Effect of Surface Roughness on Elastohydrodynamic Lubrication Performance of Cylindrical Roller Bearing

Xia YANG, Yachao LI, Guangming LIU, Jianmei WANG

Abstract: In order to study the effect of surface roughness on the Elastohydrodynamic Lubrication (EHL) performance of cylindrical roller bearing, an EHL model of cylindrical roller bearing with three dimensional surface cosine roughness based on finite length line contact theory is established. The EHL performance of cylindrical roller bearing is calculated by the Finite Difference Method (FDM) program, with which the effects of surface cosine roughness amplitude, wavelength and texture angle on EHL performance of cylindrical roller bearing are analyzed. The numerical results show that the roughness amplitude, wavelength and texture angle have great influence on the EHL performance in the contact area. The increase of roughness amplitude and wavelength in a reasonable range is beneficial to the enhancement of EHL performance of the cylindrical roller bearing, and the transverse roughness is more favorable to enhance the bearing capacity and reduce the friction coefficient.

Keywords: cylindrical roller bearing; Elastohydrodynamic Lubrication (EHL); Finite Difference Method (FDM); three dimensional cosine roughness

1 INTRODUCTION

Four-row cylindrical roller bearings, which can bear large radial loads, are widely used in rolling mill. Their precision, life, vibration and reliability play a decisive role in the normal operation of rolling mill and the quality of rolled products. Heavy loads are operated on the four-row cylindrical roller bearings, whose lubricating performances have a great influence on the bearing's life, vibration and other properties. Therefore, it is of great significance to study the elastohydrodynamic lubrication (EHL) theory of four-row cylindrical roller bearings. The EHL of cylindrical roller bearings belongs to the category of finite length roller line contact EHL. For many years, the research on the EHL characteristics of finite roller line contact was one of the hot topics.

In 1949, literature [1] combined Hertz contact theory with Reynolds lubrication theory, and gave the first analytical solution of linear contact EHL. After that, the linear contact elastohydrodynamic theory entered a rapid development period [2-3]. Literature [4] analyzed the elastohydrodynamic of the straight generatrix roller modified by tangent and intersecting circular arc at the end of the roller by inverse solution, and obtained the influence of suction velocity and the modification quantity of the busbar on the oil film pressure and thickness. Literature [5] obtained the elastohydrodynamic numerical solution of isothermal finite length straight busbar roller, revealed the edge effect of roller lubrication, and obtained the conclusion that the minimum film thickness is located at the end of roller.

Since the 21st century, with the rapid development of computer technology, the study of finite length line contact elastohydrodynamic theory has entered a period of rapid development [6]. Literature [7] took into account the thermal effect on the basis of isothermal solution, and obtained the complete numerical solution of thermo-elastohydrodynamic lubrication (THL) with finite length contact. Literature [8] studied the edge effect in finite length contact thermo-elastohydrodynamic lubrication (THL), and compared the lubrication characteristics of different modified rollers. Literature [9] studied the problem of THL with finite length contact at different secondary temperatures and oil supply temperatures. There is no absolutely smooth surface in engineering, and it is necessary to study the effects of surface roughness, because of the same magnitudes of oil film thickness and the metal surface roughness formed by cutting. It is also one of the topics, which the scholars from all over the world are interested in. Literature [10] discussed the influence of surface roughness on soft EHL, and pointed out that the pressure peak produced by roughness would not flatten the rough plane. Literature [11] studied the effect of plastic deformation of surface roughness on linear contact EHL. Literature [12] studied the EHL of isothermal finite length line contact with surface roughness, and analyzed the effects of roller contact length, crown and end chamfer on the oil film thickness and stress concentration. Literature [13] studied the EHL characteristics of isothermal finite length line contact with surface roughness. Literature [14] proposed an analytical method for THL of cylindrical roller bearings with the effect of thermoelastic deformation and roughness. Literature [15] proposed an analytical model to investigate the hydrodynamic lubrication of the short groove, and analyzed the influence of geometrical parameters of the short grooves on the hydrodynamic lubrication. Literature [16] developed a mixed EHL model and studied the effects of the wavelength and amplitude of roughness, working conditions on the roughness orientations. Literature [17] revealed the connection between the film thickness and the friction for a uniform surface texture on transition from full film to mixed lubrication in non-conformal contacts. Literature [18] studied a finite length roller subjected to a time varying load using a full-system finite element approach, and got the behaviour of finite line EHL contacts under transient conditions. Literature [19] proposed a numerical method for analyzing point contact thermal elastohydrodynamic lubrication of angular contact ball bearing based on the point contact thermal elastohydrodynamic lubrication theory.

