



Original Research Article

Linear Modelling of Water Potential and Supply for Decentralized Energy-Water-Food Systems – Case Study St. Rupert Mayer, Zimbabwe

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ABSTRACT

Limited water accessibility threatens the development of communities, especially where agriculture is the main income source. Implementing decentralized Energy-Water-Food systems is a promising approach to improve the situation in these communities, create synergies and improve the systems' profitability. The model optimizes Energy-Water-Food systems to generate the highest revenues, considering the local conditions and sustainability limits. This work improves the hydrogeological part of the model to model the water potential of a given community. It establishes interrelations of the water sector with the energy and food sectors and maximizes the long-term benefits within the sustainability limits. The proposed method was applied to the rural community of St. Rupert Mayer in Zimbabwe. The sensitivity of the main input parameters is analysed to understand the impact of data uncertainty on the model results. The results indicate that it is important to implement reliable input data for dimensioning the proper system configuration, as otherwise, the whole system would not be sustainable.

KEYWORDS

Decentralized, Energy-water-food systems, Water sustainability, Water availability, Water potential, Optimization model, Linear modelling, Rainwater.

INTRODUCTION

In most rural countries in Sub-Saharan Africa (SSA), their development is threatened by the challenges of supplying basic resources such as energy, water, and food. Due to current tendencies such as population growth and climate change, this situation is prone to get worse, as described by the Food and Agriculture Organisation of the United Nations (FAO) in [1] and [2]. These reports also indicate that the water availability could be enhanced with infrastructure, but most rural communities in SSA have no economic means to install and maintain this infrastructure. Consequently, especially outside big cities, the water supply is a matter of luck

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rather than a controlled situation. As indicated by the FAO in [3], a reliable water supply leads to stable crop production and, therefore, stable revenues, which can pay back the investment and operation costs. One promising approach is the implementation of decentralized Energy-Water-Food (EWF) systems. Nevertheless, the authors of [4] suggest that, until now, a standardized approach to planning and implementing intersectoral systems does not exist.

This work focuses on the definition and improvement of the hydrogeological section of an existing linear optimization tool, the urbs model, described below. Other approaches to assess and plan intersectoral systems at different scales have been developed, but only a limited number of approaches address all sectors simultaneously [5].

Quantitative models for optimizing EWF systems increase the efficiency of resource management by modelling positive and negative interactions of every component in all sectors and optimizing the interconnections. Some works integrate scenario-based analysis for comparison of different setup combinations and economic and physical factors, for example, the works of [6] and [8]. The work of [7] implements EWF value chains analysis (to identify important linkages), analyses the effect of institutions on production processes, and applies the results to different case studies where the actors' decisions depend on economic and social trends. The model proposed in [5] also includes a sensitivity analysis, making the approaches more robust. The work of [9] applies a multi-sectorial system analysis and combines substance flow analysis with regionalized sensitivity analysis to estimate economic benefits.

Optimization model urbs

The existing model used in this work, urbs, is an open-source linear optimization tool programmed in the language Python developed by the Chair of Renewable and Sustainable Energy Systems of the Technical University Munich (TUM). This model identifies the optimum economic configuration to meet the predetermined resource demand at the lowest feasible cost. The minimal total cost results from the techno-economic modelling of all conversion, transmission, and storage processes. A detailed description of the complex mathematical processes behind this optimization tool can be found in [10].

Initially, urbs was designed to optimize energy systems. Previous studies in urbs focused on grid-connected and microgrid renewable energy systems, for example, the works of [12] and [11]. However, urbs can be adapted to design and optimize least-cost EWF systems, thus interconnecting different sectors in circular processes. The works of [13] and [14] present the previous versions of the urbs optimization model for EWF systems. This work adds up to the previous urbs version, focussing on improving the hydrogeological sector of the model.

Figure 1 shows the flow diagram of the model. Here, it can be seen which combination of commodities can be transformed into other commodities through defined processes. Each process comprises a unit ratio for input and output commodities (e.g., m³ of groundwater for a kg of tomatoes) and a cost per unit processed.

The approaches to developing the model are based on two conventional hydrogeological models: the Soil and Water Assessment Tool (SWAT) and the modular finite-difference flow model (MODFLOW). Hydrological and hydraulic models combined can simulate the water flow in two or three dimensions [15]. SWAT is a watershed scale model to predict the impact of land management practices on water, sediment, and agricultural chemical yields. The model is physically based and requires input data from weather, soil properties, topography, vegetation, and land management in the watershed. Then, it models the physical processes of water and sediment movement, crop growth, nutrient cycling, etc. [16]. MODFLOW is an international standard for simulating and predicting groundwater conditions and interactions with surface water. MODFLOW simulates groundwater systems, solute transport, variable-density flow, aquifer-system compaction, and land subsidence [17, 18].

It is necessary to define the sustainable limits of the natural environment to guarantee that the resulting system can be operated long-term. In this model version, the sustainability frame indicates that the system can use only the rainwater infiltrating the community area.

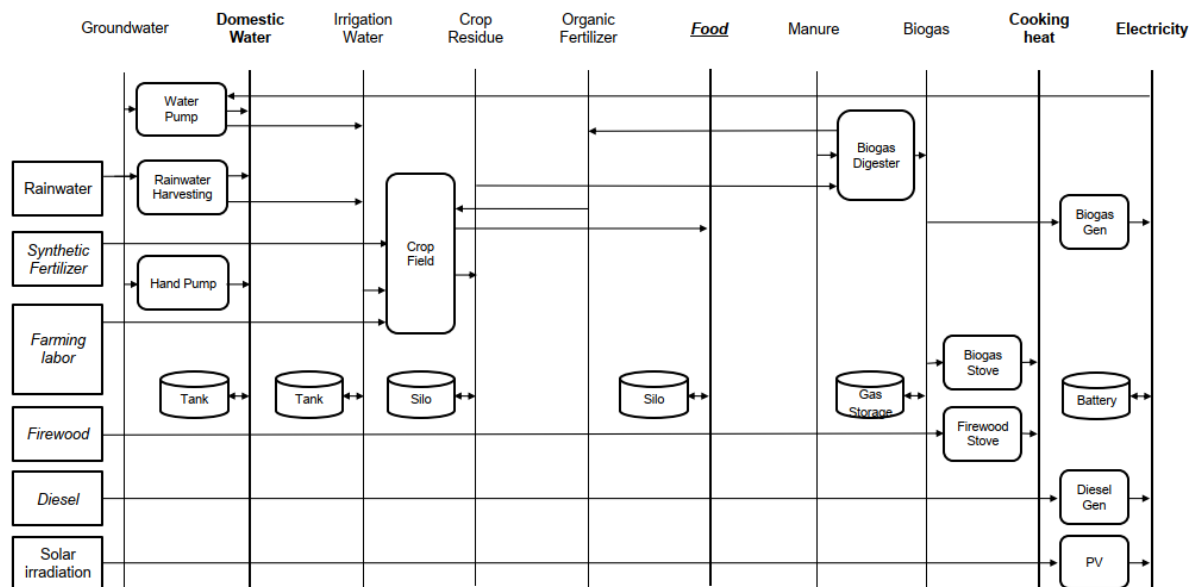


Figure 1. Flow diagram of the urbs model for EWF systems [14]

As the model can be implemented in remote regions, which often do not have access to reliable data, the model results may be affected by uncertainty. Therefore, this work assesses the impact of data uncertainty on the most relevant hydrogeological input parameters.

