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Acetylene, Vinylidene, and the Vinyl Cation in Ground and Excited States*

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Ab initio calculations using the improved virtual orbital formalism are reported for acetylene, vinylidene, and the vinyl cation, $C_2H_3^+$, in classical and bridged geometries. Electronic transition energies and equilibrium geometries for ground and lower lying electronically excited states have been calculated. A modified Walsh diagram for acetylene and simple molecular orbital considerations explain excited state structures and energy orderings. While acetylene in the ground state is much more stable than vinylidene, the energies of several corresponding excited states are comparable. The stabilities of bridged and classical structures of the vinyl cation are very similar in the ground state, but in the various excited states either structure can predominate. The proton affinity of acetylene in the ground state should be appreciably lower than in excited states.

INTRODUCTION

First invoked in the electrophilic reactions of alkynes, vinyl cations are now common reactive intermediates.¹ Since the proton affinity of acetylene is about 10 kcal/mol less than that of ethylene, the parent vinyl cation, $C_2H_3^+$, is extremely reactive and can only be observed experimentally in the gas phase.² However, many details of the ground state have been revealed by a number of theoretical investigations.³⁻⁹

In relation to the photochemistry of alkynes we have now studied new aspects; the protonation of acetylene in the lowestlying excited singlet and

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triplet states. We also reconsider the problem of the excited states of acetylene itself.

Only a few carbocations with triplet ground states have been reported. These include $C_5H_5^+$ and its relatives,¹⁰ C_2H^+ ,^{9,11} and lithiated carbenium ions like CLi_3^+ .¹² Prior studies of triplet and singlet excited states of carbocations also are rare. The triplet methyl cation (³A"), for example, is calculated to lie about 88 kcal/mol above the singlet ground state in energy and to have a non-planar geometry with C_s symmetry.¹² Excited states of the vinyl cation are also likely to exhibit interesting features.

In this respect, knowledge of the ground and excited states of the corresponding deprotonated species, acetylene (HC \equiv CH) and its isomer, vinylidene (H₂C=C), is desirable. Both C₂H₃⁺ and C₂H₂ are isoelectronic, but the vinyl cation possesses and additional C—H bond. The excited states of acetylene are the subject of an extensive literature, both experimental and theoretical.^{18-21*} Non-linear forms are favored, and *cis*- and *trans*-isomers have been calculated. While linear excited states have been considered to connect these two forms, we will show in the present work that other transition structures are lower in energy. With the exception of the triplet, excited states of vinylidene have not been investigated extensively before.²²

A further point deals with energetic ordering of the molecular orbitals and the related sequence of the various excited states.²¹ Heretofore, this sequence could not be clarified by means of simple MO theory. We will show that a modified Walsh diagram as well as an additional correction for the nearly degenerate MO's allows a complete understanding of the sequence of both singlet and triplet states.

CALCULATIONAL METHODS

The ab initio SCF calculations employed at the Gaussian lobe 4-31G basis set¹⁴ augmented by diffuse (s, p) functions (exponent 0.05) at the carbon atoms. These were included so that Rydberg states could be taken into account. The exponent chosen is similar in magnitude to that of the 4-31+G basis set, designed for calculations on carbanions, which also have occupied orbitals with diffuse character.¹⁵ The ground and lowest electronically excited singlet and triplet state geometries were calculated for both *trans*- and *cis*-conformations of planar C₂H₂. In order to examine excited states, truncated CI treatments were carried out

In order to examine excited states, truncated CI treatments were carried out within the molecular orbital framework. These were designed to provide balanced approaches to the ground and excited states as far as is possible within Koopman's approximation.¹⁶ The singly excited configurations used have common occupied MO's from which excitations, carried out conveniently within the formalism of improved virtual orbitals, are performed.¹⁷ Vertical as well as non-vertical electronic transitions are expected to be given more accurately by this procedure than by some alternative treatments which tend to favour the ground state.¹⁸

RESULTS AND DISCUSSION

Acetylene Ground and Excited States

In the most detailed earlier study, So, Wetmore, and Schaefer²¹ found different energetic orderings of the excited singlet $({}^{1}A_{u} < {}^{1}A_{2} < {}^{1}B_{2} < {}^{1}B_{u})$ and triplet $({}^{3}B_{2} < {}^{3}B_{u} < {}^{3}A_{u} < {}^{3}A_{2})$ states of acetylene, but could provide no qualitative rationalization in terms of Walsh diagram arguments.

