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Finite Element Analysis of Heat Treated Wood Filled Styrene Maleic Anhydride (SMA) Copolymer Composites

Analiza kompozita od kopolimera stirena i anhidrida maleinske kiseline (SMA) punjenih pregrijanim drvom metodom konačnih elemenata

ABSTRACT • The computer aided three dimensional static analyses of the specimens was done by using the Finite Element Method (FEM) and obtained data was compared with actual test data. The aim of this study is to compare the deformation/stress analyses with FEM analysis results of styrene maleic anhydride (SMA) copolymer composites. The heat treated wood/SMA copolymer composites were produced from different loadings (from 10 to 30 wt. %) of heat treated and untreated eastern white pine wood flours (Pinus strobus L.). All formulations of wood flour/SMA copolymer composites were produced by melt compounding through injection molding. The deformation/stress results obtained from the experimental solutions are very close to the results obtained from the numerical solutions (SAP2000 V17). As a result, it can be said that it is beneficial to use the FEM in the engineering design approach after the data obtained by the experimental solutions as meaningful values after application of the FEM.

Key words: wood polymer composite, styrene maleic anhydride (SMA), finite element method
In the recent years, more interest has been reported on wood composites as engineering materials because of renewable, biodegradable resources, no waste problems, and superior mechanical properties (Mackerle, 2005). Wood plastic composite (WPC) has gained the interest of material engineers because of its structural properties (El-Haggar and Kamel, 2011). Some of its main properties are high durability, low maintenance, strength and stiffness, lower prices and decrease in bio-degradation, which makes the composites suitable for outdoor applications. Some of the applications of these composites are: decking, sheathing, roof tiles, window trim and automobile parts. WPCs perform like conventional wood; however, they are not stiff and may require special fasteners or design changes. WPCs are still stiffer than plastics (Clemens and Caulfield, 2005).

A developing class of materials, including WPC has favorable attributes – they are cost effective and have good performance (Bledzki et al., 2002; Aydemir et al., 2014a; Aydemir et al., 2014b; Aydemir et al., 2015a; Aydemir et al., 2015b; Zor et al., 2016; Bardak et al., 2016; Sözen et al., 2017). The industrial manufacturing arena has paid superior attention to the use of wood as reinforcing filler for thermoplastics (Kishi et al., 1988; Maidas et al., 1988; Woodhams et al., 1984; Yam et al., 1990). The injection molding process and thermoforming of interior parts is used along with styrene maleic anhydride (SMA) copolymer in the automotive industry (ARCO Chemical Company, 1990). The main reason for the choice of maleic anhydride is to enhance the properties of the copolymer. The importance of using SMA lies in the fact that it demonstrates a similar behavior to maleic anhydride polypropylene (MAPP) (Takase and Shiraishi, 1989).

In the last four decades, the finite element method (FEM), used in numerous areas of structural analysis, has been used in the engineering application process, as well. Structural analysis should determine the effects of the loads on physical structures and their components. These physical structures and their components, subjected to this type of analysis, have to withstand loads, pressures, torques and moments in accordance with parameters that act on them (Figure 1).

Use of fiber composite material in load bearing applications usually requires a careful study and design of the component or product to be made. This can be achieved using numerical modeling software, such as finite element analysis (FEA) software (Lim et al., 2003). However, the accuracy of the input parameters, such as mechanical and physical properties of the material, loading and constraint conditions, plays an important role in the correct prediction of the structural behavior of the composite obtained by numerical analysis. The finite element method (FEM) is a numerical technique used in the analysis of the behavior of materials or systems (Gustafsson 1995, 1996). The FEM is used for structural analysis and modeling of materials that are subject to static or dynamic loads. Similarly, furniture components and systems are designed with the aid of structural design procedures (Eckelman, 1966).

In spite of the academic and industrial interest in heat treated wood, only few studies of heat treated lignocellulosic filled polymer composites have been pub-

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**Figure 1** Process of FEM

**Slika 1.** Postupak analize metodom konačnih elemenata
lished in the literature (Aydemir et al., 2011; Aydemir et al., 2015c; Zor et al., 2018). To the best of authors’ knowledge, there is no information related to simulation analysis of heat treated lignocellulosic-filled SMA thermoplastic composites. The aim of the study is to compare the deformation analysis with the help of the open and close numerical modeling solution with the FEM.

