

## MODIFIED ZERILLI-ARMSTRONG MODEL FOR 21-4N HEAT-RESISTANT STEEL

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The Gleeble - 1500D thermal simulator was used to conduct the isothermal compression test of 21 - 4N heat-resistant steel under the T range of 1 273 - 1 453 K and  $\dot{\epsilon}$  of 0,01 – 10 s<sup>-1</sup>. Using the obtained stress - strain data, various parameters of the modified Zerilli-Armstrong (m - Z - A) model were calculated. The constitutive equations of 21 - 4N heat-resistant steel based on the m - Z - A were established. The m - Z - A model can well describe the rheological behavior of 21 - 4N heat-resistant steel. The simulation process can be completed successfully, indicating that the established models can be used for the simulation study of thermal deformation of 21 - 4N heat-resistant steel and are correct. The results can provide some important basic data for the simulation of 21 - 4N heat resistant steel on plastic deformation process.

*Key words:* 21-4N, Zerilli-Armstrong, hot deformation behavior, heat-resistant steel

### INTRODUCTION

21 - 4N is a nickel-plated austenitic heat-resistant steel successfully developed in the 1 950. Since it contains a large amount of Cr, it has high oxidation resistance and corrosion resistance. 21 - 4N is mainly hardened by carbon and nitride precipitation, it exhibits high wear resistance and toughness at high temperatures, and it has cold and heat alternating microstructure stability. Therefore, 21 - 4N is the preferred material for production of high-power internal combustion engine valves operating under high temperature conditions, and is widely used in automobiles, space shuttles, ships and other fields [1]. The constitutive model is a mathematical model of the macroscopic properties of the reactive materials. It plays a crucial role in predicting the flow stress of actual production [2]. The more common constitutive materials. It can provide a reliable theoretical basis for models currently used are the Arrhenius model, Johnson - Cook (J - C) model, Zerilli-Armstrong (Z - A) model, Artificial Neural Network (ANN) and Fields - Backofen (F - B) model.

In recent years, many scholars have studied various constitutive models of different materials. Chan [3] used the F - B model to describe the constitutive relationship of AZ31B magnesium-based alloy. The calculated results are consistent with the experimental results. Tsao et al [4] used the F-B equation to establish and obtained good prediction results. Xu et al [5] established the m - F - B model of AA5083 alloy to predict its high temperature rheological behavior, and obtained

good prediction results. Samantaray et al [6] Z - A model and Arrhenius model to describe the flow behavior of 9Cr - 1Mo steel.

This paper based on the isothermal compression test, the modified Z - A model of 21 - 4N were established by using stress and strain data. In the end, the accuracy was verified.

### MATERIALS AND EXPERIMENTAL

The experimental material in this study is 21 - 4N, and its composition is: 0,48 - 0,58 % C, 0,35 % Si, 8 - 10 % Mn, 0,04 % P, 0,03 % S, 20 - 22 % Cr, 3, 25 - 4,5 % Ni, 0,35 - 0,5 % N, Bal. Fe.

The test was carried out on a Gleeble - 1 500D thermal simulator. The deformation temperature was set as 1 273, 1 333, 1 393, 1 453K, the strain rate was 0,01, 0,1, 1, 10 s<sup>-1</sup>, and the maximum deformation degree was 60 % (the true strain is 0,916). The sample was heated by resistance, and the heating temperature of the sample was measured by thermocouples welded to the specimen. During the test, the two ends of the sample are padded with graphite lubrication sheets to reduce friction, and the experimental data are collected by computer. The size of the test sample is  $\varphi$  8 mm  $\times$  15 mm. During the test, the sample was heated to a preset temperature at a heating rate of 10 K / s, held for 3 minutes, and then heat-compressed at a constant rate. Finally, water quenching immediately after the test was completed.