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^{*} See also O. Nomura and S. Iwata, J. Chem. Phys. 74 (1981) 6830 (added in proof)

Doubly occup and vacant S	ied (valence) SCF orbitals		Improved virtu is sir	al orbitals	when $\pi_u(x)$ ed
ground state	SEBT		singlet	n sig Tim —	triplet
	, h _u	5		\mathcal{D}_{2}	e e e e e e e e e e e e e e e e e e e
$-0.76684 \sigma_{u}$					
$-0.68747 \sigma_{g}$					
$-0.41590 \pi_u$					
0.08887 $\sigma_u R$		— 0 .	17103 $\pi_g(y)$	As OF state	$-0.22303 \ \pi_{g}(x)$
0.09402 $\sigma_g R$		0.0	$08962 \sigma_g R$	-	$-0.19302 \pi_{g}(y)$
$0.12398 \pi R$		0.	08027 σ R		$-0.10205 \sigma R$

TABLE	I	
	_	

Orbital Energies (a. u.) of Acetylene in its Ground State Geometry

R: Rydberg orbitals

To provide a better overview into the nature of the problem, we first consider vertical excitations of acetylene. Table 1 gives the orbital energies for the acetylene ground state. Next, the vacant orbitals were calculated again under the conditions that $\pi_u(x)$ was singly occupied. By removing appropriate terms from the Fock operator, the energies of the improved virtual orbitals corresponding to singlet and triplet states were obtained. These not only differ from one another in their ordering, but also from the original ordering of the unoccupied MO's in acetylene. This original ordering may thus be inappropriate not only for drawing Walsh diagrams but also for estimating excitation energies. The improved virtual orbitals should be used instead for both these purposes.

 $-0.05565 \pi_{\sigma}(x) R$

For example, vertical electronic transition energies can easily be evaluated as differences between doubly occupied and improved virtual orbitals. The Rydberg states, easily indentified by orbitals with large coefficients for the diffuse basis functions are of further interest. Table 1 shows that the Rydberg character of an orbital sometimes depends on whether this orbital is empty or singly occupied. Besides vertical transitions the nonvertical electronic transitions are of specific importance in photochemistry. The orbital analysis of the vertical transitions can provide a very useful qualitative description of equilibrium geometries in excited states and facilitates quantitative investigations.

The original Walsh diagram¹⁹ for *cis* $(C_{2\nu})$ and trans (C_{2h}) HAAH systems provided a convincing rationalization for the strongly non-linear preferences of the lowest excited singlet and triplet states of acetylene.^{19–21} In Table 2, the correlation diagram connecting these forms is extended to include a half-bent (C_s) intermediate structure.

 $-0.09129 \sigma_{\mu} R$

TABLE II

Correlation Scheme for Orbital Symmetries of HAAH Molecules in cis (C_{2v}) , Linear $(D_{\infty b})$, Half Bent (C_s) and trans (C_{2h}) Arrangements

$C_{2\nu}$ cis	$D_{\infty h}^{a}$	$C_s^{\ b}$	C_{2h} trans
<i>a</i> ₁	σ_{g}	a'	a,
b_2	σ_{u}	a'	b_u
a_1	π_{u}	a'	b_u
b_1	π_{u}	<i>a</i> ″	a_u
a2	π_{g}	a″	b_g
b_2	π_g	a'	a_g

^a Linear transition state ($D_{\infty h}$); ^b Half bent-half linear transition state (C_s).