2 EXPERIMENTAL APPROACH
2. EKSPERIMENTALNI PRISTUP
2.1 Materials
2.1. Materijali

The SMA (XIRAN® SE700) was supplied by Poyscope Polymer, USA. It has a density of 1.08 g/cm³ (Maleic anhydride contents 10 % wt., melt flow 22 g/10min at 240 °C/10.0 kg). The eastern white pine (Pinus strobus L.), used as filler in this study, was kindly supplied by Wicks Lumber in Pittsfield, ME, USA.

2.2 Heat treatment
2.2. Pregrijavanje

Pine wood samples were cut from sapwood of a radial board of eastern white pine (Pinus strobus L.). Cubic samples with dimensions of 360 mm x 20 mm x 20 mm were cut with clear faces, kept in a conditioned room at 20 °C and 50 % relative humidity for 3 weeks and weighed afterwards. The heat treatment was made in an oven heated by electric coils located in the walls and with exhaustion of the heated gases by natural convection through an opening in the oven wall. The treatment was applied at a temperature of 212 °C for 8 h (Aydemir et al. 2015b). The treatment started by putting the samples at ambient temperature in the oven. The time to reach the treatment temperature was about 60 min. After heat treatment, the solid wood board samples were removed from the oven and ground in a grinder. Wood flour of pine greater than 60 mesh was used as raw material to prepare the wood flour/SMA copolymer composites. Untreated samples were used as the control.

2.3 Processing of composite materials
2.3. Proizvodnja kompozita

The wood flour retained on 60-mesh size sieve was dried to a moisture content of less than 1 % using a conventional oven at 105 °C for 16 h. This mixture was compounded in a twin-screw extruder (C. W. Brabender Compounding Machine, ME, USA.) with the following temperature: 210/220/220/220/220/210 °C and with rotation of 60 rpm. The SMA-wood flour compounds were granulated using a lab-scale grinder. The ground particles were dried in an oven at 105 °C for 16 h before being injection molded into ASTM test specimens. All materials were injection molded using a barrel temperature of 230 °C, mold temperature of 220 °C and injection pressure of 17 MPa. The composition of the composites is shown in Table 1.

3 NUMERICAL SOLUTION
3. RAČUNSKI PRISTUP
3.1 Material properties
3.1. Svojstva materijala

Finite element analysis of wood flour filled SMA composite elements was carried out using the SAP2000 V17 program. Analyses were performed by creating numerical design models based on experimental data. It was compared to the normal stresses obtained from the numerical model and the normal stresses obtained from the experiment by using the maximum load, elastic modulus and density data with 3-point bending test. The value of vertical deformation at any point of the bar is obtained by the finite element method. Since the contribution of deformation to numerical solutions is very little, the weight of the material has been neglected. Some mechanical values entered into the program for numerical analysis of the model are given in Table 2.

Table 1 Composition of SMA, untreated and heat treated composites
Tablica 1. Sastav kompozita od SMA, nepregrijanoga i pregrijanog drva

<table>
<thead>
<tr>
<th>SMA, %</th>
<th>Untreated wood, %</th>
<th>Heat treated wood, %</th>
<th>Specimen mark</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Nepregrijano drvo, %</td>
<td>Pregrijano drvo, %</td>
<td>Oznaka uzorka</td>
</tr>
<tr>
<td>100</td>
<td>-</td>
<td>-</td>
<td>Control</td>
</tr>
<tr>
<td>90</td>
<td>10</td>
<td>-</td>
<td>10UT</td>
</tr>
<tr>
<td>80</td>
<td>20</td>
<td>-</td>
<td>20UT</td>
</tr>
<tr>
<td>70</td>
<td>30</td>
<td>-</td>
<td>30UT</td>
</tr>
<tr>
<td>90</td>
<td>-</td>
<td>10</td>
<td>10T</td>
</tr>
<tr>
<td>80</td>
<td>-</td>
<td>20</td>
<td>20T</td>
</tr>
<tr>
<td>70</td>
<td>-</td>
<td>30</td>
<td>30T</td>
</tr>
</tbody>
</table>

Table 2 Mechanical properties of materials entered into the program
Tablica 2. Mehanička svojstva materijala unesena u program