### RESULTS AND DISCUSSION

The improved Z - A model takes into account isotropic hardening, temperature softening, strain rate

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hardening and the coupling effect of temperature and strain, strain rate and temperature on flow stress, and has a good predictive ability. He et al. [7] have done a lot of researches on modified Z - A model of different materials. Based on the characteristics of the stress - strain curves of 21 - 4N, this paper further modifies the Z - A model. And the modified equation is as follows:

$$\left\{ \begin{aligned} \sigma &= (A_0 + A_1\varepsilon + A_2\varepsilon^2 + A_3\varepsilon^3) \\ &\exp[-(B_0 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3)T^*] \\ &+ (C_0 + C_1T^* + C_2T^{*2} + C_3T^{*3}) \ln \dot{\varepsilon}^* \end{aligned} \right. \quad (1)$$

$$\dot{\varepsilon}^* = \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0}$$

$$T^* = T - T_{ref}$$

In the equation:  $\sigma$  - flow stress, MPa;  $\varepsilon$  - strain;  $\dot{\varepsilon}^*$  - dimensionless strain rate;  $\dot{\varepsilon}$  - strain rate,  $s^{-1}$ ;  $\dot{\varepsilon}_0$  - reference strain rate,  $s^{-1}$ ;  $T^*$  - dimensionless deformation temperature;  $T$  - deformation temperature, K;  $T_{ref}$  - reference deformation temperature, K;  $A_0, A_1, A_2, A_3, B_0, B_1, B_2, B_3, C_0, C_1, C_2, C_3$  - constants related to materials.

When calculating model parameters, it is divided into two conditions: on the one hand, the strain rate is in the range of 0,01 - 0,1  $s^{-1}$ , at which time dynamic recrystallization is the main softening mechanism. On the other hand, the strain rate is in the range of 1 - 10  $s^{-1}$ , at which time dynamic recovery is the main softening mechanism.

**Condition 1:** When the strain rate is in the range of 0,01 - 0,1  $s^{-1}$ , set 0,01  $s^{-1}$  as the reference strain rate. At this point, the solution process of parameters  $A_0, A_1, A_2, A_3, B_0, B_1, B_2, B_3, C_0, C_1, C_2$  and  $C_3$  is as follows:

When the strain rate is the reference strain rate ( $\dot{\varepsilon} = \dot{\varepsilon}_0 = 0,01 s^{-1}$ ), Equation (1) can be rewritten as:

$$\sigma = (A_0 + A_1\varepsilon + A_2\varepsilon^2 + A_3\varepsilon^3) \exp[-(B_0 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3)T^*] \quad (2)$$

Taking the logarithm of both sides of Equation (2):

$$\ln \sigma = \ln (A_0 + A_1\varepsilon + A_2\varepsilon^2 + A_3\varepsilon^3) - (B_0 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3)T^* \quad (3)$$

Figure 1 shows the functional relationship between  $\ln \sigma$  and  $T^*$  at different strain. It can be seen from Figure

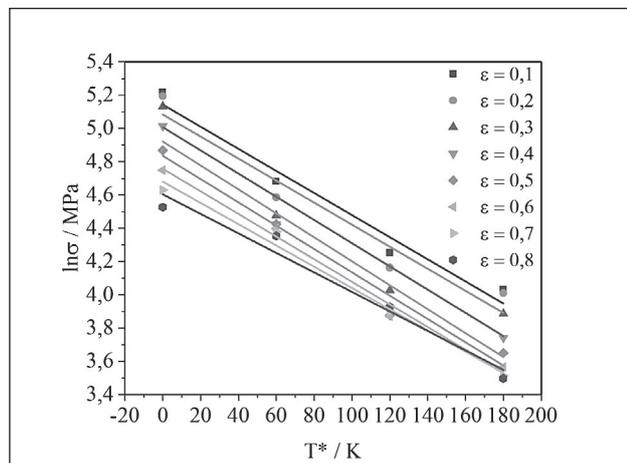


Figure 1 The relationship between  $\ln \sigma$  and  $T^*$  at different strain

2 that  $\ln \sigma$  is linear with  $T^*$ ,  $\ln \sigma = \ln (A_0 + A_1\varepsilon + A_2\varepsilon^2 + A_3\varepsilon^3) - (B_0 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3)T^*$  is the intercept,  $-(B_0 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3)$  is the slope. Let  $K_1 = \ln (A_0 + A_1\varepsilon + A_2\varepsilon^2 + A_3\varepsilon^3)$ ,  $K_2 = \ln - (B_0 + B_1\varepsilon + B_2\varepsilon^2 + B_3\varepsilon^3)$ . The values of  $K_1$  and  $K_2$  under different deformation conditions can be obtained by calculation, as shown in Table 1.