To sum up, few literatures have systematically analyzed the influence of several factors of roughness on EHL characteristics of the cylindrical roller bearing. In this paper, Newtonian fluid lubrication model will be used to
study the EHL performance of cylindrical roller bearings in line contact. By changing the amplitude, wavelength and texture angle of surface roughness, the influence of roughness on EHL characteristics of cylindrical roller bearings will be analyzed.

2 FINITE LENGTH LINE CONTACT THEORY

2.1 Mathematical Model

Finite length line contact pair is composed of two end modification roller A and roller B, as shown in Fig. 5, where, $R_1$ and $R_2$ represent the radius and the repair radius of the rollers, $L$ and $l$ represent the length and the line segment length of roller [20].

2.2 Basic Equation

(1) Reynolds equation of finite length line contacts is expressed as follows:

$$\frac{\partial}{\partial x} \left( \frac{p h^3 c_p}{\eta} \right) + \frac{\partial}{\partial y} \left( \frac{p h^3 c_p}{\eta} \right) = 12 u_s \frac{\partial (\rho h)}{\partial x},$$

where, $p$ represents the oil film pressure, $h$ represents the film thickness, $\rho$ represents the oil density, $\eta$ represents the oil viscosity, $u_s$ represents the suction velocity.

(2) Boundary conditions equations are expressed as follows:

$$\begin{cases}
p(x_{in}, y) = p(x_{out}, y) = p(x, y_{in}) = p(x, y_{out}) \\
p(x, y) \geq 0 (x_{in} < x < x_{out}, y_{in} < y < y_{out})
\end{cases}$$

where, $x_{in}$ and $x_{out}$ represent the entrance and export coordinate of x direction respectively, $y_{in}$ and $y_{out}$ represent the entrance and export coordinate of y direction.

(3) Film thickness equation is expressed as follows:

$$h(x, y) = h_0 + \frac{\nu^2}{2R} + v(x, y) - s(x, y),$$

where, $h_0$ represents the rigid film thickness, $R = R_1R_2/(R_1+R_2)$ represents the equivalent radius of curvature, when the centers of curvature of two contact surfaces are located on different sides of the contact point, take the symbol of ‘−’; else take the symbol of ‘+’, $v$ represents the elastic deformation, $s$ represents the roughness.

(4) Elastic deformation equation is expressed as follows:

$$v(x, y) = \frac{2}{\pi E} \int \int \frac{\rho(\xi, \zeta)}{\sqrt{(x-x)\zeta + (y-y)\xi}} d\xi d\zeta$$

where, $E' = \frac{1}{2} \left( \frac{1}{E_1} + \frac{1}{E_2} \right)$ represents the composite elasticity modulus, $E_1$ and $E_2$ represent the elasticity moduluses of the two contact bodies respectively, $\mu_1$ and $\mu_2$ represent the Poisson ratios of the two contact bodies respectively.

(5) Roughness equation is expressed as follows:

$$s(x, y) = Ra \cdot \cos \left( \frac{2\pi \cos \beta}{l} x \right) \cos \left( \frac{2\pi \sin \beta}{l} y \right)$$

where, $Ra$ represents the roughness peak amplitude, $l$ represents the roughness wavelength, $\beta$ represents the roughness texture direction.

(6) Viscous pressure equation is expressed as follows:

$$\eta = \eta_0 \exp \left( \ln \eta_0 + 9.67 \right) \left[-1 + (1 + p_0 p)^2 \right]$$

where, $z = \alpha [5.1 \times 10^{-4} (\ln \eta_0 + 9.67)]$, usually take 0.68, $\eta_0$ represents the initial oil viscosity, $p_0$ represents the pressure coefficient, usually take $5.1 \times 10^{-9}$.