The developed model is applied to the case study of the Jesuit mission St. Rupert Mayer (SRM) in Zimbabwe. SRM is located 200 km west of the capital Harare, in a rural area with a low population density. The main income sources are agriculture and farming on a small scale, producing maize and vegetables. The mission offers the following services: hospital, preschool, primary school, high school, and a church. The community's water supply now depends on rainfall and electric pumps. Then again, the energy supply for the pumps depends on the centralized supply from the Zimbabwean Electricity Security Authority and on diesel (which often is complicated to obtain). Consequently, in the dry season, there is no water supply if there is no energy supply.

METHODS

The urbs model supplies the demand efficiently and with the lowest possible costs. In the hydrogeological component of urbs, complex natural processes are represented in simplified calculations: as accurate as necessary and as simple as possible. In most locations, the rainfall is the only reliable natural water source, as other possible sources (e.g., rivers or lakes) may not exist in the surroundings or be contaminated [3]. The model's main water source is rainfall (and aquifer recharge). Then, if the model calculates water deficits, it is possible to buy water at a given price per unit.

The input parameters needed to run the urbs model are divided into two main categories:

- Techno-economical parameters – all information regarding the available technologies, including the capacities and operation modes of the machines, as well as the costs for investment and maintenance. The social and economic situation of the community is considered for deciding which processes can be implemented depending on the users' acceptance and capacities of the local operators.
- Environmental parameters – physical, climatic, and hydrogeological parameters (e.g., land use, rainfall, climate, soil, and aquifer characteristics).

The hydrogeological part of the model is divided into two steps: the pre-calculations and the optimization. Every process that does not need to be optimized is pre-calculated, and the obtained results are introduced in the model.

Pre-urbs calculations

These calculations prepare the input data for the hydrogeological processes in an Excel datasheet based on the equations used in the programs SWAT and MODFLOW. The outputs of this tool are net rainfall, aquifer parameters, and water demand.

Net rainfall. Calculates the losses from the total rainfall due to the following factors in a daily resolution: canopy interception and evaporation, runoff, transpiration, soil retention, and soil evaporation. The "net rainfall" is the amount of rainwater that can be used in the model. The involved hydrogeological processes are presented in **Figure 2**.

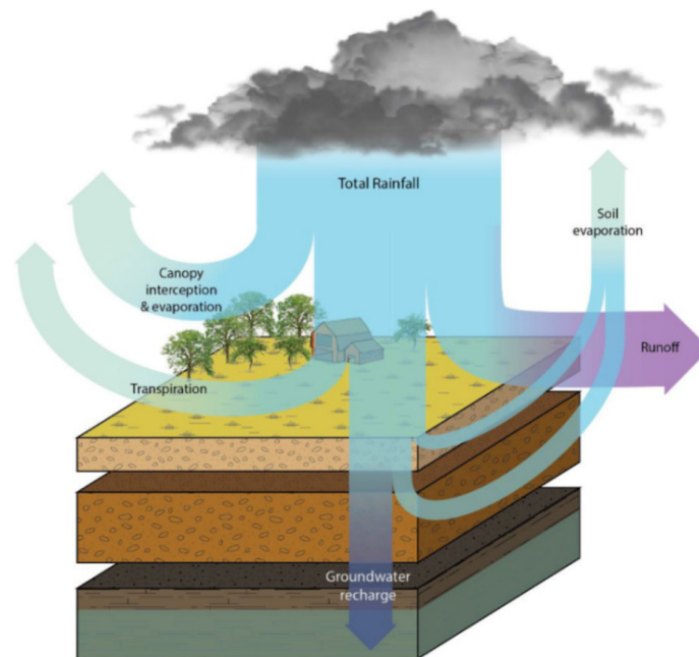


Figure 2. Natural processes involved in the calculation of the net rainfall

The most important input parameters include reliable rainfall data. A suitable option is the remote sensing data from the Tropical Rainfall Measuring Mission (TRMM) [19, 20].

Similar to the calculation approaches of the SWAT program, the community's area is subdivided into "Hydrological Response Units (HRUs)". These subareas are classified depending on land use, topography (slope), soil type, and vegetation [15]. This assessment and the calculation of the HRUs can be made using Geographic Information System (GIS) tools and digital elevation models. For this model setup (adapted to the case study), the HRUs are grouped in three different sectors, which have different processes for the falling rainfall:

- A) Crop fields – the rainfall can supply the crops' water demand directly and recharge the aquifer. The net rainfall is the sum of the groundwater recharge plus the retention in the top soil and unsaturated zone (UZ), minus the soil evaporation.
- B) Area outside the crop fields minus the area of buildings – this sector can be subdivided into different land uses (HRUs), such as fallow land (B.1) and forest (B.2). The rainwater falling in this sector can only be utilized if it reaches the aquifer.
- C) Building roofs – the rainwater falling in this sector can be harvested to supply the domestic water demand.

The following hydrogeological processes are calculated daily in the pre-urbs tool:

- Evapotranspiration – depending on the potential evapotranspiration and water available.
- Interception – the rainfall volume intercepted by the vegetation, which can evaporate depending on the Leaf Area Index (LAI) and climatological aspects [21, 22]. The tool calculates the daily amount of rainfall stored and evaporated and the amount exceeding the retention capacity.
- Runoff – this quantity depends on the slope, soil type, vegetation, and dryness or saturation of the ground, as well as on the rainfall intensity [23]. The calculation employs the Soil Conservation Service runoff equation [24], considering the previous rain events.
- Transpiration – the amount of water consumed by the plants depending on their morphology and growth phase and available water. For the B sector areas (forest and fallow land), this process is a "water loss".
- Soil evaporation – if the potential daily evaporation has not been met after canopy evaporation and transpiration, a certain volume will evaporate from the soil's water retention. Depending on the climatic and geological circumstances, the water can be extracted from the top soil or deeper layers. This amount depends on the degree of shading and the extent of biomass above the ground (vegetation) [22].