However, the original Walsh diagram¹⁹ has features which are not confirmed by exact calculations (shown in Figure 1). Thus, *cis* and *trans* geometrical distortions do not always lead to similar raisings and lowerings. Other connections also are indicated: In the original diagram for *cis* and *trans* conformations, the orbitals $4a_1 - 3b_u$ and $1b_1 - 1a_u$ are connected. In Figure 1 alternative pairings are suggested: $4a_1 - 1a_u$ and $1b_1 - 3b_u$. This reflects the ordering in Table 3 better, and leads to the correct prediction that the singlet ${}^{1}A_{u}$ (trans) state is favored over ${}^{1}A_{2}$ (cis). The same applies to the triplet A states. Likewise, the ${}^{3}B_{2}$ (cis) state is favored over ${}^{3}B_{u}$ (trans); the singlet B states are ordered similarly.²⁰

TABLE III

Valence Orbital Energies (a. u.) for the Ground and Excited States of Acetylene. The Last two Orbitals of the Excited States are Singly Occupied; Improved Virtual Orbitals are Utilized for the Highest Energy Orbital

¹∑g ⁺	¹ A ₂	¹ A _u	³ B ₂	${}^{3}B_{u}$
$-1.047 \sigma_{g}$	$-1.025 a_1$	$-1.029 \ a_{g}$	$-1.038 a_1$	$-1.036 a_{o}$
0.767 σ_{u}	-0.771 b ₂	$-0.784 b_{,i}$	$-0.763 b_2$	— 0.781 b _n
$-0.687 \sigma_{g}$	$-0.661 a_1$	$-0.623 a_{\sigma}$	$-0.656 a_1$	-0.632 a
$-0.416 \ \pi_{u}$	$-0.389 a_1$	-0.412 b _u	$-0.398 b_1$	- 0.398 a
	$-0.394 b_1$	$-0.392 a_{\mu}$	$-0.390 a_1$	-0.413 b
	$-0.286 b_2$	$-0.326 a_g$	$-0.369 b_2$	$-0.352 \ a_g$

Furthermore the splitting of the two π_u orbitals due to symmetry reduction is so small that the usually applied aufbau principle fails for these closely spaced orbitals. In other words, neither the original¹⁹ nor the new Walsh diagram (Figure 1) allows a reliable qualitative decision to be made concerning the preferred occupancy.

For example, consider various excitations from $1b_1$ or from $4a_1$. The energetic orderings of the resulting singly occupied orbitals are quite different:

$1b_1 \rightarrow 3b_2 - 0.286$	$4a_1 \rightarrow 1a_2 - 0.1988$
$\rightarrow 5a_1 - 0.091$	$\rightarrow 3b_2 - 0.132$
$\rightarrow 4b_2 - 0.072$	$\rightarrow 5a_1 - 0.087$
$\rightarrow 1a_2 - 0.061$	$\rightarrow 4b_2 - 0.070$

The lowest excited singlet state with the cis conformation $({}^{1}A_{2})$ and the lowest excited triplet state with the *trans* conformation $({}^{3}B_{u})$ both are derived from excitations $(1b_{1} \rightarrow 3b_{2} \text{ and } 3b_{u} \rightarrow 4a_{g}$, respectively) which do not originate from the highest occupied orbital (see Figure 1). The valence orbital energies are represented in Table 3 for the ground state as well as for the lowest singlet and triplet states in their calculated local minima.

Thus we have arrived at the following situation: While the Walsh diagram is able to predict the preference for *cis* or *trans* conformations of a given state, it is incapable of ordering the different states among each other. The Walsh diagram predictions are:

 ${}^{1}A_{u} < {}^{1}A_{2}$ ${}^{1}B_{2} < {}^{1}B_{u}$ ${}^{3}A_{u} < {}^{3}A_{2}$ ${}^{3}B_{2} < {}^{3}B_{u}$

However, even though the *cis-trans* energy differences are much smaller than those between different states, e. g., between A_2 and B_2 , these cannot be ordered readily.