(7) Dense pressure equation is expressed as follows:

$$\rho = \rho_0 \left( 1 + \frac{0.6 \times 10^{-9} p}{1 + 1.7 \times 10^{-9} p} \right)$$

where, $\rho_0$ represents the initial oil density.

(8) Load equation is expressed as follows:

$$\int_{\Omega} \rho(x, y) dxdy = w$$

where $w$ represents the external applied load.

(9) Friction coefficient equation

Friction coefficient is an important parameter in the study of EHL. Under the condition of steady state and sufficient oil supply, friction coefficient is determined by the shear performance of lubricant.

In the research of bearing EHL theory, the lubrication oil is generally regarded as Newtonian fluid. In the analysis of point contact and line contact elastomeric flow, the oil film thickness and pressure obtained are consistent with the actual situation. However, in the process of solving the friction, it is found that the friction calculated by using Newtonian fluid deviates greatly from the reality. In addition, it turns out that in the simple fluid that we use, the rheological properties of lubrication oil can be accurately described by Ree-Eyring model. Therefore, the Ree-Eyring
non-Newtonian fluid is used to calculate the friction in the contact area of cylindrical roller bearing, and to obtain the friction coefficients.

Constitutive equation of Ree-Eyring Model is expressed as follows [14]:

\[
\begin{align*}
\tau_x &= r_0 \sinh^{-1} \left( \frac{\eta \nu_x}{r_0 b_0} \right) \\
\tau_y &= r_0 \sinh^{-1} \left( \frac{\eta \nu_y}{r_0 b_0} \right)
\end{align*}
\]  

(9)

where, \( \tau_0 \) represents the extreme shear force of lubrication oil, \( b_0 \) represents the average oil film thickness of the contact area of the rolling bullet flow, \( \nu_x \) and \( \nu_y \) represent suction velocity of roll direction and end-flow rate of the lubrication oil respectively.

Therefore, the calculation formula of friction coefficient can be derived as follows:

\[
\mu = \frac{1}{W} \left( \int \tau_x \, dx \right)^2 + \left( \int \tau_y \, dx \right)^2
\]

(10)

3  FINITE DIFFERENCE METHOD (FDM)

To facilitate numerical calculation, the above basic Eqs. (1)-(10) are transformed into dimensionless form. Dimensionless quantities are defined as: \( P \) represents the dimensionless oil film pressure, \( P = p/\rho \Delta \), \( H \) represents the dimensionless oil film thickness, \( H = h/h_0 \), \( h_0 \) represents film thickness parameter, \( h_0 = b^2/R \); \( \eta^* \) represents the dimensionless oil film viscosity, \( \eta^* = \eta/\eta_0 \); \( \rho^* \) represents the dimensionless oil film density, \( \rho^* = \rho/\rho_0 \); \( W \) represents the dimensionless load, \( W = \omega/(E' R) \); \( X \) represents the dimensionless coordinate variables of rolling direction, \( X = X_0/b_0 \); \( Y \) represents the dimensionless coordinate variables of busbar direction, \( Y = Y/b_0 \); \( U \) represents the dimensionless velocity parameter, \( U = \eta_0 \mu_0 \omega / (E' R) \).

The dimensionless Reynolds equation, oil film thickness equation, dense pressure equation, viscous pressure equation and load equation are discretized by FDM. In this paper, \( X_0 = 2.5 \) and \( X_{out} = 1.5 \), the EHL region is divided equidistantly. Through the continuous iterations of oil film thickness and pressure in steady state, the new oil film thickness and pressure are calculated as initial values, until the iterative process can satisfy the precision requirement of convergence. In order to improve the convergence accuracy and ensure the reliability of the numerical solution, the convergent accuracy of pressure and load is taken as \( 10^{-5} \). Fig. 2 shows the flowchart of FDM calculation program. It can be briefly summarized as follows:

(1) Input basic parameters of the bearing and the load \( w \), then calculate contact width \( b \) according to the load \( w \).

