Correctness by Construction for Pairwise Sequence Alignment Algorithm in Bio-Sequence

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Abstract: Pairwise sequence alignment is a classical problem in bioinformatics, aiming at finding the similarity between two sequences, which is important for discovering functional, structural and evolutionary information in biological sequences. More algorithms have been developed for the sequence alignment problem. However, there is no formal development process for the existing pairwise sequence algorithms and leads to the low trustworthiness of those algorithms. In addition, the application of formal methods in the field of bioinformatics algorithm development is rarely seen. In this paper, we use a formal method PAR to construct a pairwise sequence alignment algorithm, analyze the essence of the pairwise sequence alignment algorithm, construct the Apla algorithm program by stepwise refinement, and further verify its correctness. Finally, a highly reliable and executable pairwise sequence alignment algorithm program is generated from Apla program via PAR platform. The formal construction process ensures the reliability of the algorithm, and also demonstrates the algorithm design idea clearly, which makes the originally difficult algorithm design process easier. The successful practice of this method on the pairwise sequence alignment problem in biological sequence analysis can provide a reference for the construction of highly reliable algorithms in complex bioinformatics from both methodological and practical aspects.

Keywords: automatic verification; correctness by construction; pairwise sequence alignment; PAR method

1 INTRODUCTION

The biological macromolecular sequences studied in current biological analysis usually evolved from ancient ancestral sequences. If two related sequences evolved from the same ancestral sequence, then they are said to have homology, and one of the main bases for judging the homology between the two is similarity [1]. Sequence similarity is usually assessed by the character differences between sequences, where an effective measure to analyze whether sequences have sufficient similarity to each other is sequence alignment. Pairwise sequence alignment aims to find the similarity relationship between two sequences and is a classical problem in the application of computers to solve biological problems. The most classical deterministic pairwise sequence alignment algorithms are the NW (Needleman-Wunsch) algorithm [2] based on global matching and the SW (Smith-Waterman) algorithm [3] based on local matching. Subsequently, a series of algorithms based on the above algorithms for parallel optimization [4-7], space complexity optimization [8-9], and backtracking strategy improvement [10] have been developed in domestic and international research. In addition, Garai et al. [11] proposed a new sequence alignment technique based on genetic algorithms that can achieve global or near-global optimal solution capability and obtained good performance; Rashed et al. [12] used FPGAs and custom convolutional neural networks to accelerate pairwise sequence alignment of DNA, which can achieve 98.3% accuracy; Song et al. [13] defined an environment and agent for implementing reinforcement learning in sequence alignment systems, and proposed a new method for pairwise sequence alignment that uses deep reinforcement learning to improve older pairwise sequence alignment algorithms.

The main focus of the above work is on the optimization of the pairwise sequence alignment algorithm, but the research on the reliability of the algorithm is missing, and the correctness of the algorithm cannot be guaranteed. The purpose of this paper is to propose an algorithm design method that can be applied to biological sequence analysis, using formal techniques to ensure the correctness of the algorithm, so as to solve the above-mentioned problems and finally generate an executable and highly reliable pairwise sequence alignment algorithm program. The formal method is based on a rigorous mathematical and mechanism approach to prove, verify, and evolve computational systems, and is an important method for improving and ensuring the quality of computational systems, which can effectively improve and guarantee the credibility of the systems. In recent years, many famous research institutions have invested a lot of human and material resources in the research of this area. For example, SpaceOS, an aerospace operating system independently developed by the Fifth Academy of China Aerospace Science and Technology Corporation, and HarmonyOS, Hongmeng operating system independently developed by Huawei, both use formal methods. Formal development is mainly to construct and prove the equivalence transformation and refinement relationship between formal statutes, and to develop a system that meets the needs by progressively refining the formal model of the system as a guide, which is also called correctness by construction [14]. The PAR method [15] provides the Radl language to write the statute and describe the algorithm, designs the rules for the statute transformation, and supports formal development. The formal derivation of algorithmic programs using the PAR method not only ensures the correctness of algorithmic programs logically, but also reveals the essential features of algorithmic program design.

In this paper, we use the PAR method to first analyze the dual sequence matching problem in depth, and then develop the recurrence relations and loop invariants for the solution of the problem by dividing the subproblem and formalizing the transformation of the statute. In order to ensure the reliability of the constructed pairwise sequence alignment algorithm, this paper formally proves the correctness of the Apla program, and then generates the executable program using the code generation system of PAR platform. In the verification process, it is tedious and error-prone to verify the correctness of the program manually using Dijkstra’s weakest pre-predicate method. Therefore, in this paper, the Isabelle theorem provers are
used instead of manual verification to overcome the drawbacks of manual verification and effectively improve the reliability of the constructed algorithm. In addition, the Apla program is easy to prove formally, and the code generation system of the executable program in PAR platform can guarantee the semantic consistency from the Apla program to the executable program. By verifying the correctness of the Apla program first and then generating the executable program from the Apla program according to the code generation system of the executable program in PAR platform, the verification work can be easier and the reliability of the algorithm can be guaranteed. In this paper, a classical algorithm in bioinformatics is used as an example to show the process of constructing the algorithm, and finally a highly reliable pairwise sequence alignment algorithm is generated. The work carried out in this paper can provide a valuable reference framework for the formal construction of complex algorithms in the field of bioinformatics.