The energetic sequence of the ${}^{1}A_{2}$ and ${}^{1}B_{2}$ as well as the ${}^{3}A_{2}$ and ${}^{3}B_{2}$ states can easily be predicted on the basis of the present results. The A_{2} and B_{2} states involve excitations, $4a_{1} \rightarrow 1a_{2}$ and $4a_{1} \rightarrow 3b_{2}$, respectively. Because of the close energetic relationships shown in Figure 1, the former is essentially a $\pi_u(x) \to \pi_g(y)$ excitation, while the latter involves $\pi_u(x) \to \pi_g(x)$. Singlet and triplet excitation energies to the same configuration are given by

$$\Delta E \begin{pmatrix} S \\ T \end{pmatrix} = \varepsilon_k - \varepsilon_i - J_{ik} + \begin{pmatrix} 2 K_{ik} \\ O \end{pmatrix}.$$

When wellknown relationships are employed,

 $J_{xx} = K_{xx}$ and $J_{xx} = J_{xy} + 2 K_{xy}$

one obtains as an approximation for ΔE :

$$S \qquad \begin{array}{c|c} \pi_{u}\left(x\right) \rightarrow \pi_{g}\left(x\right) & \pi_{u}\left(x\right) \rightarrow \pi_{g}\left(y\right) \\ + J_{xx} & -J_{xy} + 2K_{xy} \\ - J_{xx} & -J_{xy} \end{array}$$

(The difference $\varepsilon_k - \varepsilon_i$ is neglected due to the essentially degenerate character of the $1a_2$ and $3b_2$ orbitals.)

Because $J_{xx} > J_{xy}$, it follows that ${}^{3}B_{2} < {}^{3}A_{2}$; since $J_{xx} > -J_{xy} + 2 K_{xy}$, ${}^{1}A_{2} < {}^{1}B_{2}$. This gives the following sequences:

$${}^{1}A_{u} < {}^{1}A_{2} \ll {}^{1}B_{2} < {}^{1}B_{u}$$
$${}^{3}B_{2} < {}^{3}B_{u} \ll {}^{3}A_{u} < {}^{3}A_{2}$$

Thus, such simple considerations answer questions put forward in the literature. 21

TABLE IV

Equilibrium Geometries and Relative Energies for the Ground and the Lowest Excited Singlet and Triplet States of Acetylene. The Linear Excited States are Presented in Order to Show Their Vertical Excitations

Electronic state	r _e (CC) (Å)	r _e (CH) (Å)	Θ_e (CCH) (deg)	E (eV)
${}^{1}\Sigma_{g}^{+}$	1.200 (1.208) ^a	1.060 (1.058) ^a	180.0 (180.0) ^a	0.0 (0.0) ^a
$1\Sigma_{\mu}^{-}$	1.200	1.060	180.0	6.67
¹ A ₂	1.332	1.070^{b}	137.5	5.22
${}^{1}A_{u}$	1.356 (1.388)ª	1.070 ^b	128.0 (120) ^a	4.82 (5.23) ^a
$^{3}\Sigma_{u}^{+}$	1.200	1.060	180.0	5.25 (5.2)°
³ B ₂	1.317	1.070^{b}	130.5	3.21 (2.6—4.7) ^d
³ B _u	1.320	1.070 ^b	131.0	3.43

^a Reference 28; ^b The same CH distance is used for excited states; ^c Reference 29; ^d Reference 30

The relative energies as well as geometry parameters of ground and excited states are listed in Table 4. As far as comparisons with experimental assignments are possible, the calculated results are in reasonable agreement.

Earlier calculations of Rydberg states of acetylene have assumed initial geometries (vertical transitions), but have shown that carefully extended diffuse basis sets are needed.¹⁸ In the present investigation the two lowest singlet and triplet Rydberg states were studied and the equilibrium CC distances determined. All these states are found to correspond to linear geometries; the structural parameters and energetic orderings are given in Table 5. Since these Rydberg states are above the dissociation limit, the calculated geometries may correspond to local minima.