Table 1 The values of  $K_1, K_2$  at different strain.

Strain	0,1	0,2	0,3	0,4
$K_1$	5,14 275	5,08 331	5,00 735	4,92 121
$K_2$	0,00 664	0,00 662	0,00 697	0,0 072
Strain	0,5	0,6	0,7	0,8
$K_1$	4,83 546	4,75 755	4,67 963	4,60 333
$K_2$	0,00 701	0,00 679	0,00 639	0,00 586

The values of  $A_0, A_1, A_2, A_3, B_0, B_1, B_2$ , and  $B_3$  can be obtained by fitting  $\exp K_1 - \varepsilon$  and  $K_2 - \varepsilon$  under different strain with the least square method, as shown in Figure 2. And the results are shown in Table 2.

Table 2 Parameters for the modified Z-A model.

Parameter	$A_0$	$A_1$	$A_2$
Value	181,199	-89,310	-82,581
Parameter	$A_3$	$B_0$	$B_1$
Value	84,461	0,006	0,002
Parameter	$B_2$	$B_3$	
Value	0,0 014	-0.0063	

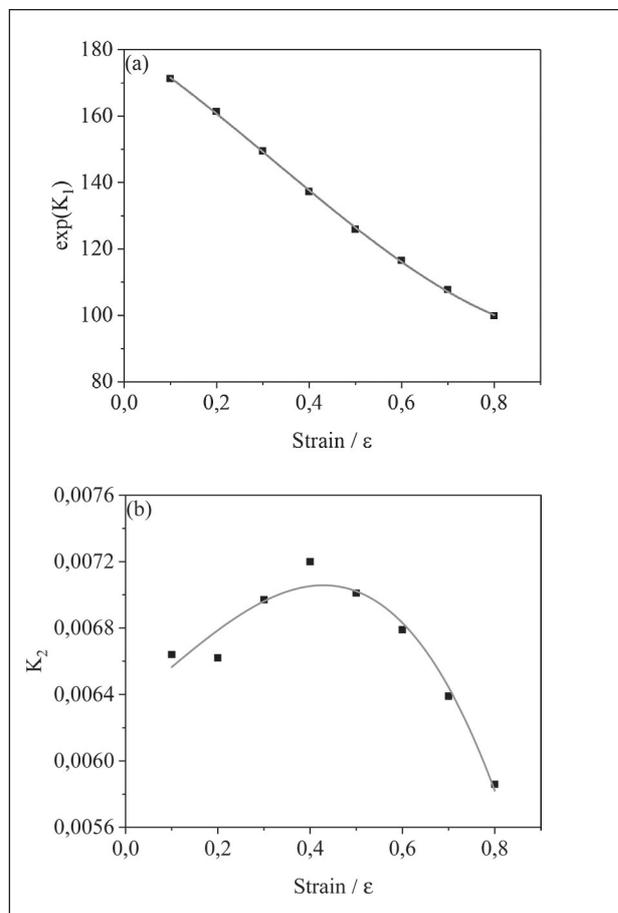
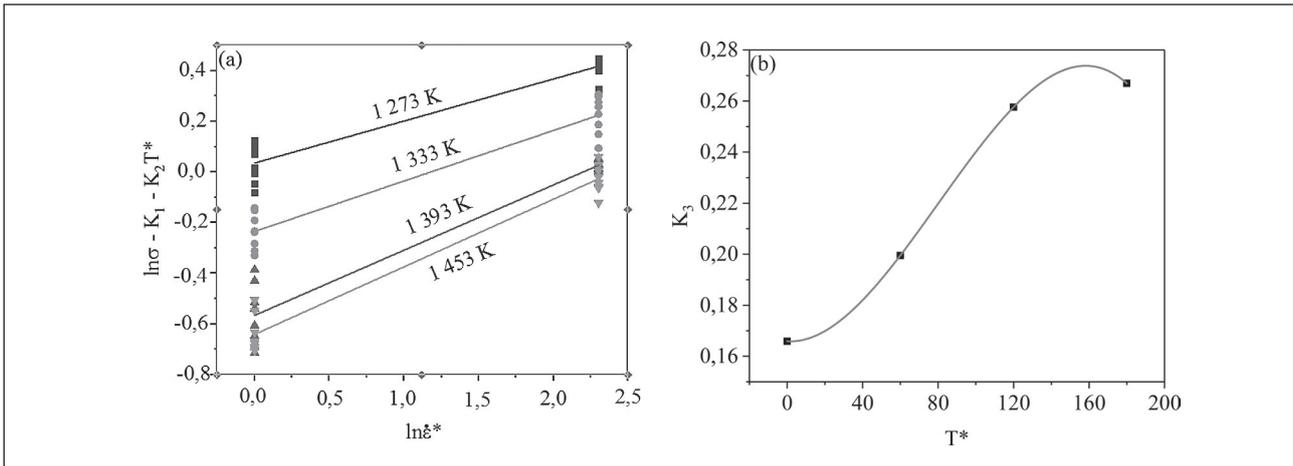


