{1}$$

where a and b are fitting parameters. ρ_0 can be obtained by a quantum chemical calculation at all-electron level, because core electrons, such as $1s_{1/2}$ and $2p_{1/2}$ electrons, need to be included to get the electron density at the nucleus. The estimation of a linear correlation between the experimental δ and the calculated ρ_0 enables us to evaluate the performance of a computational method. Model compounds for this study are listed in Table 1 with the experimental Mössbauer isomer shifts reported by Karraker and Stone.^[12,14] We referred the experimental X-ray structures of the corresponding complexes^[15–18] and subsequently optimized all the geometries of Cp₃Np^{IV}X complexes. Normal vibrational frequencies were calculated for the equilibrium structures obtained by geometry optimization. Complexes with X = Cl and *n*Bu were created by changing a center metal to Np atom. Complex with X = OtBu was constructed by substituting a tBu group for a Ph group. We considered $X = BH_4$ complex as that BH_4^- ligand works as a tridentate hydrogen donor, as indicated in the infrared spectroscopic study for Cp₃U^{IV}(BH₄) complex reported by Marks and Kolb.^[19] Complex with X = Ph was assumed as that Ph⁻ ligand coordinates to Np^{IV} ion as a η^{1-} carbon donor, although the single crystal structures of their analogues have never been characterized.

All DFT calculations were performed by using ORCA ver. 3.0.0 program.^[20] Zeroth-order relativistic approximation (ZORA)^[21] was employed for all-electron Kohn-Sham Hamiltonian at scalar-relativistic level, which was constructed with model potential approximation.^[22] Although ZORA method tends to underestimate the core electron densities compared to two-component Dirac method,^[21] this underestimation might be systematic and hardly affect the comparison among Np complexes. Spinorbit coupling was neglected. Segmented all-electron relativistically contracted (SARC) basis sets optimized for ZORA Hamiltonian were assigned to Np element^[23] and the other atoms.^[24] Geometry optimizations and standard vibrational modes calculations were carried out at ZORA-BP86 level of theory with SV-ZORA plus one polarization function. ZORA-BP86 with SV-ZORA reproduced the experimental geometries for Eu and Np complexes.^[10] Single-point calculations were performed at ZORA-B2PLYP level of theory with TZV-ZORA plus one polarization function. ZORA-B2PLYP with TZV-ZORA reproduced the experimental Mössbauer isomer shifts for ¹⁵¹Eu and ²³⁷Np.^[10] The accuracy of self-consistent-field (SCF) calculation was achieved under the same condition with our previous work.^[10,11] We set the ground state of Np complexes to spin quartet and obtained their electronic states by unrestricted Kohn-Sham equation. The resolution of the identity (RI) approximation, Split-RI-J^[25] or RIJCOSX,^[26] was employed into all SCF calculations for pure-DFT or hybrid-DFT procedure, respectively. The molecular geometries and the topologies of molecular spinor orbitals were visualized three-dimensionally by using VESTA ver. 3.3.0 program.^[27] Density of states (DOS) and overlap population analyses were carried out in order to evaluate the bonding nature between Np ion and ligands by Mulliken's procedure.[28]

RESULTS AND DISCUSSION

Equilibrium Structures of Cp₃Np^{IV}X

All equilibrium structures by geometrical optimization were obtained in local minima, where all normal vibrational modes have positive frequencies. As shown in Figure 1, their structures have three η^5 -Cp ligands, which are arranged with the approximately $C_{3\nu}$ symmetry. Table 2 shows that the calculated Np–C(Cp) lengths are 2.76–2.78 Å for all systems. It was indicated that the coordination environments consisting of Np and three Cp ligands are almost the same for all Cp₃NpX geometries. For X = Cl, OtBu

Model compounds	$\delta_{ m Np}{}^{ m exp}$ / mms $^{-1}{}^{ m (a)}$	Reference compounds ^(b)
Cp ₃ Np ^{IV} (BH ₄)	14.5 ± 4 ^(c) [Ref. 12]	Cp₃U ^{IV} (HBBN) ^(e) [Ref. 15]
Cp₃Np ^{IV} Cl	14 ± 10 [Ref. 14]	Cp₃U ^{IV} CI [Ref. 16]
Cp₃Np ^{IV} (O <i>t</i> Bu)	8.6 ± 3 [Ref. 12]	Cp₃Np ^{IV} (OPh) [Ref. 17]
Cp₃Np¹∨(Ph)	4.2 ± 2.8 ^(d) [Ref. 12]	Cp₃U ^{IV} (<i>n</i> Bu) [Ref. 18]
Cp₃Np ^{ıv} (<i>n</i> Bu)	2.7 ± 0.7 [Ref. 12]	Cp₃U ^{IV} (<i>n</i> Bu) [Ref. 18]

Table 1. Model compounds for calculation with experimental ²³⁷Np Mössbauer isomer shifts (δ_{Np}^{exp}) and reference compounds.