(2) Set the initial oil film thickness \( h_0 \) and oil film pressure \( p_0 \).

(3) Set surface roughness amplitude, wavelength, texture angle.

(4) Calculate the viscosity, density, elastic deformation and oil film thickness.

(5) Solve the Reynolds equation by using the FDM, and obtain the new oil film thickness \( h \) and oil film pressure \( p \).

(6) Judge if the convergence precision of pressure is satisfied or not. If yes, go to step (7). Otherwise, go to step (4).

(7) Judge if the convergence precision of pressure is satisfied or not. If yes, go to step (8). Otherwise, go to step (4).

(8) Calculate the dimensional oil film thickness, oil film pressure and friction coefficients, and output the results.

4  EXAMPLES AND RESULT ANALYSIS

In this paper, the research object is a four-row cylindrical roller bearing, whose bearing type is FC2234120. One row of the bearing is taken as the EHL research object. The calculation parameters are shown in Tab. 1.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inner diameter of inner race</td>
<td>110 mm</td>
</tr>
<tr>
<td>Outer diameter of inner race</td>
<td>124 mm</td>
</tr>
<tr>
<td>Outer diameter of outer race</td>
<td>170 mm</td>
</tr>
<tr>
<td>Inner diameter of outer race</td>
<td>154 mm</td>
</tr>
<tr>
<td>Roller diameter</td>
<td>30 mm</td>
</tr>
<tr>
<td>Viscosity</td>
<td>0.08 Pa·s</td>
</tr>
<tr>
<td>Density</td>
<td>875 kg/m³</td>
</tr>
<tr>
<td>Elasticity modulus</td>
<td>2.2×10¹¹ MPa</td>
</tr>
<tr>
<td>Poisson ratio</td>
<td>0.3</td>
</tr>
<tr>
<td>External applied load</td>
<td>10000 N</td>
</tr>
</tbody>
</table>

Figure 2 Flowchart of FDM calculation program
4.1 Calculation Results under Smooth Condition

Assuming that the contact surfaces between the roller and the races are smooth, after applying the external load as shown in Tab. 1, the oil film thickness and pressure in the EHL region between the roller and the inner race of the cylindrical roller bearing are obtained by the FDM calculation program. And the three dimensional cloud diagram and contour diagram of oil film thickness are shown in Fig. 3.

The oil film thickness presents a downward parabola distribution from the inlet region to the outlet region, and a wave trough of oil film appears in the outlet region. The oil film thickness in the range of Hertz contact width is about 1.5 μm. The oil film thickness distributes evenly along the busbar between roller and inner race. However, the oil film thickness decreases obviously in the end of roller, and the lubrication condition in the middle area deteriorates.

The three dimensional cloud diagram of friction coefficient is shown in Fig. 5(a), and when \( Y = 0 \) and \( X = 0 \), the friction coefficients are shown in Fig. 5(b) and Fig. 5(c). It can be seen from Fig. 5(a) that the friction coefficient is larger in the inlet region than other region. The minimum friction coefficient appears at \( X = 0.5 \) where near the outlet region from Fig. 9(b), and the value is \( 2.901 \times 10^{-3} \). From Fig. 5(c), we know that along the busbar direction, the friction coefficients are approximate symmetric distribution relative to \( Y = 0 \), and distribute uniformly in the middle region.

4.2 The Effect of Surface Roughness Amplitude \( R_a \)

Now, let’s analyze the effect of the surface roughness amplitude of the contact pair between the roller and the inner race. When the wavelength is 0.2\( \mu m \) (\( \phi \) is the contact width) and the texture angle is 60°, the calculation was carried out with different surface roughness amplitudes of \( R_a = 0.02h_0, 0.05h_0\) and 0.1\( h_0 \). Fig. 6 and Fig. 8 show the three-dimensional distribution oil film thickness and pressure with different surface roughness amplitudes, receptively. When \( Y = 0 \) and \( X = 0 \), the two-dimensional oil film thickness, pressure and the friction coefficient are
shown in Fig. 7, Fig. 9 and Fig. 10, respectively. From the calculation results we know that the value of surface roughness amplitude has great influence on the EHL characteristics of cylindrical roller bearings.