Figure 2 The relationship between  $\exp K_1$  and  $\varepsilon, K_2$  and  $\varepsilon$  at different strain



**Figure 3** The relationship between  $\ln\sigma - K_1 - K_2T^*$  and  $\ln\dot{\epsilon}^*$ ,  $K_3 - T^*$  at different deformation conditions

Taking  $K_1$  and  $K_2$  at different deformation conditions into Equation (2), and fitting  $\ln\sigma - K_1 - K_2T^*$  and at  $\ln\dot{\epsilon}$  different deformation conditions (Figure 3 (a)), the values of  $C_0 + C_1T^* + C_2T^{*2} + C_3T^{*3}$  (let  $K_3 = C_0 + C_1T^* + C_2T^{*2} + C_3T^{*3}$ ) can be obtained, as shown in Table 3.

**Table 3** The values of  $K_3$  at different deformation conditions.

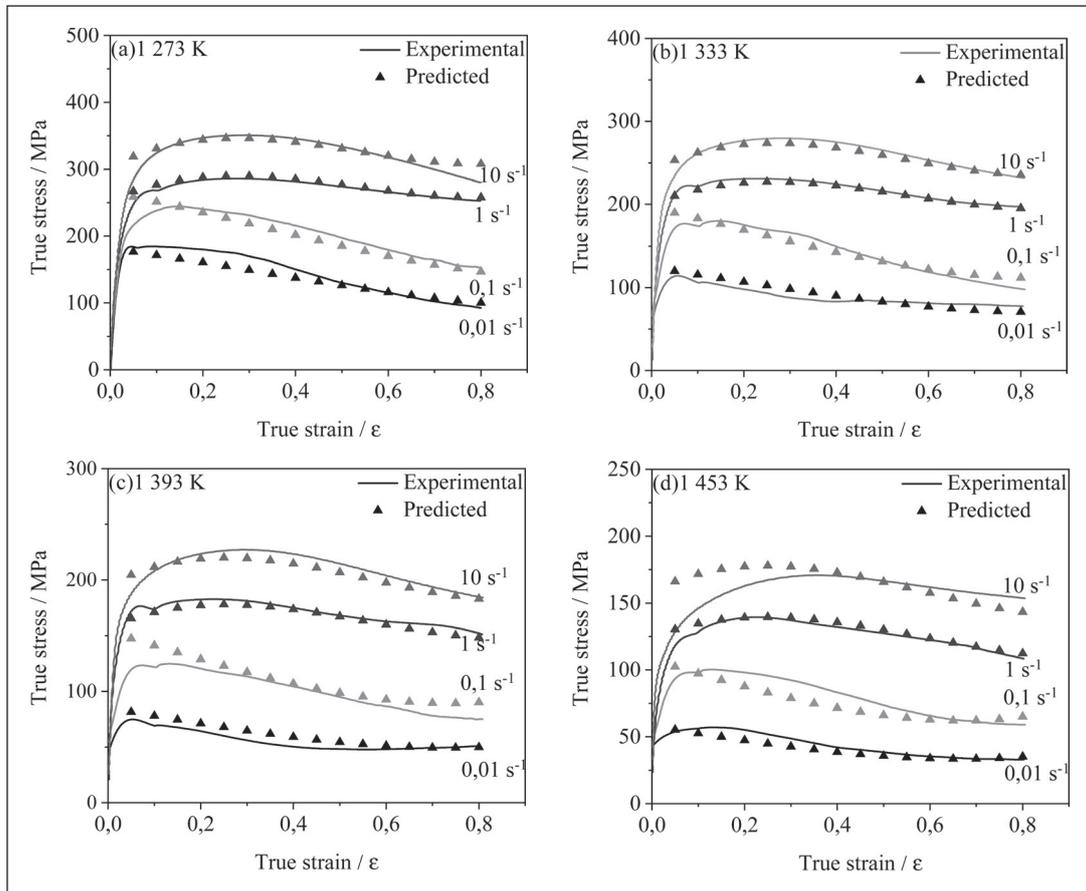
T/K	1 273	1 333
$K_3$	0,16 593	0,19 953
T/K	1 393	1 453
$K_3$	0,25 761	0,26 693

By fitting  $K_3 - T^*$  under different deformation conditions (Figure 3 (b)), the values of  $C_0$ ,  $C_1$ ,  $C_2$  and  $C_3$  can be obtained, as shown in Table 4.

**Table 4** Parameters for the modified Z-A model

Parameter	$C_0$	$C_1$	$C_2$
Value	0,166	$-5,089 \times 10^{-5}$	$1,357 \times 10^{-5}$
Parameter	$C_3$		
Value	$-5,651 \times 10^{-8}$		

**Condition 2:** When the strain rate is in the range of  $1 - 10 \text{ s}^{-1}$ , set  $1 \text{ s}^{-1}$  as the reference strain rate. At this



**Figure 4** Stress prediction of modified Z - A model of 21 - 4N under different deformation conditions

point, the solution process of parameters  $A_0, A_1, A_2, A_3, B_0, B_1, B_2, B_3, C_0, C_1, C_2$  and  $C_3$  is the same as in condition 1, the results are shown in Table 5.

Table 5 Parameters for the modified Z - A model.

Parameter	$A_0$	$A_1$	$A_2$
Value	253,723	299,752	-736,575
Parameter	$A_3$	$B_0$	$B_1$
Value	459,933	0,004	$4,802 \times 10^{-4}$
Parameter	$B_2$	$B_3$	$C_0$
Value	$-7,024 \times 10^{-4}$	0,00 139	0,077
Parameter	$C_1$	$C_2$	$C_3$
Value	$-2,539 \times 10^{-5}$	$1,683 \times 10^{-6}$	$-3,735 \times 10^{-9}$

## MODEL ACCURACY ANALYSIS

Figure 4 shows the calculated stress obtained by the modified Z - A model is basically on the experimental curves under different deformation conditions, indicating that the modified Z - A model has a high predictive ability and can describe the high temperature rheological behavior of 21 - 4N.

## CONCLUSIONS

(1) The modified Z - A model is suitable for the prediction of  $\sigma$  under various deformation conditions in the study range.

(2) By comparing with the experimental value, it is shown that the constitutive relationship of 21-4N alloy can accurately predict the flow stress in the experimental range.

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**Note:** The responsible translator for English language is W.C. PEI North China University of Science and Technology, China