(a) Relative values to NpAl₂ at 4.2 K with experimental errors.
 (b) Single crystal X-ray structures employed in creating the starting coordinates of model compounds.

(c) Experimental value of (MeCp)₃Np^{IV}(BH₄) complex.

(d) Experimental value of $(MeCP)_{3}Np^{V}(C_{6}H_{4}C_{2}H_{5})$ complex.

(e) HBBN means 9-borabicyclo(3.3.1)nonane hydride.

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Figure 1. Three-dimensional descriptions of optimized Cp₃NpX complexes, $X = BH_4$ (a), X = CI (b), X = OtBu (c), X = Ph (d), and X = nBu (e), without hydrogens of Cp rings for clarity. Black, blue, red, brown, green and light pink spheres show Np, Cl, O, C, B and H elements, respectively.

and *n*Bu complexes, it was found that the calculated values of Np–C(Cp) and Np–X lengths are consistent with the experimental values. The obtained structure of X = BH₄ has three bridging hydrogens (H_{bridge}) and one terminal hydrogen (H_{terminal}) of BH₄⁻ ligand, as shown in Figure 1a. Table 3a shows the selected IR frequencies obtained by the normal vibrational mode calculation without any scaling factors. The calculated IR frequencies of C–H (Cp) wagging and B–H stretching vibrations. The calculation for X = Ph complex shows that Ph⁻ ligand has σ -type coordination property (Figure 1d). The calculated IR frequencies for X = Ph complex are shown in Table 3b. It was confirmed by the vector analysis of normal vibration modes that the vibrational frequencies of 1200–1300 and 1400–1600 cm⁻¹ are assigned to the vibrations attributed to Ph⁻ ligand, being consistent with the corresponding experimental frequencies^[29] (Table 3b). Because stretching vibration frequency of aromatic C=C bond is in this region, Ph⁻ ligand in complex remains to have an aromaticity. These results support the above assumption that Ph⁻ ligand has a η^1 -coordination mode.

Correlation Between ρ_0^{calc} and δ_{Np}^{exp}

We performed the calculation of ρ_0 at Np nucleus position for the optimized Cp₃NpX structures at ZORA-B2PLYP /

Table 2. Calculated bond lengths between metal and ligands for Cp₃NpX complexes and the comparison with some experimental values

Dond longths / Å	$X = BH_4$	X = Cl		X = OtBu		X = Ph	X = <i>n</i> Bu	
Bond lengths / A	Calc.	Calc.	Exp. [Ref. 16]	Calc.	Exp. [Ref. 17]	Calc.	Calc.	Exp. [Ref. 18]
M–C(Cp) _{ave}	2.776(12)	2.757(10)	2.741(38)	2.777(16)	2.733(16)	2.765(12)	2.765(9)	2.739(39)
M–X	2.316(10)	2.595	2.556	2.085	2.137	2.489	2.435	2.426



Table 3. Comparison in IR frequencies (cm^{-1}) between calculation and experiment for complexes with X = BH₄ (a) and X = Ph (b)

(a) $X = BH_4$

	Cp₃Np(BH₄)	Cp ₃ U(BH ₄)	Assignment
_	Calc. ^(a)	Exp. [Ref.19]	Assignment
_	800, 828	797, 825	C–H(Cp) in-plane wagging
	1014	1020	C–H(Cp) out-of-plane wagging
	2226, 2251	2160, 2220, 2295	B–H _{bridge} (BH ₄) stretching
	2551	2480	B–H _{terminal} (BH ₄) stretching

(b) X = Ph

Cp₃Np(Ph)	$Cp_3U(C_6F_5)$	Assignment
Calc. ^(a)	Exp.[Ref.29]	Assignment
770	739	C–H(Cp) in-plane wagging
1008	945	C–H(Cp) out-of-plane wagging
1178, 1272	1248, 1315	C—H(Ph) or C—F(C₀F₅) in-plane wagging
1400, 1443, 1574	1415, 1540, 1628	C–C(Ph) stretching

 (a) Calculated frequencies at ZORA-BP86 / SARC theory without any scaling factors.