Soil and Aquifer data. The urbs model conceives three ground layers: the Top Soil layer (TS), the Unsaturated Zone (UZ), and the aquifer (Aq), as can be seen in **Figure 3**.

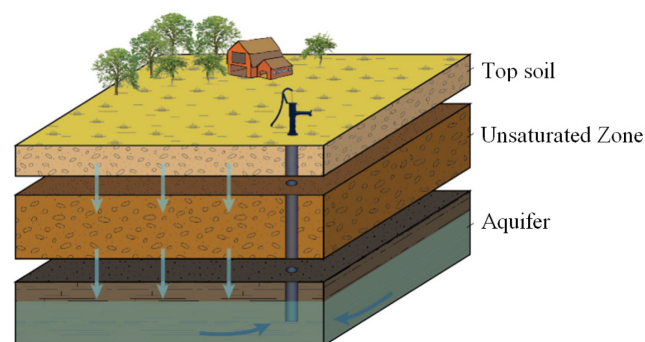


Figure 3. Ground storage units in urbs

The soil evaporation and the water amount exceeding the retention capacity are calculated daily to indicate the volume percolating to the lower ground layer. The groundwater flow is described by Darcy's Law [22], whereas the rate at which the infiltrated water reaches the water table depends on the thickness of the UZ [25]. The relation between rainfall and percolation is directly related to the annual rainfall pattern (intensities) [26, 27]. As the aquifer's water-storage capacities may vary greatly over short distances [28], extensive measurements should be done onsite to define the structure of the aquifer. General geological data, for example, the Quantitative Maps of Groundwater Resources [29], constitute an option for rough estimations of the aquifer structure.

Water demand data. Two kinds of demands expressed as hourly rates are the drivers of the optimization processes:

- Domestic water demand – it is measured for the given community, considering the minimum water demand per person of 50 litres per day [30].
- Crop water demand – the crop evapotranspiration [31] is calculated depending on local climatic and geographic characteristics, as well as on the crop type and its growth phase. The program CropWat 8.0 from the FAO is a useful tool [32, 33]. As crops can resist a couple of days without irrigation [31, 34], this supply is flexible in time and volume.

Water component of the urbs model

The urbs model operates with a complex Python optimization code, which gathers input data from a structured Excel document. It includes all hydrogeological processes directly affecting the water availability per time step and the system's costs. The model flow diagram can be seen in **Figure 4**. The model input data are classified in:

- Demand – defined in m³/h of each water type;
- Commodities – resources including their prices per unit [€/m³];
- Fluctuation supply – availability of natural resources at each time step;
- Processes – specification of costs and efficiencies involved (e.g., transport capacities [m³/h], annual fixed costs [€/y per m³/h], etc.);
- Process-Commodities – the ratio between input and output commodities for every process;
- Storage – storage units for a specific commodity, including a percentage loss per hour (represents tank leakages or evapotranspiration).

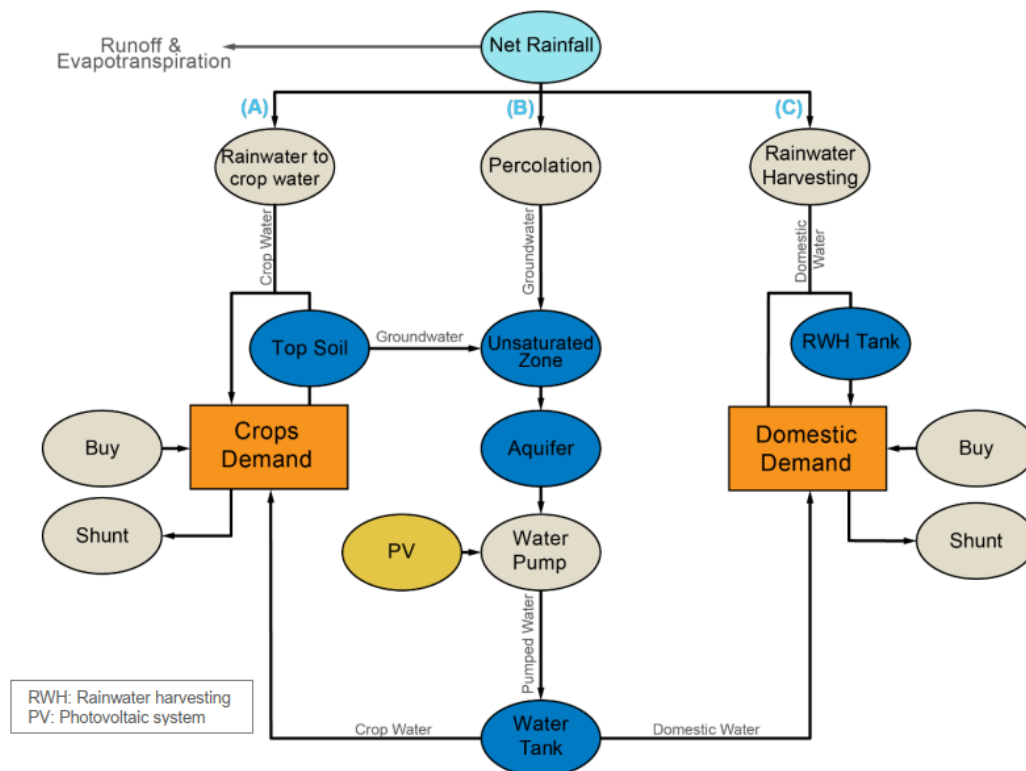


Figure 4. Flow diagram of the water component of the urbs model

As can be seen in **Figure 4**, the domestic water demand is supplied from the pumped groundwater and harvested rainwater, whereas the crop water demand is supplied by:

- Rainwater – calculated by multiplying the net rainfall by the crops area and used in three ways: 1) to supply the demand directly; 2) if its volume is greater than the demand, the rest is stored in the top soil for later use; 3) percolation to deeper layer if the top soil is saturated.
- Irrigation – if the usable rainwater does not cover the demand, the missing volume is supplied through irrigation. The total Irrigation Delivery Requirement (IDR) includes the plant watering requirement and the water losses for distribution.

The system will buy water if the local water resources are insufficient to cover the demand. This also indicates that the system is not self-sustainable and should be improved (e.g., by changing the crop types for ones consuming less water).

The net rainfall is introduced into the model as an intermittent supply input. It is modelled as a change in capacity (a capacity of 100 % represents a rainfall of 10 mm/h) multiplied by the area of each HRU.