<table>
<thead>
<tr>
<th>Material properties</th>
<th>Control</th>
<th>UT*</th>
<th>T**</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Kontrola</td>
<td>%10</td>
<td>%20</td>
</tr>
<tr>
<td>Density / gustoća, g/cm³</td>
<td>1.05</td>
<td>1.07</td>
<td>1.10</td>
</tr>
<tr>
<td>Elasticity modulus of bending / modul elastičnosti, GPa</td>
<td>1.96</td>
<td>2.52</td>
<td>2.69</td>
</tr>
<tr>
<td>Poisson ratio / Poissonov omjer</td>
<td>0.3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Bending stress / čvrstoća na savijanje</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Max fracture load / najveća sila loma, N</td>
<td>128</td>
<td>120</td>
<td>119</td>
</tr>
<tr>
<td>Sample properties / dimenzije uzorka</td>
<td>127 mm x 22 mm x 3.2 mm</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

* UT – untreated wood / nepregrijano drvo; **T – heat treated wood / pregrijano drvo
3.2 Finite element method (open solution)

The Finite Elements Method (FEM) is a numerical method used in engineering to analyze the behavior of materials or systems against external factors (force, heat, electricity, etc.). FEM contains the numerical solution of the mathematical model established by equalizing stiffness matrix \([K]\), deformation vector \([u]\) and force vector \([F]\) in structural static calculations. The force vector, \([F]\), was determined as (Eq. 1):

\[
\{F\} = [K] \{U\}
\]

(1)

Where \([F]\) is the force vector, \([K]\) is the stiffness matrix, \([u]\) is the deformation vector.

When the force is applied to the material, the extensions of the material are proportional to stretching within the elastic limits. This is called the “Hooke Law”. The modulus of elasticity is a characteristic feature of the material. The modulus of elasticity, \(E\), was determined as (Eq. 2):

\[
E = \frac{\sigma}{\varepsilon}
\]

(2)

Where \(E\) is the modulus of elasticity, \(\sigma\) is the stress, \(\varepsilon\) is the deformation.

In a beam subjected to bending, the normal stress is as given in Eq. 3.

\[
\sigma_{(z)} = \frac{M}{I_s} y_{(z)}
\]

(3)

Where \(\sigma_{(z)}\) is the normal stress along section height, \(M\) is the bending moment at any distance of the bar, \(y_{(z)}\) is the distance of cross-section, \(I_s\) is the moment of inertia.

If the same beam is subjected to a force (tension or compression) only in the \(z\)-axis direction (first local axis of the bar), a constant \(\sigma_0\) strain occurs along the rod and section height as given in Eq. 4.

\[
\sigma_{(z)} = \sigma_0 = \frac{P}{A}
\]

(4)

Where \(\sigma_0\) is the stress, \(A\) is the cross-sectional area.

3.3 Finite element modeling (close solution)

The maximum force obtained by the 3 point bending test was compared with the normal stresses obtained from the normal tensile test obtained from the numerical model using the elastic modulus and density data. In addition, the value of vertical deformation at any point of the bar is obtained by the finite element method. In this study, vertical deformations were given at the midpoint of the bar where the force was applied. Vertical deformation (Eq. 5) at any \(z\) distance of a beam subjected to 3 point bending test is shown in Figure 2. 3D view of finite element model is given in Figure 3.

\[
\delta y = \frac{P \cdot L^3}{48 \cdot E \cdot I}
\]

(5)

Where \(\delta y\) is the vertical deformation, \(P\) is the applied maximum force (N).

The steps that are followed in the program to solve the problem with the FEM are given below.

1. Creating the Model
2. Identification of Material Properties
3. Implementation of border conditions
4. Meshing
5. Analysis and evaluation of results.

3.4 Deformation analysis with finite element modeling

The comparison of the experimental deformation results with the data obtained with the aid of Eq. 5 is given in Table 3. Linear elastic behavior obtained by neglecting the weight of the material was analyzed numerically using the SAP2000 V17 program.

According to the 3 point bending load, the deformation results obtained with Eq. 5 and SAP2000 V17 numerical deformation results are very close to each other.

Table 4 shows the results of the maximum stresses obtained from numerical modeling with the maxi-
In order to determine the accuracy of the experimental data in the 3-point bending load, with data obtained by the numerical model technique that used the SAP2000 V17 software, it was seen that close results were found. These results show that the sample distribution varies in the 30 % composite groups. This is because, as the wood flour ratio increases during the production of the injection molding machine, the material cannot be obtained homogeneously at the desired temperature under high temperature, and the material does not exhibit the behavior of the linear isotropic material.