2 RELATED WORK

The formal development method based on the formal specification language has been developed so far, and many methods have been formed, such as VDM [18], Z [19], Event-B [23] and Designware [24]. The theoretical basis of VDM is first-order logic and abstract data types, support data specificity and operation decomposition, etc. Similar to VDM, Z is also a specification language with refinement as the core, but neither support object-oriented software specification and refinement. To solve this problem, extended from these two methods VDM++[20] and Object-Z [21]. B [22] is a formal description language, which can also be used for formal proof. It is developed on the basis of VDM and Z methods. It is a relatively mature method. Event-B is a method that is refined and expanded based on method B. It has been used to develop many practical projects, and it has certain advantages in the development of large-scale projects. But Event-B uses abstract machine to describe the software development process, and it is too complicated to use it to develop algorithms. Designware is a system developed by professor DR Smith of the Kestrel Institute in the United States, which can realize the transformation development from the specification to the algorithm, but the requirements for users are too high.

In domestic and foreign research, there have been many works on formalized development of algorithms. For example, Bird et al. [25] used calculus of lists in the derivation process, and finally synthesized a very short functional program with a functional version of the Knuth-Morris-Pratt algorithm for pattern matching; JE Durán [26] proposed a transformation development method for efficient imperative network algorithms based on the Miller algebra of formal languages and derived the shortest path tree algorithm based on this method; Abrial et al. [27] designed and implemented the minimum spanning tree and Prim problem models using the Event-B method and transformed them into the corresponding solution algorithms; Almeida et al. [28] demonstrate three known sorting algorithms derived from a similar sequence of transformation steps from a general specification; Nedunuri et al. [29] transformed a naive algorithm into an efficient program by applying appropriate semantic-preserving transformations, and deduced three maximum segment sum problems; Mu et al. [30] construct a problem specification using equality reasoning the backtracking algorithm of n-queens. These existing works are mainly applied to general areas in combinatorics, but formal methods have not been applied to develop algorithms in the field of bioinformatics.

The PAR method based on partition and recursion technology covers all stages of algorithm development, and can clearly show the design process of the algorithm, which is very suitable for the construction of the algorithm, that is, the correct development. Before this, the works of literature [31, 32] used the PAR method to formally develop a series of algorithms for combinatorial mathematics problems, illustrating the feasibility of using the PAR method to develop related algorithms. Biological sequences and combinatorial mathematics are inextricably linked. Biological sequences include DNA, RNA, and biological macromolecular sequences. These can be regarded as sequence structures in combinatorial mathematics, so this paper applies the PAR method to formally develop algorithms in the field of bioinformatics.

3 FORMAL CONSTRUCTION METHOD OF PAIRWISE SEQUENCE MATCHING ALGORITHM

In this section, we first introduce the formal development method PAR used in this paper, and then use the PAR method to derive general recurrence relations for various penalty rules from the problem statute. In addition, the Apla program for the pairwise sequence alignment algorithm is constructed using a specific penalty rule as an example.

3.1 Overview of the PAR Approach

The PAR method is a simple and practical formal method for designing algorithms, which covers a variety of known algorithm design techniques and supports the whole process of algorithm program development [16]. The strategy of the PAR method to develop an algorithm is shown in Fig. 1. The specification in this paper adopts a unified quantifier representation \((Q_i : r(i) \land f(i))\), which means “the value obtained by performing the \(q\) operation corresponding to the quantifier \(Q\) on the function \(f(i)\) over the range \(r(i)\).” The quantifiers used in this article are MAX and \(\Sigma\), and the corresponding operations are max and +, which represent the maximum value and the sum, respectively. Using the properties of quantifiers, the specification can be equivalently transformed to expose the problem The idea of solving [15]. The properties used in this paper for specification refinement are given below:

1. Single range: \((Q_i : i = k : f(i)) = f(k)\)
2. Range splitting: \((Q_i : r(i) \land f(i)) = (Q_i : r(i) \land b(i) : f(i)) \land (Q_i : r(i) \land \neg b(i) : f(i))\)
3. Associative law of function: \((Q_i : r(i) \land f(i)) g(q(i)) = (Q_i : r(i) : f(i)) g(q) \land (Q_i : r(i) : g(i))\)
4. Disjunctive range: if \(a = a\), the operation \(q\) is said to be idempotent. For the idempotent operation \(q\), there is \((Q_i : r(i) \land s(i) \land f(i)) = (Q_i : r(i) \land f(i)) q (Q_i : s(i) \land f(i))\)
3.2 Formal Construction of Pairwise Sequence Alignment Algorithm