The ground layers are represented as storage units with specific urbs properties: storage capacity, input-output capacity (representing infiltration), and hourly discharge (representing soil evaporation). For simplification, it is assumed that the ground is homogenous in all directions and completely interconnected. The infiltration rate is modelled by adopting the methods of the program MODFLOW, which calculates the groundwater flow in three-dimensional ground units [18]:

- Top soil storage (TS) – the storage capacity is calculated as the crops area multiplied by the root depth and water percentage available for the plants (soil porosity minus the wilting point). The commodity stored is Crop Water and is affected by soil evaporation.
- Unsaturated Zone, modelled analogously to the top soil. It buffers the water path from the top soil to the aquifer, which is modelled as a transfer from the TS unit into the UZ at a given (percolation) rate. The stored water cannot be used.
- Aquifer – for simplification, represented as a shallow unconstrained aquifer. The total volume is the community area multiplied by the aquifer depth and the usable storage capacity.

The model's infrastructure system is composed of a solar pump, photovoltaic panels, and a storage tank, which are dimensioned to optimize all costs. To generate electricity, the process "PV" converts the fluctuating resource solar irradiation into electricity, where the efficiency is determined by the solar capacity factor per time step. In the solar-pump process, electricity and groundwater are the inputs with specific ratios, and "pumped water" is the output. This commodity is stored in tanks and can be transformed into "crop water" or "domestic water" to supply the respective demands. The pump size is limited by the aquifer's extraction capacities. The pump rate should be obtained by performing pump tests onsite. The hydraulic sizing of the submersible pump represents the electrical power needed to pump one cubic meter of groundwater to the storage tank, considering the dynamic groundwater level and the system efficiency.

Sensitivity analysis

Because of the uncertainty of the available data, it is necessary to identify which input parameters have a greater impact on the model results. Some parameters may need exact input data to obtain reliable results.

The base scenario consists of one solar pump to cover the water demand of 15 ha of Maize with three harvests per year and a community of 600 people. For this analysis, the following parameters are to be tested:

- Maximum pumping rate (max. Q) – the limit of the pumping rate must be based on aquifer characteristics. The values used are 0.1, 0.5, 1.0, 1.5 and 2.5 l/s
- Aquifer hydraulic conductivity (K) – affecting the infiltration rate and storage capacity. The values used are $K = 8E-07$ m/s for the base scenario, $3E-04$ m/s for the best-case scenario, and $8E-09$ m/s for the worst-case scenario (fractured metamorphic rock) [35].
- Aquifer storage capacity – in the base scenario, the aquifer area is the area of the whole community, assumed to be completely interconnected (every water drop percolating anywhere could be extracted by the pump). For the worst-case scenario, the aquifers area is 0.75 % of the community area and has a hydraulic conductivity of $K = 8E-09$ m/s.
- Land use – two scenarios are analysed: 1) deforestation scenario, 73.7 % of the forest area is converted into fallow land; 2) afforestation scenario, the forest area increases 66.5 %
- Rainfall pattern – different scenarios are analysed, representing changes due to climate change and local environmental changes. Two artificial rainfall patterns with the same total rainfall amount (864 mm/y) are considered. In the first scenario, the daily rainfall intensities are reduced, and the total rain volume is distributed over more days in the wet season (mid-November to mid-March). In the second scenario, the daily rainfall intensity

is increased, and the number of rainy days is reduced, concentrating the water volumes on fewer days. These rainfall patterns can be seen in **Figure 5**.

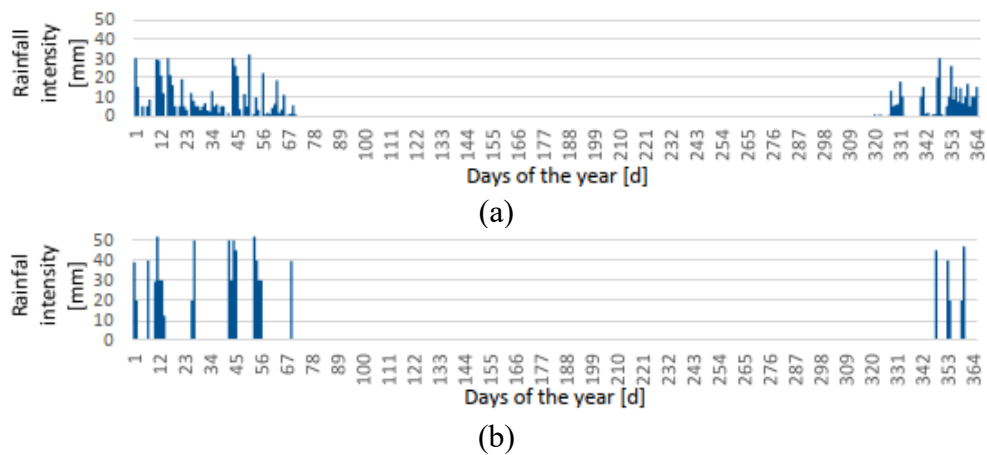


Figure 5. Modified rainfall intensity patterns: (a) first scenario; (b) second scenario

RESULTS AND DISCUSSION

In the following, the results of the pre-calculations and the urbs model are presented and discussed.

Pre-calculation results

For the case study in SRM, four HRUs are defined (crop fields, fallow land, forest, and buildings), and their respective net rainfall values are calculated. The calculated yearly water balance for 2017 can be seen in **Figure 6**. This figure shows which amount of the total rainfall is available for the model (groundwater) and which is lost due to the different factors (runoff, canopy interception, soil evaporation, and transpiration). The forest HRU supplies the highest amount of available water for the model with 233.5 mm, whereas the fallow land only supplies 4.3 mm. For the crop area, the useful water amount comprises the groundwater (83.9 mm) and the plant's transpiration (287.1 mm), thus reducing the demand for irrigation.