TABLE V

Equilibrium Data and Relative Energies for the Lowest Rydberg States of Acetylene

Electronic state	- 1 ²	r _e (CC) (Å)	E (eV)	
¹∏"		1.242	8.79	8.21°
		$(1.26)^{a}$	$(8.16)^{\rm b}$	
¹∏ _g		1.261	8.98	8.73°
³∏ _u		1.242	8.46	8.10°
³∏ _σ		1.293	8.60	8.61°
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^a Reference 31; ^b Reference 28; ^c Reference 18

In Figure 2 the energies of the lowest excited singlet and triplet states are shown with respect to their calculated bond angles for *cis* and *trans* conformations. Do these local minima correspond to static or to dynamic structures? The energy barriers shown by solid lines in Figure 2 are so high that a static structure must be assumed for both ${}^{1}A_{u}$ and ${}^{3}B_{2}$. This is so despite the fact that the energy barrier in Figure 2 corresponds to the linear structure whereas the lowest transition state corresponds to a half bent — half linear structure which reduces the barrier by approximately a factor of two. Thus, it is likely that the singlet excited state will only be observable in the *trans* conformation as *cis* to *trans* conversion will occur very rapidly. The situation with the triplet ist not as clear.

Vinylidene and its Excited States

Vinylidene (H₂C=C), a higher energy isomer of acetylene, has often been considered before in its singlet (${}^{1}A_{1}$) ground state.²²⁻²⁶ While the vinylidene--acetylene energy difference is not very sensitive to the level of ab initio theory employed, the calculated 1,2-H shift barrier connecting these two singlet isomers depends greatly on the size of the basis set and the extent of electron correlation corrections.^{22,26} It is likely that singlet vinylidene is not a local minimum, and rearranges to acetylene without activation.^{22,27}

The triplet ${}^{3}B_{2}$ state of vinylidene, although estimated to be about 42 kcal/mol higher in energy than the ${}^{1}A_{1}$ singlet,²² is the form which is experimentally observable because the 1,2-H shift barrier is quite high.²⁷ Other

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excited state configurations have been considered by Davis, Goddard, and Harding.²³ However, these authors only examined vertical transitions, and did not revaluate the geometries of the higher excited states. Vertical excitation energies for vinylidene also were calculated by Dykstra and Schaefer.²⁴



Figure 2. Energy for ground and lowest excited singlet and triplet states as a function of angle bending from linearity. Linear transition state $(D_{co}h)$: full lines; bent transition state (C_s) : dashed lines. The geometries of Table IV are used.

TABLE VI

Equilibrium Geometries and Energies of Vinylidene and Acetylene in Ground and Excited States

Vinylidene			Acetylene				
State	r _e (CC) (Å)	$\Theta_e ({ m HCH})^{ m a}$ (deg)	E (kcal/mol)	State	r _e (CC) (Å)	$\Theta_e (\mathrm{HCC})^\mathrm{a}$ (deg)	E (kcal/mol)
$^{1}A_{1}(C_{2v})$	1.298	118.8	35.9 ^b	${}^{1}\Sigma_{g}^{+}(D_{\infty h})$	1.203	180	0.0 ^b
$^{1}A_{1}(C_{2\nu})$	1.291	118.6	39.3°	${}^{1}\Sigma_{g}^{*+}(D_{\infty h})$	1.203	180	0.0°
${}^{1}A_{2}(C_{2\nu})$	1.402	114.0	110.8	${}^{1}A_{u}(C_{2h})$	1.353	127.4	110.4
${}^{1}B_{2}(C_{2\nu})$	1.328	120.0	136.3	${}^{1}B_{2}(C_{2v})$	1.335	134.2	120.4
${}^{8}A_{2}(C_{2y})$	1.406	114.2	95.1	${}^{3}A_{\mu}(C_{2h})$	1.352	126.0	92.8
${}^{3}B_{2}(C_{2\nu})$	1.304	116.0	73.3	${}^{3}B_{2}(C_{2v})$	1.325	130.5	73.6

^a The CH bond lengths were fixed at 1.06 Å;
 ^b SCF approach, total energy -76.71702 a.u.;
 ^c with electron corrections, total energy -77.18422 a.u.

Our calculations on vinylidene ground and excited states are compared with those for acetylene in Table 6. In agreement with earlier results,²² the energy of the ${}^{1}A_{1}$ (H₂C=C) state is 36—39 kcal/mol higher than that of the acetylene ground state (${}^{1}\Sigma_{g}^{+}$) at both HF and correlated levels. However, the energy differences between corresponding excited states are much smaller. Indeed, both the lowest triplet (${}^{3}B_{2}$) and the lowest singlet (${}^{1}A_{2}$) excited states of vinylidene are calculated to have nearly the same energy as the lowest triplet (${}^{3}B_{2}$) and lowest singlet (${}^{1}A_{u}$) excited states of acetylene, respectively. The ${}^{3}A_{2}$ state of vinylidene is only a little above the second triplet state (${}^{3}A_{u}$) of acetylene.

