

MATHEMATICAL MODEL OF PHASE COMPOSITION DIAGRAM OF $\text{CaO} - \text{SiO}_2 - \text{Fe}_2\text{O}_3 - \text{B}_2\text{O}_3$ SYSTEM

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There is developed a method of the mathematical description of a phase composition diagram of n-component systems in the (n - 1) - dimensional space. There is built a phase composition diagram of the $\text{CaO} - \text{SiO}_2 - \text{Fe}_2\text{O}_3 - \text{B}_2\text{O}_3$ system and developed its mathematical model. It permits to determine its phase composition according to the chemical composition of the initial material. There is also solved the reverse problem: determination of the appearance and quantity of components of the initial furnace charge for obtaining a product of the required phase composition. An example of the use of models to estimate the phase composition of iron ore pellets.

Key words: Phase composition, diagram $\text{CaO} - \text{SiO}_2 - \text{Fe}_2\text{O}_3 - \text{B}_2\text{O}_3$ mathematical models, metallurgy, pellet

INTRODUCTION

The $\text{CaO} - \text{SiO}_2 - \text{Fe}_2\text{O}_3$ system is an important component of multicomponent systems, and for a number of productions has also an independent value. It is included, for example, into the six - component $\text{CaO} - \text{SiO}_2 - \text{Al}_2\text{O}_3 - \text{MgO} - \text{FeO} - \text{Fe}_2\text{O}_3$ system which describes the processes of production of cement clinker, ceramics, refractory materials, smelting of cast iron, steel, ferroalloys and other production. As independent it describes, for example, the processes of production of pellets by the annealing method from ferriferous quartzite. For this reason this system is a subject of continuous studies.

The $\text{CaO} - \text{SiO}_2 - \text{Fe}_2\text{O}_3$ system state diagram was repeatedly studied, specified and in the graphic view, according to Osborn and Muena, provided in the work by Berezhnoy [1]. There is also proposed the phase composition diagram of this system in the form of elementary triangles of the coexisting phases.

In this work there was defined the purpose of studying the regularities of phase forming when entering boric anhydride (B_2O_3) in the $\text{CaO} - \text{SiO}_2 - \text{Fe}_2\text{O}_3$ system.

It has a strong effect of lowering viscosity, refractoriness, surface tension of the silicate systems, to construct the phase composition diagram and to develop its mathematical model.

METHODS OF STUDYING

The method which is based on the thermodynamic assessment of the possibility of the secondary compounds coexistence, as well as the principles of topolo-

gy of diagrams [1, 2] is applied for the development of the phase composition diagram.

In the graphic representation the $\text{CaO} - \text{SiO}_2 - \text{Fe}_2\text{O}_3 - \text{B}_2\text{O}_3$ system represents a tetra-hedron made of private systems (Table 1).

Table 1 **List and number of private systems**

Number of		Systems
compo- nents	systems	
1	4	$\text{CaO}; \text{SiO}_2; \text{Fe}_2\text{O}_3; \text{B}_2\text{O}_3$
2	6	$\text{CaO} - \text{SiO}_2; \text{CaO} - \text{Fe}_2\text{O}_3; \text{CaO} - \text{B}_2\text{O}_3;$ $\text{SiO}_2 - \text{Fe}_2\text{O}_3; \text{SiO}_2 - \text{B}_2\text{O}_3; \text{Fe}_2\text{O}_3 - \text{B}_2\text{O}_3;$
3	4	$\text{CaO} - \text{SiO}_2 - \text{Fe}_2\text{O}_3; \text{CaO} - \text{SiO}_2 - \text{B}_2\text{O}_3;$ $\text{CaO} - \text{Fe}_2\text{O}_3 - \text{B}_2\text{O}_3; \text{SiO}_2 - \text{Fe}_2\text{O}_3 - \text{B}_2\text{O}_3$
4	1	$\text{CaO} - \text{SiO}_2 - \text{Fe}_2\text{O}_3 - \text{B}_2\text{O}_3$.