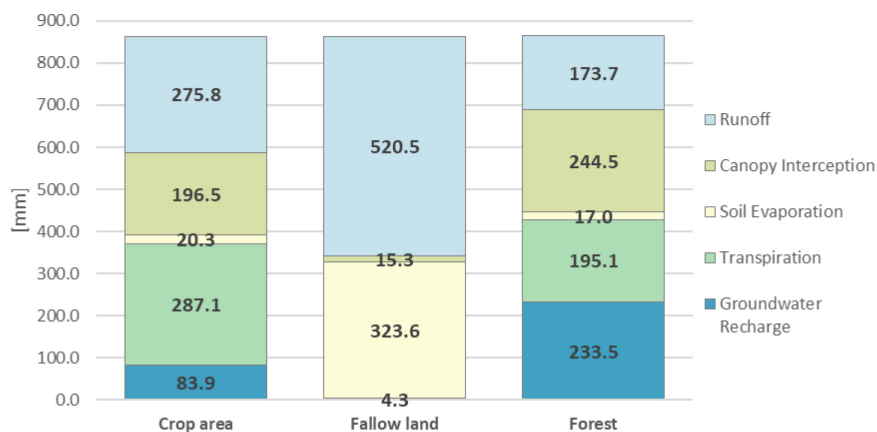


Figure 6. Steady state water balance in SRM, 2017

The forest HRU has greater canopy interception and transpiration losses than the fallow land, but in the fallow land, the losses through runoff and soil evaporation are significantly higher, which affects the percentage of groundwater recharge. This is a clear example of the value of trees and vegetation, which also increases the roughness of the ground, decreasing the surface runoff [23]. Considering the small water cycle and its long-term effects, by increasing the vegetation, it is possible to preserve and increase the local water availability [36].

The water sources to cover the domestic demand are shown in **Figure 7**. During the rain season, the domestic water demand is supplied mainly through rainwater harvesting (purple) and the stored water (yellow) — there is no need to use the pump. In the dry season, the demand is covered by a combination of a water pump (blue) and storage.

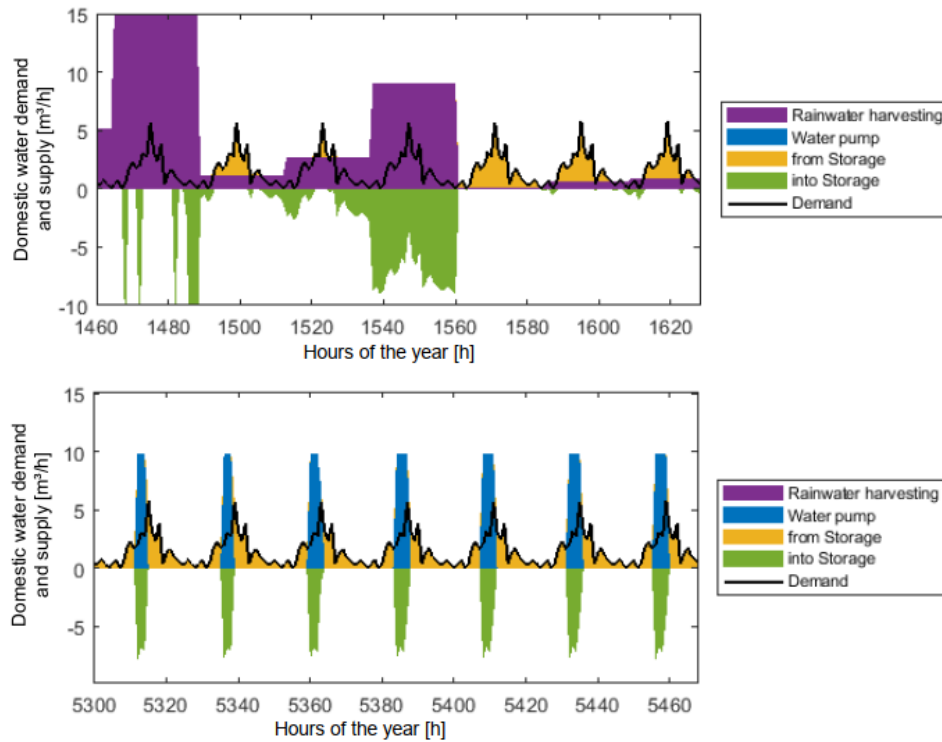


Figure 7. Domestic water demand: rainy season (top) and dry season (bottom).

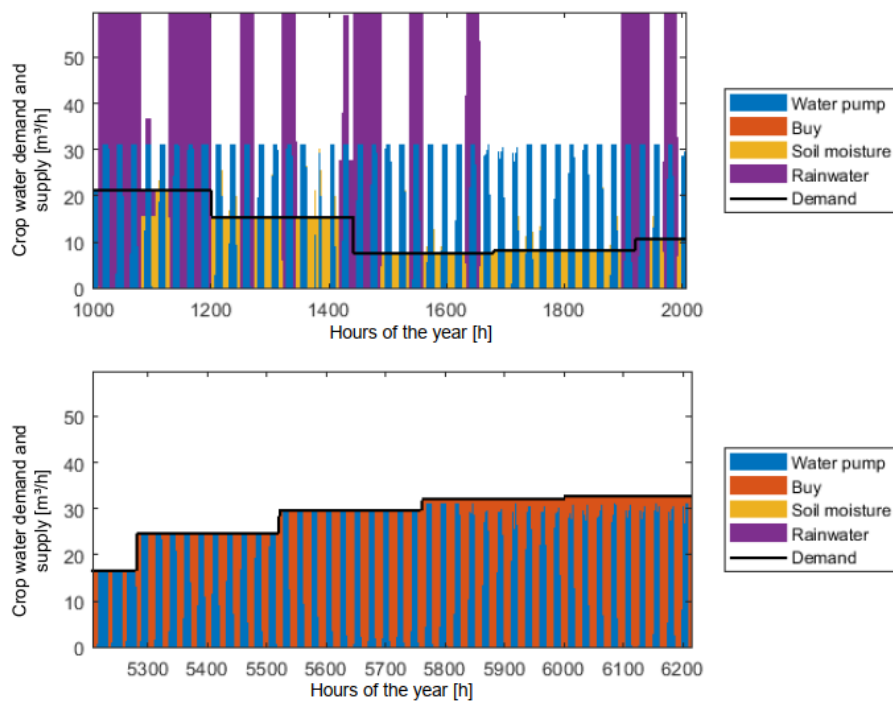


Figure 8. Crop demand: rainy season (top) and dry season (bottom).

The water sources to cover the crop water demand can be seen in **Figure 8**. For the crop water demand, during the rainy season, a great amount is covered directly by the rainwater

(purple) stored in the top soil (yellow). When the incoming rainfall exceeds the demand and the soil's retention capacity, this amount percolates into the lower ground layer, reaching the aquifer at some point. The stored water volume in the top-soil layer can be seen in **Figure 9**. As the operation costs for the solar pump (blue) are assumed negligible, it runs for some hours every day, even though it is not necessary.

In the dry season, the only local water source available is the solar pump (blue), which is not enough to cover the demand. Therefore, the model indicates that buying water (orange) is necessary to cover the deficits.