All vinylidene states have $C_{2\nu}$ symmetry, and there is little variation in the HCH bond angles. Due to the partial occupancy of a π^* -type orbital (b_1) , the ${}^{1}A_2$ and ${}^{3}A_2$ states have elongated C—C bonds (1.40 Å vs about 1.30 Å in all the other states). The C—C bond lengths in the excited states of acetylene are longer than in the ground state for similar reasons.

 $C_{2}H_{3}^{+}$

Since the first explorations of protonation of acetylene and ethylene by quantum chemical procedures,³ many investigations have been concerned with the crucial question of reactive stabilities of classical and non-classical (bridged) structures.⁴⁻⁹ At high theoretical levels, the bridged form of the vinyl cation is more stable, but only by a few kcal/mol. If there is an energy barrier between these structures, it must be quite small, approximately 1 kcal/mol.⁷ Hence, protonated acetylene is a fluxional system in the ground state. The three protons move rapidly around the CC fragment, but all atoms remain in a plane (Figure 3). The equilibrium structures (Figure 4) with the basis set employed here which included additional d-type polarization functions at the carbon atoms, are presented in Table 7. In electronically excited states



Figure 3. Schematic representation of the dynamic structure of $C_2H_3^+$ in the ground state; all atoms are in the same plane.





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the »classical« and bridged structures are expected to exhibit much larger energy differences. As is well precedented, our SCF results with the augmented 4-31G basis set favor the classical structure (Figure 4). The calculation of both classical and bridged structures in the given geometries were also carried out with the larger 6-311G** triply split valence basis set (which includes p-type functions on hydrogen) with electron correlation corrections using our standard procedure. The two forms are practically isoenergetic, in general agreement with the literature.

TABLE VII

Equilibrium Geometries and Relative Energies for the Ground State of $C_2H_3^+$ in Classical and Bridged Conformations (cf. Figure 4)

Structure	r _e (CC) (Å)	r _e (CH ₂) (Å)	r _e (CH ₁) (Å)	$\Theta_e (\text{CCH}_2)$ (deg)	E (kcal/mol)
classical	 1.272	1.082	1.070	120.0	0.0
bridged	1.211	1.070	1.296	177.8	10.6^{a}

 $^{\rm a}$ This value was reduced by an improved basis set (6—311G**) and with electron correlation corrections to 2.5 kcal/mol.

TABLE VIII

Orbital Energies (a. u.) for the Classical and the Bridged Structures of $C_2H_{3^+}$ (cf. Figure 4) Using the Geometries from Table 7

Doubly and vac	occupied (valence) cant SCF orbitals	Improved virtual orbitals when b ₁ is singly occupied singlet triplet	
classical	$\begin{array}{cccc} -1.37401 & a_1 \\ -1.09338 & a_1 \\ -0.95759 & a_1 \\ -0.90534 & b_2 \\ -0.72953 & b_1 \end{array}$		e Serverence - A
	$\begin{array}{c}0.23902 \ b_2 \\0.13275 \ b_1 R \\0.08561 \ a_1 R \end{array}$	$\begin{array}{cccc}0.62711 & b_2 & -\\0.32750 & b_1 R & -\\0.30257 & a_1 R & -\end{array}$	$\begin{array}{c} -0.66084 \ b_2 \\ -0.55372 \ b_1 \\ -0.32920 \ a_1 R \end{array}$
bridged	$\begin{array}{ccc}1.43954 & a_1 \\1.07559 & b_2 \\0.99993 & a_1 \\0.87374 & a_1 \\0.75159 & b_1 \end{array}$		
	$\begin{array}{c}0.13995 \ b_2 \ R \\0.12017 \ a_2 \\0.10992 \ a_1 \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} -0.54655 & a_2 \\ -0.53131 & b_2 \ R \\ -0.41684 & a_1 \end{array}$