Table 4
Comparison of numerical solution and experimentally obtained stresses with 3-point bending load

<table>
<thead>
<tr>
<th>Materials</th>
<th>Experimental solution, MPa</th>
<th>Numerical (close) solution, MPa (Eq. 4)</th>
<th>Difference, %</th>
<th>Open solution, MPa</th>
<th>Difference, %</th>
</tr>
</thead>
<tbody>
<tr>
<td>Control</td>
<td>70.21</td>
<td>68.18</td>
<td>2.89</td>
<td>68.18</td>
<td>2.89</td>
</tr>
<tr>
<td>10UT</td>
<td>69.25</td>
<td>63.89</td>
<td>7.74</td>
<td>63.92</td>
<td>7.70</td>
</tr>
<tr>
<td>10T</td>
<td>68.9</td>
<td>62.86</td>
<td>8.76</td>
<td>63.38</td>
<td>8.01</td>
</tr>
<tr>
<td>20UT</td>
<td>63.89</td>
<td>60.39</td>
<td>5.47</td>
<td>63.38</td>
<td>0.8</td>
</tr>
<tr>
<td>20T</td>
<td>70.89</td>
<td>65.52</td>
<td>7.57</td>
<td>63.92</td>
<td>9.83</td>
</tr>
<tr>
<td>30UT</td>
<td>71.5</td>
<td>63.92</td>
<td>10.6</td>
<td>64.45</td>
<td>9.86</td>
</tr>
<tr>
<td>30T</td>
<td>70.97</td>
<td>63.39</td>
<td>10.68</td>
<td>64.45</td>
<td>9.19</td>
</tr>
</tbody>
</table>

The maximum stress and deformation of the 3-point bending result of the pure SMA samples, which are the control samples, are shown as examples in Figures 4 and 5.

4 RESULTS AND DISCUSSION
4. REZULTATI I RASPRAVA

When exposed to 3-point bending, the close solutions of the control group are received as 2D stress value of 68.18 MPa and the deformation value of -11.66 mm. According to the experimental and open solution approaches, the deformation value difference is 0.6 % and the stress value difference is 2.89 %.

When exposed to 3-point bending, the close solutions of 10 % UT group composite are received as 2D stress value of 63.89 MPa and the deformation value of -8.49 mm. According to the experimental and open solution approaches, the deformation value difference is 0.47 % and the stress value difference is 7.74 %. When exposed to 3-point bending, the close solutions of 10 % T group composite are received as 2D stress value of 62.86 MPa and the deformation value of -7.91 mm. According to the experimental and open solution approaches, the deformation value difference is 0.50 % and the stress value difference is 8.76 %.

When exposed to 3-point bending, the close solutions of 20 % UT group composite are received as 2D stress value of 60.39 MPa and the deformation value of
and the stress value difference is 7.57%. According to the experimental and open solution approaches, the deformation value difference is 0.49% and the stress value difference is 10.60%. When exposed to 3-point bending, the close solutions of 30% T group composite are received as 2D stress value of 63.92 MPa and the deformation value of -5.47 mm. According to the experimental and open solution approaches, the deformation value difference is 0.36% and the stress value difference is 10.68%.

5 CONCLUSIONS

This study investigated the design possibilities for engineering materials by linear elastic analysis using SAP2000 V17 software. The deformations obtained by simulation were compared with experimental data. As a result of the numerical solutions carried out by finite element analyses, normal stresses were obtained along the bending beam.

When the normal stress values obtained from numerical solutions using SAP2000 V17 software are compared with the open solution using Eq. 3, it is seen that the results are very close to each other. These values were compared with the experimental results, it was observed that the differences in the values obtained for the composites containing 30% wood flour were increased. For this reason, it can be said that the material starts to lose its homogenous, isotropic and linear behavior. When the numerical analysis and the deformation values obtained by using Eq. 5 are compared, it is seen that the results are very close to each other.

Based on the findings obtained from the present study, it was concluded that SAP2000 V17 simulation software could be used in the calculation of the component displacements, strains, and stresses for composite/engineering materials under internal and external loads. This reduces the need for a large number of prototypes; it requires fewer product development cycles and means lower costs (time/cost), as well as the improvement of the quality of engineering applications.

Due to the use of computer technology in the design and analysis of wood or wood based composite elements, it is possible to provide important information to product designers who can obtain preliminary information about the impacts of the loads to which a product will be exposed at the usage site before the production of a specific material.

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5 REFERENCES


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