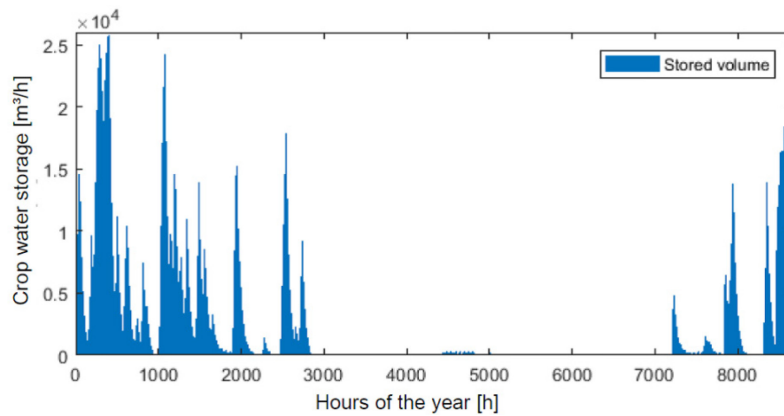


Figure 9. Top Soil storage

Sensitivity analysis

The maximum pumping rate (max. Q) significantly impacts the model optimization. **Figure 10** shows the water sources to cover the demand and their shares for each scenario with different pump rates. The water deficit (buy) increases for lower pumping rates, being 99,224 mm for a rate of 0.1 l/s and 0 mm for a rate of 2.5 l/s.

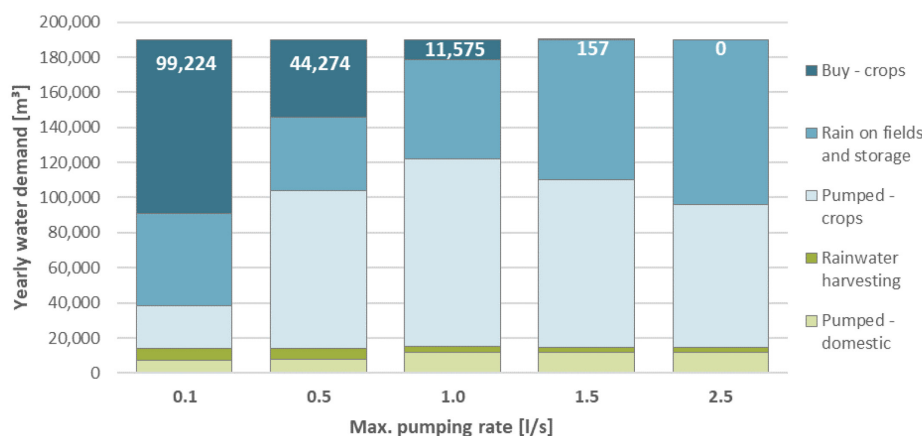


Figure 10. Effects of maximum pumping rate on the coverage of the yearly water demand

As can be seen in **Figure 11** and **Figure 12**, the max. Q impacts the water deficit significantly, especially in the dry season. With a max. Q of 0.1 l/s, in the dry season, the available water (blue) is critically lower than the demand (the orange area represents the water deficit to cover the demand). A max. Q of 1 l/s improves the water supply significantly, but it is still insufficient to cover the demand in the dry season. For a pumping rate of 1.5 l/s, the water deficit represents 0.08 % of the demand. **Figure 13** shows the amount of water deficit for each scenario.

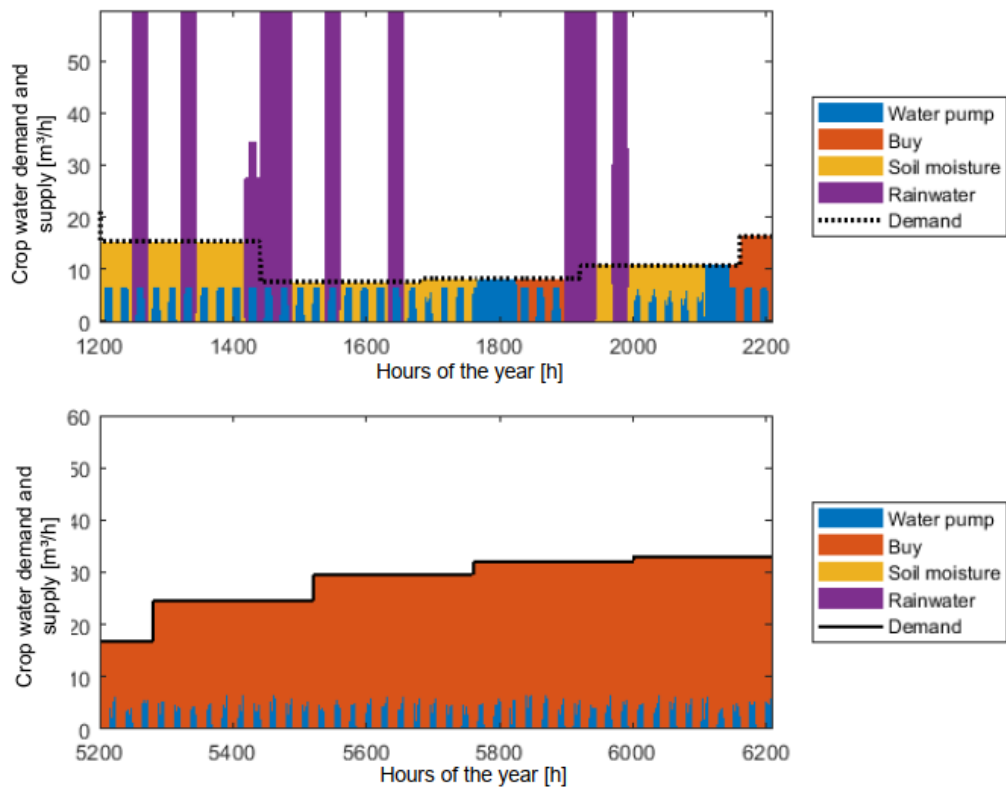


Figure 11. Max. $Q = 0.1$ l/s – Crop Water supply in the rainy season (top) and dry season (bottom)