The data of the carried out studies were planned to be used first of all for high-temperature processes. Therefore for the development of a diagram from the reference media there were selected stable (congruently melting) compounds. They were applied on the triangle of compositions. By triangulation in each three-component system there was determined the number of elementary triangles of the coexisting phases that gave the phase composition diagram. Based on the triangulation of ternary systems it was built diagram of the phase composition of the quaternary system $\text{CaO} - \text{SiO}_2 - \text{Fe}_2\text{O}_3 - \text{B}_2\text{O}_3$. (For brevity phase designated as $\text{CaO} - \text{C}$, $\text{SiO}_2 - \text{S}$, $2\text{CaO} \cdot \text{SiO}_2 - \text{C}_2\text{S}$ etc).

RESULTS OF THE STUDIES AND THEIR DISCUSSION

$\text{CaO} - \text{SiO}_2 - \text{Fe}_2\text{O}_3$ system.

It is made of three binary systems: $\text{C} - \text{S}$, $\text{C} - \text{F}$ and $\text{S} - \text{F}$ [1]. In the first one there are formed four calcium

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silicates: C₃S, C₂S, CS and C₃S₂, the first and last of which melt with decomposition and therefore they are not accepted for the development of the diagram. In the second one (C - F) there are three ferrites of calcium: two-calcic C₂F one - calcic CF and semi - calcic CF₂. C₂F is stable. In the third binary system (S - F) there are no chemical compounds [1]. Triple compounds are absent in the system. Triangulation of C - S - F system executed with the use of methods [1, 2] finds in it 4 triangles of the coexisting phases (Figure 1): 1, C - C₂S - C₂F, 2, C₂S - C₂F - F, 3, C₂S - F - CS, 4, F - CS - S

CaO - SiO₂ - B₂O₃ system.

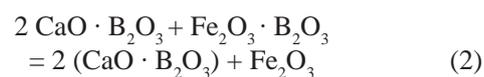
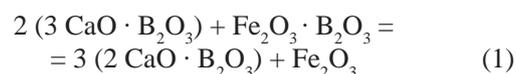
This system was considered in work [3]. From the list of presented there phases there are excluded C₂B₃ and CBS₂, which are formed only by the method of hydrothermal synthesis. By data [4] in this system there are two triple compounds: C₅BS and C₁₁BS₄. But they melt with decomposition and therefore they cannot be used for the development of the diagram.

The compounds which are available in the binary C - S system were listed above, in the S - B system chemical compounds are absent, and in the C - B system there was established the existence of four calcium borates: C₃B, C₂B, CB and CB₂, from which diborate (CB₂) melts with decomposition [5]. So, for the development of the diagram there were selected 5 binary phases (C₂S, CS, C₃B, C₂B, CB). Triangulation gives the diagram (Figure 1) in which we allocate 6 elementary triangles of the coexisting phases: 1, C - C₃B - C₂S, 2, C₃B - C₂B - C₂S, 3, C₂S - C₂B - CS, 4, C₂B - CB - CS, 5, CB - CS - S, 6, CB - S - B.

CaO - Fe₂O₃ - B₂O₃ system.

In literature there are no phase composition diagrams of the CaO - Fe₂O₃ - B₂O₃ system. Therefore triangulation is carried out by the data of its binary systems. C - F and C - B systems were considered above. In the B₂O₃ - Fe₂O₃ system according to data [6] there are two chemical compounds: FB и FB₃. In the quadrangle of the C₂B - C₃B - C₂F - F (Figure 1) substances there was written the reaction $2 C_2B + C_2F = 2 C_3B + F$. Calculation using complex software HSC Chemistry 5.1 (Finland) shows that it $DG_{298,15 K} = -71,4$, and $DG_{738 K} = -2,07$ kJ/mole, giving the possibility to claim the coexistence of the reaction products (C₃B and F) in a broad range of temperatures, in which connection on the diagram they were connected with a straight line. The existence of this line geometrically reveals the only option of coexistence of two-calcic ferrite (C₂F) with three-calcic borate (C₃B).