It can been seen from Fig. 6 and Fig. 7, that with the increase of the surface roughness amplitude, the peak and valley values of the oil film thickness both increase along the suction direction and the busbar direction. In the busbar direction, the minimum oil film thickness increases slightly at the ends of the roller, and the end lubrication situation is improved.

It can be seen from Fig. 8 that with the increase of the surface roughness amplitude, the oil film pressure increases continuously and fluctuates sharply. Fig. 9(a) shows the variation of oil film pressure along the suction direction. Fig. 9(b) shows the distribution of oil film pressure in the busbar direction, the oil film pressure fluctuates violently at the ends of the roller. At the same time, pressure peak and valley appear in the middle region of the busbar.
Figure 7 The two-dimensional oil film thickness

Figure 8 The three-dimensional oil film pressure

Figure 9 The two-dimensional oil film pressure
It can be seen from Fig. 10 that with the increase of roughness amplitude, the friction coefficient decreases first and then increases in the suction direction. If the amplitude is in a certain range, the friction coefficient will decrease, and if the amplitude exceeds the certain range, the friction coefficient will increase greatly with the increase of the amplitude. The increase of surface roughness amplitude can decrease the friction coefficient to improve the friction conditions, but the unrestrained increase will affect the load distribution.

4.3 The Effect of Surface Roughness Wavelength

In this part, the effect of the surface roughness wavelength will be analyzed. When the surface roughness amplitude is 0.08$h_0$ and the texture angle is 60°, the calculation was carried out with different surface roughness wavelengths of $l = +\infty$, 0.2$b$, 0.5$b$ and 0.8$b$. Fig. 11 and Fig. 13 show the three-dimensional distribution of oil film thickness and pressure with different surface roughness wavelengths, receptively. When $Y = 0$ and $X = 0$, the two-dimensional oil film thickness, pressure and the friction coefficient are shown in Fig. 12, Fig. 14 and Fig. 15, respectively. From the calculation results we know that the value of surface roughness wavelength has great influence on the EHL characteristics of cylindrical roller bearings.

It can be seen from Fig. 11 and Fig. 12, that with the increase of the surface roughness wavelength, the oil film thickness increases first and then decreases. In the reasonable range of wavelength, the increase of the roughness wavelength makes the film thickness fluctuate and the oil film thickness at the end of the bearing increase, which reduces the end effect and improves the lubrication condition of the contact surface. Thus, to a certain extent, the increase of roughness wavelength improves the lubrication condition of bearing surface.
Figure 12 The two-dimensional oil film thickness

Figure 13 The three-dimensional oil film pressure

Figure 14 The two-dimensional oil film pressure
It can be seen from Fig. 13 and Fig. 14 that oil film pressure forms pressure peaks and valleys at the peaks and valleys of the roughness. In a certain range, the bearing capacity of oil film increases with the increase of wavelength. However, from Fig. 13(b) - 13(d), we know that the roughness wavelength cannot be increased much more, which will reduce the EHL performance and make the stress concentration at the end more obvious. The increase of roughness wavelength in a reasonable range is beneficial to the enhancement of EHL performance of cylindrical roller bearings.

It can be seen from Fig. 15 that with the increase of roughness wavelength, the friction coefficient increases first and then decreases in the suction direction, if the wavelength exceeds a certain range, the friction coefficient will increase significantly, and the same law to the friction coefficient in the busbar direction. It can be seen that the surface roughness wavelength affects the friction and wear of the roller contact pair, which increases the uncertainty of the bearing operation. Therefore, reasonable texture surface roughness is conducive to the long-term operation of the bearing.