TZVP(SARC) level of theory. Figure 2 shows the correlation between experimental δ_{Np} and calculated ρ_0 values. It was found that calculated ρ_0 values strongly correlate to experimental δ_{Np} values with negative linear relationship, in which correlation coefficient (*R*) is -0.968. ²³⁷Np isomer shifts can be calculated by using the fitting parameters *a* and *b* in Equation (1), which are obtained by the linear regression analysis between ρ_0^{calc} and δ_{Np}^{exp} . The calculated δ_{Np} values reproduced the experimental δ_{Np} values within their experimental errors (Table 4). The negative correlation between ρ_0^{calc} and δ_{Np}^{exp} is consistent with the experimental fact that $\Delta R/R$ value, where *R* is Mössbauer nucleus radii and ΔR is defined as ΔR (= $R^{excited} - R^{ground}$) of ²³⁷Np Mössbauer transition is negative,^[30] since $\Delta R/R$ is correlated to *a* with the following equation:^[13]

$$(\Delta R/R) = a \left(5\varepsilon_0 E_{\nu}\right) / \left(3Ze^2 cR^2\right)$$
⁽²⁾

where ε_0 , e and c are dielectric constant, elementary charge and the speed of light, respectively. Z and E_{γ} mean the atomic number and the γ -ray transition energy of Mössbauer nucleus, respectively. We also calculated $\Delta R/R$ value by using Equation (2), in which an approximate value of R as 1.2 $A^{1/3}$ fm (A: the mass number of Mössbauer nucleus) is introduced, resulting in -2.44×10^{-4} . This value correlates to the experimental value ($\Delta < r^2 > / < r^2 > = -3.5 \times$ 10^{-4}),³⁰ since $\Delta < r^2 > / < r^2 >$ value is approximately double of

Table 4. Calculated ρ_0 and δ_{Np} values, which were obtained by fitting parameters a, b (Eq. 1), at ZORA-B2PLYP / SARC theory with experimental δ_{Np} values

Х	$\delta_{ m Np}{}^{ m exp}$ / mms $^{-1}$	$ ho_0^{ m calc}$ / a.u. ⁻³	$\delta_{ m Np}{}^{ m calc}$ / mms $^{-1}$	
BH4	14.5(40)	13180638.890	14.63	
Cl	14(10)	13180644.139	12.20	
O <i>t</i> Bu	8.6(30)	13180647.573	10.61	
Ph	4.2(28)	13180662.004	3.94	
<i>n</i> Bu	2.7(7)	13180664.857	2.62	
Correla	ation efficient (R)	-0.968		
a /	′ a.u. ³ mms ^{–1}	-0.462		
<i>b</i> / a.u. ⁻³		13180670.529		
MA	AD ^(a) / mms ⁻¹	0.86		

^(a) Mean absolute deviation value obtained as the standard deviation between δ_{Np}^{exp} and δ_{Np}^{calc} values.

 $\Delta R/R$ value. However, it should be noted that this calculation includes some limitations as pointed out by Filatov and coworkers.^[31] This is because Equation (2) derived by non-relativistic treatment is employed and the finite nucleus effect is not considered for ρ_0 values obtained by the present ZORA-DFT calculation.

Population Analyses for Cp₃NpX Complexes

The negative linear correlation between ρ_0 and δ_{Np} values means that the core electrons, mainly including 1s and 2s electrons, are more shielded by the valence electrons with the increase in δ_{Np} , leading to smaller ρ_0 . We have already reported that the valence *f*-electron density relates to the



Figure 2. Plot of calculated ρ_0 (ρ_0^{calc}) versus experimental δ_{Np} (δ_{Np}^{exp}) for Cp₃NpX complexes at ZORA-B2PLYP / SARC theory.



tendency in δ_{Np} values.^[10] Although the correlation with *s*-orbital population and the tendency in the Np-ligand lengths are interesting points, any correlation and tendency were not observed. In this section, we focus on the relationship between *f*-orbital population and δ_{Np} values. The result of the visualization of the molecular orbitals, where the valence *f*-electron of Np atom distributes, shows the observation of the bond overlapping between 5*f*-orbital of Np and ligands. Figure 3 exhibits the topological description of the selected MOs for complexes with X = BH₄ and *n*Bu. Complex with X = BH₄ has the large overlapping between Np *f*-orbital and BH₄⁻⁻ ligand (Figure 3a). On the other hand, complex with X = BH₄ and the smaller overlapping compared to complex with X = BH₄ and

(a) $X = BH_4$ complex:



Figure 3. Isosurface density of selected MOs of complexes with $X = BH_4$ (a) and X = nBu (b) at 0.00005 e/bohr³.

also has anti-bonding overlap character, as seen in 106α , 107α and 108α MOs (Figure 3b). It was also found that complex with X = Cl has the same bonding nature to that with X = BH₄, while complexes with X = OtBu and Ph have the same character to that with X = *n*Bu. It might be indicated that the bonding strength between *f*-orbital of Np atom and ligands for complexes with X = BH₄ and Cl is stronger than those of the other complexes.