In the known literature there were not found thermodynamic data for Fe₂O₃ · 3 B₂O₃ and Fe₂O₃ · B₂O₃, therefore for the further triangulation there were attracted other principles. The preference of interaction of the strong base (CaO) with the strong acid oxide (B₂O₃) rather than the same base with feeble acid oxide (Fe₂O₃), permitted to consider the following reactions proceeding in the forward direction:



Based on this, the products of the given reactions (C₂B and F, as well as CB and F) on the triple diagram of the studied C - F - B system were connected by straight lines as the coexisting phases. As for the phase Fe₂O₃ · 3 B₂O₃, after the executed triangulation for it there is the only thing the option of coexistence with CaO · B₂O₃. It should be noted that the executed splitting does not contradict the rule of coexistence of congruent compounds with congruent and isomorphic [1, 7]. Thus, in this system triangulation reveals 7 elementary triangles of coexisting phases: 1, C - C₃B - C₂F; 2, C₃B - C₂F - F; 3, C₃B - F - C₂B; 4, C₂B - F - CB; 5, CB - F - FB; 6, CB - FB - FB₃; 7, CB - FB₃ - B (Figure 1).

SiO₂ - Fe₂O₃ - B₂O₃ system.

The phase composition diagram of the S - F - B system is also constructed for the first time. In binary SiO₂ - Fe₂O₃ and SiO₂ - B₂O₃ systems chemical compounds are absent [1, 5], and in Fe₂O₃ - B₂O₃ system there are two already mentioned compounds FB and FB₃. Therefore it is broken into three elementary triangles of the coexisting phases 1, S - F - FB, 2, S - FB - FB₃ и 3, S - FB₃ - B (Figure 1).

CaO - SiO₂ - Fe₂O₃ - B₂O₃ system.

The existence of the phase composition diagrams of private three - component systems permitted to make splitting into elementary tetrahedrons the four-component CaO - SiO₂ - Fe₂O₃ - B₂O₃ system. In addition to the used above ones there was also used the method of "closing" triangles on the tetrahedron by comparison of their compositions [1, 7], which allowed to beat the CaO - SiO₂ - Fe₂O₃ - B₂O₃ system 9 elementary tetrahedrons of coexisting phases: 1, CB - B - FB₃-S, 2, CB - FB₃ - S - FB, 3, CB - S - FB - F, 4, CB - S - F - CS, 5, CB - CS - F - C₂B, 6, C₂B - CS - F - C₂S, 7, C₂S - C₂B - C₃B - F, 8, C₃B - C₂S - F - C₂F, 9, C₃B - C₂S - C₂F - C. In Figure there is shown the obtained tetrahedron and its scanning by the edges which can be used for determination of the phase composition.

But searching for the phase composition by geometrical creations in the tetrahedron is complicated, and in five -, six - and more component systems is impossible. The single way is the development of a mathematical model. In this paper, we proposed a method used mathematical description of phase diagrams of the composition, based on the balance of the distribution of the initial phases of the oxides in the image [8]. The mathematical model is created for each (seven) elementary tetrahedron. For example, to obtain such a tetrahedron №1 equation: $CB=2,2523 \cdot C_0$, $B = 1,2523 \cdot C_0 - 1,3127 \cdot F_0 + 1 \cdot B_0$, $FB_3 = 2,3127 \cdot F_0$, $S = 1 \cdot S_0$, wherein through

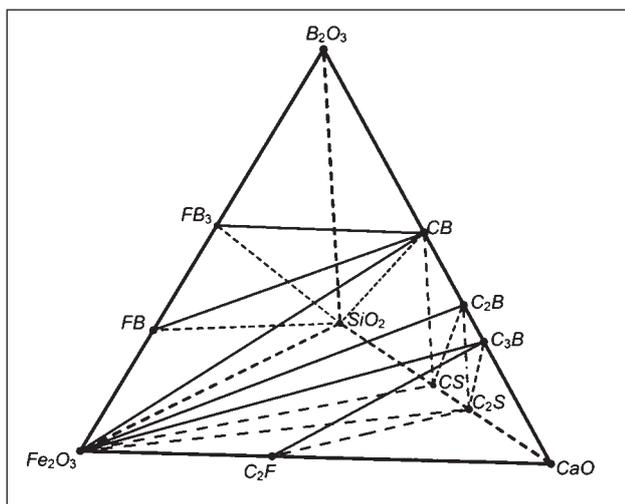


Figure 1 Phase composition diagrams of the CaO - SiO₂ - Fe₂O₃ - B₂O₃

C₀, F₀, B₀ and S₀ designated contents of CaO, Fe₂O₃, B₂O₃ and SiO₂ in the feed in weight percent based on chemical analysis.