R: Rydberg orbitals

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In Table 8 doubly occupied, vacant, and singly occupied molecular orbitals are represented for the vinyl cations in their ground state geometries. The procedure used is the same as that of Table 1. For the classical structure the vacant orbitals as well as improved virtual singlet and triplet orbitals show a common ordering. For the bridged structure, all three sets of orbitals have different orderings. The vertical excitation energies for both structures are listed in Table 9. For the ${}^{1}A_{2}$ state the transition energies are in qualitative agreement with recently reported values.⁷

Electronic state	E classical	(eV) bridged
$ \frac{{}^{1}A_{2} (b_{1} \rightarrow b_{2})}{{}^{1}A_{1} (b_{1} \rightarrow b_{1})} $	2.79	6.68
	11.62	9.56 11.71
${}^{3}A_{2} (b_{1} \rightarrow b_{2})$ ${}^{3}A_{1} (b_{1} \rightarrow b_{1})$	1.87 4.78	5.99
$^{3}B_{1} (b_{1} \rightarrow a_{1})$ $^{3}B_{2} (b_{1} \rightarrow a_{2})$	10.89	$9.11 \\ 5.58$

TABLE	IX
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 H_2 H_3 H_3 H_1 H_1 H_1 H_1 H_2 H_3 H_1 H_1 H_1 H_1 H_1 H_2 H_3 H_1 H_2 H_1 H_1 H_2 H_1 H_2 H_2 H_3 H_1 H_2 H_2 H_3 H_1 H_2 H_3 H_3

Vertical Electronic Transition Energies of $C_2H_3^+$

Figure 5. Classical and bridged structures of $C_2H_3^+$ in the lowest excited state.

TABLE X

Equilibrium Geometries and Relative Energies for the Classical and Bridged Structures of $C_2H_3^+$ in the Lowest Excited Singlet States (cf. Figure 5)

State	Structure	r_e (CC)	$r_e (CH_2)$	$r_e (\mathrm{CH_1})$	Θ_e (CCH ₁)	Θ_e (CCH ₂)	E
	003	(Å)	(Å)	(Å)	(deg)	(deg)	(kcal/mol)
¹ A″	classical	1.380	1.079	1.068	147	121.3	0.0
${}^{1}A_{2}$	bridged	1.370	1.082	1.338	59	149.0	77.8
-							

In searching for the equilibrium structures for excited states, symmetry reduction was taken into account. For the lowest singlet excited states of the classical $({}^{1}A'')$ and the bridged $({}^{1}A_{1})$ species, the equilibrium structures

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are shown in Figure 5 and in Table 10. The classical excited state (${}^{1}A''$) has a *bent* structure and is considerably stabilized with respect to the bridged excited state (${}^{1}A_{2}$), in which the acetylene moiety is bent markedly but the overall symmetry ($C_{2\nu}$) is retained. The Walsh diagram (Figure 6) explains why out-of-plane bending is not found. For the lowest triplet state (${}^{3}A''$), geometry parameters are essentially the same as are reported in Table 10 for the ${}^{1}A''$ singlet state. Only the change in the CCH₁ angle (to 139°) is significant. The ordering of electronic states (using the bent ${}^{1}A''$ geometry for all calculations) indicates the energy of the ${}^{3}A''$ triplet state to be only 0.07 eV higher than the singlet ${}^{1}A'$ bent ground state; the ${}^{1}A''$ energy is 1.48 eV higher.



Figure 6. Walsh diagram for bridged $C_2H_3^+$ structures in the lowest excited state. The singly occupied orbitals are shown.

The situation for the second excited singlet states (Table 11) is quite different. The bridged structure (${}^{1}B_{1}$) is more stable. The »classical« structure of the second excited state ${}^{1}A'$ is not planar. This can be rationalized by the orbital correlation diagram in Figure 7; the orbital energies reflect the ordering of total energies of the states quite well.