In order to understand this difference from the viewpoint of *f*-orbital bonding, we performed the bond overlap population (BOP) analysis between Np and X-donor atoms in valence MOs. BOP analysis enables us to evaluate the bonding type and strength of the focusing bond overlap. The value of BOP was estimated by the following equation:²⁸

$$n_i^{kl} = 2S^{kl}c_i^{k}c_i^{l} = 2\Sigma_{\mu}\Sigma_{\nu}S_{\mu\nu}^{kl}c_i^{k\mu}c_i^{l\nu}$$
(3)

where n_i^{kl} is overlap population between φ^k and φ^l atomic orbitals in *i*-th MO. S^{kl} and c_i show the overlap integral between φ^k and φ^l atomic orbitals and the MO coefficient of each AO in *i*-th MO, respectively. Since atomic orbitals are described as linear combination of basis function, n_i^{kl} is evaluated by the sum of products $S_{\mu\nu}{}^{kl}$, which is the overlap integral between $\chi_{\mu}{}^{k}$ and $\chi_{\nu}{}^{\prime}$ basis functions belonging to φ^k and φ^l , respectively, $c_i^{k\mu}$ and $c_i^{l\nu}$, which are the MO coefficients of each basis function in *i*-th MO. Figure 4 shows the partial density of states (PDOS) of Np 5f-electron and the BOP as the solid line and the broken line, respectively, for Cp₃NpX complexes. There exits about 90 % of the valence three 5f electrons in the orbital energy region from -12 to -10 eV for all complexes (Figure 4). Focused on the contribution of BOP in this region, complexes with X = BH₄ and Cl have more positive BOP contribution, that is, larger bonding contribution compared to the others. Comparing complexes among X = OtBu, Ph and nBu, complex with X = nBu has the largest anti-bonding contribution among them. The integral value of BOP in this region decreases in order of $X = BH_4$ (0.262), Cl (0.199), OtBu (0.134), Ph (0.039) and nBu (0.031), correlating to the tendency in the decrease of δ_{ND} value. This result implies that the larger covalent interaction of the Np-X bond leads to the larger δ_{Np} value, resulting in the smaller ρ_0 and vice versa. This tendency can be understood by considering the shielding effect of f-electron. For example, in the case of strong bonding interaction such as $X = BH_4$ or Cl, the increase of the electron density of *f*-orbital by the strong donation of X ligand leads to the large shielding to core electrons, resulting in the small ρ_0 . Through the above discussion, we indicate that the bonding strength between *f*-electron of Np and X atom correlates to the experimental ²³⁷Np Mössbauer isomer shifts for Cp₃NpX complexes.





Figure 4. Partial density of states (PDOS) curve of Np 5*f*-electron (solid line) and bond overlap population (BOP) curve between Np and donor atoms of X ligand (broken line) in α -spinor valence region. Both curves were normalized by same values and obtained by Gaussian-type line with the half-width value of 0.1 eV.

CONCLUSION

We discussed the electronic and bonding states of Cp₃NpX (X = BH₄, Cl, OtBu, Ph, nBu) complexes by means of allelectron relativistic DFT calculation. The validity of the optimized geometries of these compounds was confirmed by comparing them with the previously published X-ray structures. The electron densities at Np nucleus position (ρ_0) calculated by ZORA-B2PLYP / SARC theory strongly correlated to the experimental ²³⁷Np Mössbauer isomer shifts (δ_{Np}). The calculated $\Delta R/R$ value obtained by the linear regression analysis between the calculated ρ_0 and the experimental $\delta_{\rm Np}$ values reproduced the negative sign of the experimental value. Finally, the result of the bond overlap population between Np atom and X ligand might suggest that the covalency of Cp₃NpX complexes depends on the contribution of 5f-electron to Np-X bond. The fundamental discussion, such as the bonding nature, for actinide compounds leads to the rigorous understanding of their stability and reactivity. Moreover, the participation or nonparticipation of *f*-electron to the covalent interaction was discussed.^[11] We believe that this study gives a new insight for the basic and applied actinide chemistries.

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