In metallurgy importance attached to the formation of an optimal phase composition of agglomerated iron ore (sinter, pellet), giving it a high strength [9,10]. The above model was used as an example for these purposes. In Table 2 there is provided the chemical and phase composition of the sheaf (dead rock) of pellets from ferrous quartzite of the Northern Mining and Processing works (Ukraine) [11]. It is described by the private CaO - SiO₂ - Fe₂O₃ system considered above. The low - base ((CaO / SiO₂ = 0,3) and produced at the factory (CaO / SiO₂ = 0,65) pellets are placed in elementary triangle 4, F - CS - S. With growing the degree of fluxing (CaO additives) as a part of the sheaf, there increases the quantity of wollastonite (from 50 to 78 %) which recrystallizing in the reducing conditions of the blast furnace is the reason of the low durability of these pellets [11].

When increasing basicity to 1,2 and 1,5 the sheaf moves to the calcic corner of the diagram and gets to the field of elementary triangle C₂S - F - CS. Here alongside with wollastonite (CS) there is two - calcic silicate (C₂S) which though reduces crystallinity of the sheaf but is dangerous because of the possibility of inversion with changing the volume [12] that can lead to destruction of pellets. The additive of boric anhydride sharply reduces the field of crystallization of two-calcic silicate

Table 2 Calculated phase composition of the mixed pellets made of ferrous quartzite concentrates

CaO / SiO ₂	Chemical and phase composition / %									
	CaO	SiO ₂	Fe ₂ O ₃	B ₂ O ₃	C ₂ S	CS	F	S	C ₂ B	CB
0,3	24,2	52,8	23,0			50,1	23,0	26,9		
0,5	28,2	50,2	21,6			58,4	21,6	20,0		
1,0	37,5	42,5	20,0			77,6	20,0	2,4		
1,2	42,2	42,8	15,0		6,9	78,1	15,0			
1,5	46,5	39,5	14,0		29,6	56,4	14,0			
1,2	42,0	42,6	14,9	0,5	4,4	79,4	14,9			
1,2	41,8	42,4	14,9	1,0	1,8	80,7	14,9		1,3	
1,2	41,4	41,9	14,7	2,0		81,3	14,7		2,6	
									2,0	2,0

(C₂S) and already at 2% of B₂O₃ the sheaf leaves this dangerous field moving to tetrahedron 5, CB - CS - F - C₂B (Table 2).

It is the consequence of thermodynamic preference of borate formation rather than calcium silicates. All described is a cardinal measure of disposal from 2 CaO · SiO₂. But if it is necessary for technological reasons in the pellets to maintain a high ratio CaO · SiO₂ and at the same time to prevent its destruction, you can do more economical measures. The matter is that in the presence of B₂O₃ the replacement of (SiO₄)⁴⁻ anion, two-calcic silicate by (BO₄)⁵⁻ anion, boric anhydride with formation of a solid solution stabilizes the high-temperature (not breaking up) forms 2CaO·SiO₂, and for this purpose there is sufficient only 0,25 - 0,50 % of B₂O₃[13].

The positive effect of B₂O₃ on the properties of iron-ore pellets shows us the laboratory and industrial trials [14].

It should be also noted that when processing these materials in the blast furnace, B₂O₃ contained in them will partially pass into slag reducing its refractoriness and viscosity, and partially will be reduced into cast iron and in to pass subsequently into steel and rolled metal, considerably improving their properties at concentrations making from 0,001 to 0,003 % [15].

CONCLUSION

There is built a diagram of the phase composition of the CaO - SiO₂ - Fe₂O₃ - B₂O₃ system and developed its mathematical model. It permits to determine its phase composition by the chemical composition of the material. Using the model it is also possible to define the type and quantity of components of the initial furnace charge for obtaining the product of the required phase composition. It is shown that the addition to the system CaO - SiO₂ - Fe₂O₃ boric anhydride reduces field dicalcium silicate crystallization and stabilizes the collapse of materials containing it. An example of the positive impact of B₂O₃ on the properties of iron - ore pellets.

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- Note:** The responsible translator for English language is Nataliya. Drag, Karaganda, Kazakhstan