TABLE XI

Equilibrium Geometries and Relative Energies for the Classical and Bridged Structures of $C_2H_3^+$ in the Second Excited Singlet State (cf. Figure 7)

State	Structure	r _e (CC) (Å)	r _e (CH ₂) (Å)	r _e (CH ₁) (Å)	$\Theta_e ({ m CCH_1})$ (deg)	$\Theta_e ({ m CCH}_2)$ (deg)	E (kcal/mol)
1 <i>A</i> ′	classical	1.380	1.083	1.078	126	120	0.0
¹ B ₁	bridged	1.250	1.065	2.095	73	180	64.6

The calculated proton affinity of C_2H_2 based on the neutral and cation ground states is 164 kcal/mol, in agreement with other calculations.⁴ Proton affinities for excited states can be defined when the symmetry of the wave-functions of the neutral system and the cation can be correlated. However, with ionic-neutral comparisons, symmetry arguments are questionable. Nevertheless, comparison of total energies for excited states listed in Table 12 suggests a marked increase in the proton affinitiy with respect to that of the ground state.



Figure 7. Orbital diagram and state diagram for the lowest excited states of classical $C_2H_3^+$. Excitations come from the lowest orbital. (Energies in a. u.)

The triplet vinyl cation $({}^{3}A'')$ should be an attractive target for experimental study. Its energy is indicated (Table 12) to lie only about 32 kcal/mol (1.39 eV) above that of the vinyl cation ground state, which is known experimentally to have $\Delta H_{fo}^{0} = 266$ kcal/mol. Hence ΔH_{fo}^{0} ($C_{2}H_{3}^{+}$, ${}^{3}A''$) should be about 298 kcal/mol; this corresponds to a relatively low ionization potential of 10.3 eV from the vinyl radical (The IP of $C_{2}H_{4}$ is 10.51 eV). The triplet vinyl cation also has a similar structure to that of the vinyl radical (e.g.; $\langle HCC = 139^{\circ}$ and 135°, respectively), except that the latter has a somewhat shorter C—C bond (1.38 Å vs 1.33 Å) due to the presence of two instead of one π electron.

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	E_{PA} (kcal/mol)	164	218	210	206	158			
ates	E (a. u.)		76.887			76.851			
d and Excited Sti	C ₂ H ₃ + State	$^{1}A_{1}$	<i>"V</i> ₁	1B_1	″Vε	$^{3}A'$			
TABLE XII PA) of C_2H_2 in Ground	Structure	$_{\rm H}^{\rm H}$ > c ⁺ =cH	$_{\rm H}^{\rm H}$ $>$ $_{\rm C^{+}=C}^{\rm H}$	H-C=C-H	H H $C^{+}=C$ H	$_{\rm H}^{\rm H} > {\rm C^{+=C}} \blacktriangleleft {\rm H}$			
Proton Affinities (E	E (a. u.)	-76.717		76.394	76.599	iv taligio La via de caracia de caracia de caracia de caracia de caracia			
	C ₂ H ₂ State	1 8 8	^{1}Au	$^{1}\Pi_{u}$	$^{3}\mathrm{B}_{2}$				
nti - mu dira no - 1.4,165, no - 1.4,165, no - 1.4,165,170	Structure	H—C≡C—H	н С=С	Н—С≡С—Н	υ=c c=c	Н			

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SAŽETAK

Acetilen, viniliden i vinil kation u osnovnom i pobuđenim stanjima

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Prikazani su rezultati ab initio računa za klasične i premoštene geometrije acetilena, vinilidena i vinil kationa, $C_2H_3^+$. Izračunane su energije prijelaza elektrona, te ravnotežne geometrije temeljnih i niže pobuđenih elektronskih stanja. Za objašnjenje struktura pobuđenog stanja acetilena predložen je Walsh-ov dijagram. Dok je acetilen u temeljnom stanju stabilniji od vinilidena, energije nekoliko odgovarajućih pobuđenih stanja su im približne. Stabilnost premoštenih i klasičnih struktura vinil kationa vrlo je slična u temeljnom stanju, ali u različitim pobuđenim stanjima pojedina struktura može prevladavati. Afinitet prema protonu mora biti znatno manji u temeljnom nego u pobuđenim stanjima acetilena.

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