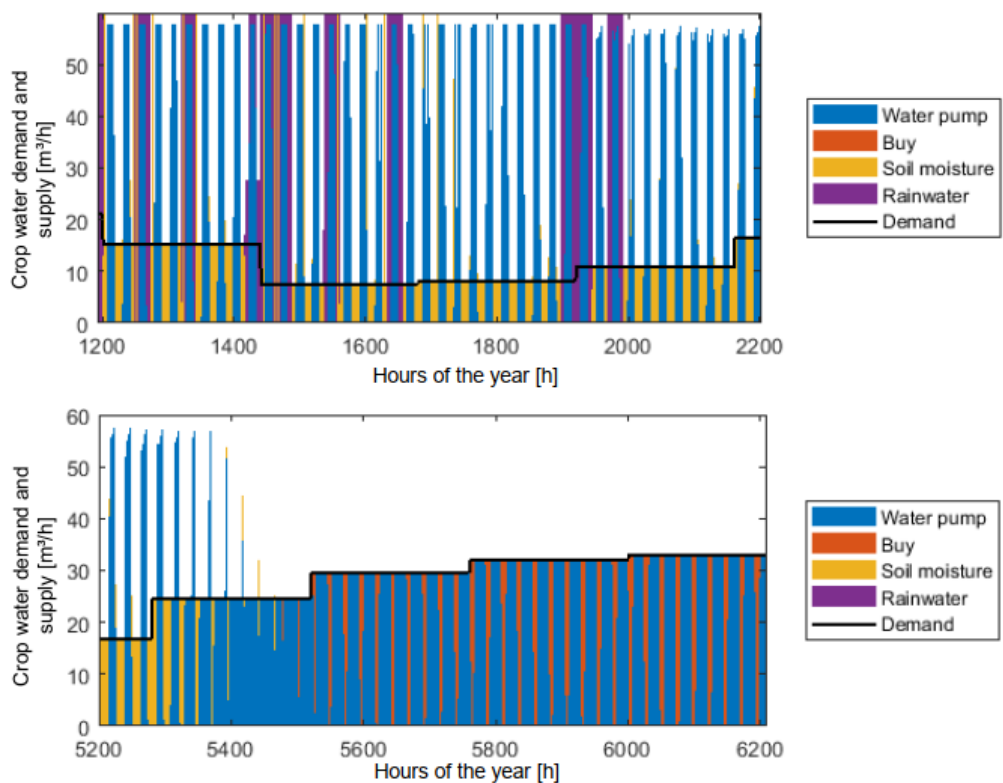


Figure 12. Max. $Q = 1.0$ l/s – Crop Water supply in the rainy season (top) and dry season (bottom)

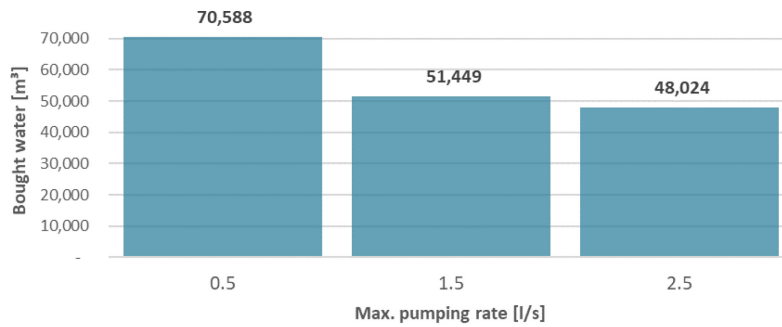


Figure 13. Water deficit for different max. Q values and K = 8E-09 m/s

The parameter aquifer’s hydraulic conductivity has an impact on the water deficit. Even in scenarios where large maximum pumping rates are allowed, this parameter is limited by the aquifers properties. Therefore, the hydraulic conductivity has a greater importance for the optimization. This impact can be seen in [Figure 14](#).

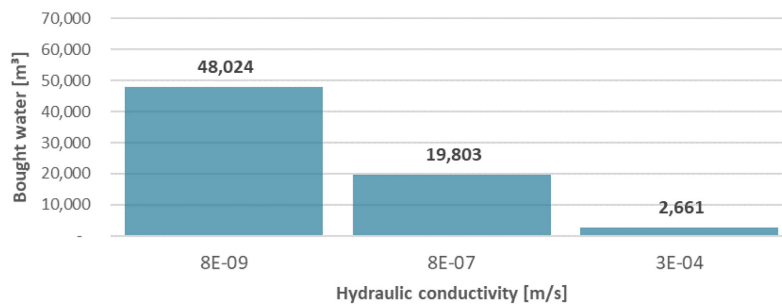


Figure 14. Water deficit for different K values and max. Q = 54 m³/h

The parameter aquifer storage capacity has a significant impact on the optimization results. The percolation rate into the aquifer is 28.8 m³/(h ha) in the base scenario, compared to 0.3 m³/(h ha) in the worst-case scenario (decreased aquifer area and hydraulic conductivity), increasing the total water deficit. These results can be seen in [Figure 15](#).

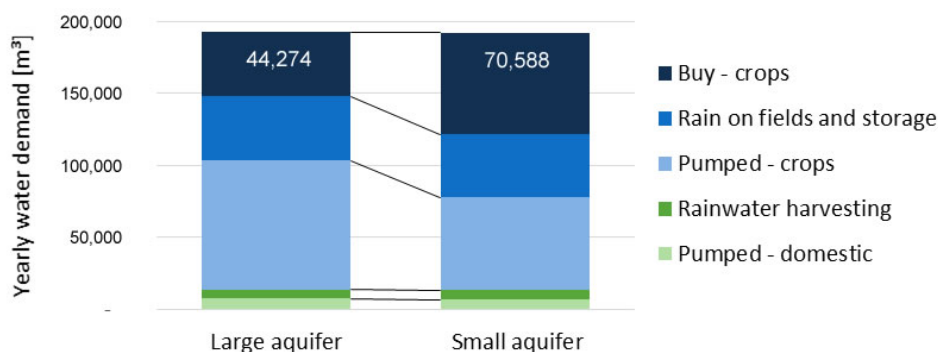


Figure 15. Effect of aquifer size on the coverage of the yearly water demand

In the base scenario, the pumping rate is the limiting factor. In the worst-case scenario, the limiting factor is the groundwater storage volume. Thus, urbs administrates the available resources by implementing lower pumping rates. In the base scenario, the aquifer is frequently full (storage volume of 80,000 m³); in the worst-case scenario, the maximum volume stored is 697 m³ (right after the rainy season). The stored volume constantly decreases to empty by the

dry season's end. In the "perfect" scenario for this case, the aquifer storage capacity must be big enough to store the groundwater needed in the dry season, and the pumping rate should be 2 l/s or higher.

Regarding land use, in SRM, from the 864 mm of total rainfall in the year 2017, the fallow land has a calculated yearly runoff of 520.5 mm (60.3 %) and the forest 173.7 mm (20.1 %). Whereas the forest area contributes to the yearly groundwater recharge, a calculated volume of 233.5 mm (27.0 %), the fallow land contributes only 4.3 mm (0.5 %). In the deforestation scenario (forest area decreases 73.7 %), the runoff volume increases 50 %, and the groundwater recharge decreases 67.2 %. In the afforestation scenario (forest area increases 66.5 %), the runoff volume decreases 44.2 %, and the groundwater recharge increases 60.6 %.