4.4 The Effect of Surface Roughness Texture Angle $\beta$

The roughness texture angle is caused by the difference between the feed speed and the rotation speed of the workpiece when the surface is machined. In this part, the effect of the surface roughness texture angle will be analyzed. When the surface roughness amplitude is $0.05h_0$ and the wavelength is $0.2b$, the calculation is carried out with different surface roughness texture angles of $\beta = 0^\circ$, $\beta = 30^\circ$, $\beta = 60^\circ$, and $\beta = 90^\circ$. Figure 16 shows the three-dimensional oil film thickness with different texture angles.
30°, 60° and 90°. Fig. 16 and Fig. 18 show the three-dimensional distribution of oil film thickness and pressure with different surface roughness texture angles, respectively. When $Y = 0$ and $X = 0$, the two-dimensional oil film thickness, pressure and the friction coefficient are shown in Fig. 17, Fig. 19 and Fig. 20, respectively. From the calculation results we know that the value of surface roughness texture angle also has great influence on the EHL characteristics of cylindrical roller bearings.

Fig. 16(a) shows the oil film thickness distribution with texture angle $\beta = 0°$ (transverse texture), the three-dimensional oil film thickness along the suction direction distributes as cosine, and the oil film thickness decreases with the increase of roughness texture angle. Fig. 16(d) shows the oil film thickness distribution with texture angle $\beta = 90°$ (longitudinal texture), and the oil film thickness in the $X$ direction is the smallest, which is not conducive to the formation of the EHL oil film. When $\beta = 0°$, the end effect is the most obvious in the busbar direction, and the oil film thickness in the end region is the smallest. The end effect decreases with the increase of roughness texture angle.
The effect of roughness texture angle on the oil film pressure distribution can be clearly seen in Fig. 18. When $\beta = 0^\circ$, the oil film pressure peak increases, especially in the ends of the roller, the pressure value is twice as much as that in the middle region, which will decrease the reliability of the bearing. With the increase of texture angle, the bearing capacity of oil film decreases, and the end effect decreases also, which enhances the reliability of bearing. When the roughness texture angle is $\beta = 90^\circ$, the oil film pressure is minimum because it cannot form an effective oil film, and the oil film pressure distribution is similar to the smooth condition.

It can be seen from Fig. 20, when $\beta = 0^\circ$, the friction coefficient of the oil film is the smallest, because the transverse texture roughness can form a large number of lubrication oil in the peak and valley region, which can form an EHL oil film to separate the roller from the race effectively. When $\beta = 90^\circ$, the effective oil film cannot be formed better, because of the leakage of lubrication oil in the busbar direction. Therefore, the film thickness is reduced, and the oil supply is insufficient, and there will be serious friction and wear problem on both the surfaces.

5 CONCLUSION

In this paper, an EHL model of cylindrical roller bearing with three dimensional cosine roughness based on finite length line contact theory is established, and the program of FDM is complied, by which the EHL performances of cylindrical roller bearing with different surface cosine roughness amplitude, wavelength and texture angle are calculated. According to the results of calculation, it is concluded that:

1. With the increase of the surface roughness amplitude of the contact pair between the roller and the inner race, the oil film thickness increases along the suction direction and the busbar direction, the oil film pressure increases continuously and fluctuates sharply, and the friction coefficient decreases first and then increases in the suction direction. If the surface roughness amplitude is in a certain range, the increase of amplitude can improve the EHL performance of cylindrical roller bearing, but if the amplitude exceeds the certain value, it may bring harm to the operation of the bearing.

2. With the increase of the surface roughness wavelength, the bearing capacity of oil film pressure will increase. However, the surface roughness wavelength is not the larger the better. The roughness wavelength cannot be increased much more, which will reduce the EHL performance and make the stress concentration at the end more obvious. The increase of roughness wavelength in a reasonable range is beneficial to the enhancement of EHL performance of the cylindrical roller bearing.

3. With the increase of the surface roughness transverse texture, the oil film thickness and pressure decrease, and the friction coefficient increases. The transverse texture can form a good oil film shape, but enhance the end effect. Roughness longitudinal texture cannot form a good oil film and the oil film bearing capacity is low, but the end effect is the smallest. Therefore, selecting a reasonable processing technology to produce the surface with a certain texture angle can improve the bearing performance and prolong the service life.

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6 REFERENCES


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