Nevertheless, the land use has little impact on the results of the model optimization. This may be due to the local rainfall patterns (intense rainfall events and long dry periods) with high runoff and evapotranspiration rates. In the rainy season, the available rainwater exceeds the demand and storage capacities, but at the end of the long dry season, all available water (from storage) is consumed. Considering the local natural conditions, it is clear that the rainwater storage capacities should be increased to cover the demand of the whole year.

With the rainfall intensity and pattern of SRM (short events of high intensity in the rainy season), even receiving a greater volume of rainwater would not decrease the water deficit significantly because the water availability in the dry period would not increase. Instead, a rainfall pattern with lower intensities and more rainy days would improve the local water availability, especially if the dry season is shortened. The effects of different rainfall intensities on the yearly water balance can be seen in **Figure 16**.

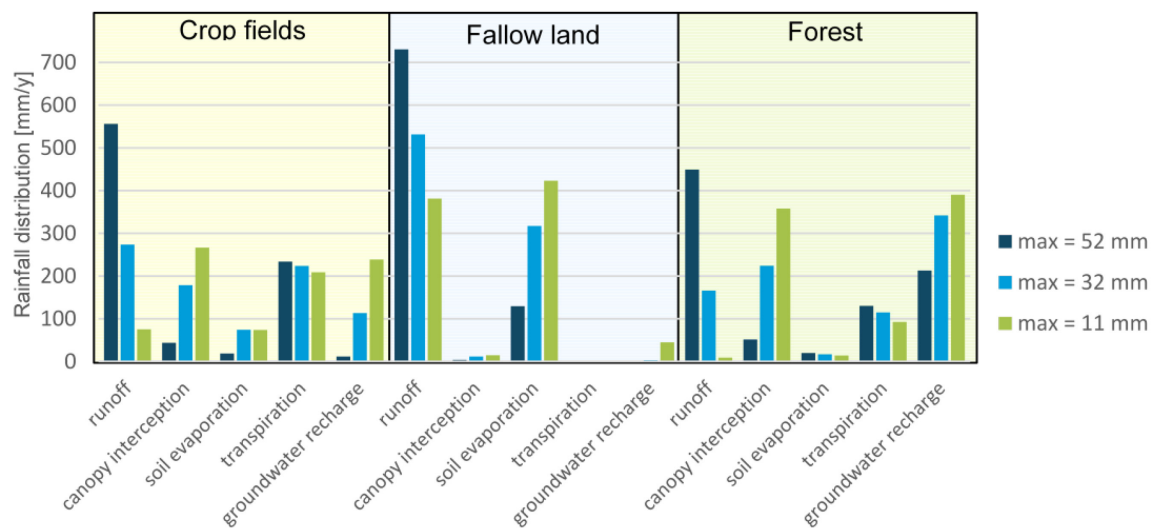


Figure 16. Effect of rainfall intensity (52 mm, 32 mm, and 11 mm) and distribution patterns on the yearly water balance for the different HRUs

The rainfall intensity and pattern significantly impact the calculation of the net rainfall. In all HRUs, the runoff percentage rises with increasing rain intensities. Concerning the losses through canopy interception in the crop fields and the forest areas, these losses increase with more rainy days of lower intensities. The same applies to the losses through soil evaporation in the fallow land. In contrast, the groundwater recharge in the fallow land decreases for rain patterns of high intensities on less rainy days because losses through surface runoff are greater. Further on, in the rainy season, whereas a rain pattern of low intensities is enough to cover the whole demand, the rain pattern of high intensities and less rainy days presents water shortages. This deficit occurs because the rainfall volume at each rain event is greater than the volume that can be used or retained; thus, a smaller amount can be utilized.

CONCLUSION

This work develops the water component of the urbs model to represent hydrogeological processes – as accurately as necessary and as simple as possible – in the frame of a decentralized EWF system. A pre-urbs calculation tool is created to estimate all model input parameters that need not be optimized. The urbs model is improved based on the approaches used in conventional hydrogeological models. To assess the performance of the model, it is implemented in the rural community of St. Rupert Mayer, Zimbabwe.

The available input data are examined in the Sensitivity Analysis to assess the impacts of some parameters on the results. This analysis indicated the aquifer characteristics are the most sensible parameters. However, these input data are the most difficult to obtain in remote rural areas, especially if it is not possible to do measurements onsite.

The urbs model is a valuable tool to optimize the elements of an EWF system and to assess if the planned dimensioning is sustainable or not, providing the input data are reliable. The final results must be corroborated in detail, as the uncertainty in the input data may have an impact. Further on, the model optimizes the costs of the system within the physical and sustainability limits. However, the model cannot describe the accurate allocation of water resources that must be defined by experts. Also, the allocation and installation of the system components require professional expertise.

The water component of urbs could be improved using GIS methods to define and calculate the HRUs. Another possible improvement is to consider additional water sources, for example rivers or the reuse of treated wastewater. Further on, the whole model could be developed to model urban systems, including further infrastructure elements, such as, for example, biogas (energy) generated from wastewater in treatment plants. Additionally, extra measures to increase the local water availability could be implemented in the community, for example, reducing the runoff, collecting rainwater for agricultural use, increasing the aquifer recharge, and adapting the crop fields to reduce water losses.

The limited water availability is one significant factor threatening the development of rural communities in Sub-Sahara-Africa, especially if the main source of income is agriculture. This situation will worsen due to climate change, where the available water will decrease due to extreme seasons. Guaranteeing a water supply reduces the dependency on rainfall events and minimizes the impacts of climate variability. Moreover, the farmers can increase their revenues as the agricultural activities are not limited to the rainy season.

Decentralized Energy-Water-Food Systems are a promising approach to prompt development in remote rural communities, supplying the community's needs with low environmental impacts and generating revenues. The program urbs can be used for dimensioning decentralized EWF systems for a given location and optimizing each of the system components within the sustainability frame, securing the food and water supply.

NOMENCLATURE

Abbreviations

Aq	Aquifer
EWF	Energy-Water-Food
FAO	Food and Agriculture Organisation of the United Nations
GIS	Geographic Information System
HRU	Hydrological Response Units
IDR	Irrigation Delivery Requirement
K	Aquifer hydraulic conductivity
LAI	Leaf Area Index
MODFLOW	Modular finite-difference flow model
Q	Pumping rate
SRM	St. Rupert Mayer (Community in Zimbabwe)

SSA	Sub-Sahara Africa
SWAT	Soil and Water Assessment Tool
TRMM	Tropical Rainfall Measuring Mission
TS	Top Soil
TUM	Technical University Munich
UZ	Unsaturated Zone

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