The natural language description of the pairwise sequence alignment problem is as follows: Given two sequences seq1 and seq2 of length m and n, respectively, elements in the sequence can be matched in three ways - match, mismatch, and space, respectively, indicates that two identical elements match, two different elements match, and one of the elements in the sequence matches a gap. Each matching method corresponds to a penalty, and there are many kinds of penalty rules; the most commonly used are two - for constant weight model and affine penalty model, different penalty rules correspond to different sequence similarity evaluation criteria. To better demonstrate the construction process, this paper uses the simplest penalty rules, as shown below:

3.2.1 Problem Specification

The natural language description of the pairwise sequence alignment problem is as follows: Given two sequences seq1 and seq2 of length m and n, respectively, elements in the sequence can be matched in three ways - match, mismatch, and space, respectively, indicates that two identical elements match, two different elements match, and one of the elements in the sequence matches a gap. Each matching method corresponds to a penalty, and there are many kinds of penalty rules, the most commonly used are two - for constant weight model and affine penalty model, different penalty rules correspond to different sequence similarity evaluation criteria. To better demonstrate the construction process, this paper uses the simplest penalty rules, as shown below:

\[
\begin{align*}
\text{match} &= 1 \\
\text{mismatch} &= -1 \\
\text{space} &= -2
\end{align*}
\]

(1)

Starting from the first element of the two sequences and matching from front to back, until all the elements of the two sequences are matched, it is an alignment, and the alignment score is the sum of the corresponding penalty points for each element matching. The goal is to obtain the largest alignment score from all possible alignments, thereby assessing the similarity between sequences.

A coordinate in the form of \((i, j)\) is used to represent the current matching position, \(i\) represents the matched length of seq1, and \(j\) represents the matched length of seq2.

A quaternion sequence is used to represent an element match, two different elements match, and one of the elements in the sequence matches a gap. Each matching method corresponds to a penalty, and there are many kinds of penalty rules; the most commonly used are two - for constant weight model and affine penalty model, different penalty rules correspond to different sequence similarity evaluation criteria. To better demonstrate the construction process, this paper uses the simplest penalty rules, as shown below:

3.2.2 Search for Recursion Relation

According to the definition of align\((i, j)\), it can be concluded that the last element of align\((i, j)\) is \([i-1, j, i, j]\) or \([i, j-1, i, j]\) or \([i-1, j-1, i, j]\), which means align\((i, j)\) = align\((i-1, j)\) ∪ \([i-1, i, j, j]\) \(∪\) align\((i, j-1)\) ∪ \([i, i-1, i, j]\) \(∪\) align\((i-1, j-1)\) \(∪\) \([i-1, j-1, i, j]\). Use score\((cs)\) instead of \((\Sigma sgl : sgl \in cs : rule(sgl))\), consider the general case:

\[
\begin{align*}
\text{maxScore}(i, j) &= (\text{MAX } cs : cs = \text{align}(i, j) : \text{score}(cs)) \\
&= (\text{MAX } cs : (cs = \text{align}(i-1, j) \cup \{i-1, i, j, j\}) \; \lor \; (cs = \text{align}(i, j-1) \cup \{i, i-1, i, j\}) \; \lor \; (cs = \text{align}(i-1, j-1) \cup \{i-1, j-1, i, j\}) : \text{score}(cs))
\end{align*}
\]
The definition of rule can be simplified as follows: 

\[ \text{maxScore}(i, j) = \max \{ \text{maxScore}(i-1, j) + \text{space}, \text{maxScore}(i, j-1) + \text{rule}(i, j) \} \]

(5)

Considering the special value, when \( i \) and \( j \) are both 0, it means that two empty sequences are aligned, obviously \( \text{maxScore}(0, 0) = 0 \); when one of \( i \) and \( j \) is 0 and the other is not 0, it means a sequence that is not empty is aligned with another empty sequence, there is only one case, that is, every element in the sequence which is not empty matches the gap, \( \text{maxScore}(i, 0) = \text{space} \times i \), \( \text{maxScore}(0, j) = \text{space} \times j \). From this, the recurrence relation can be obtained:

\[ \text{maxScore}(i, j) = \begin{cases} 
0, & i = 0 \land j = 0 \\
\text{space} \times i, & i \neq 0 \land j = 0 \\
\text{Eq. (5)}, & i \neq 0 \land j \neq 0
\end{cases} \]

(6)

According to the recurrence relation of the specified specific penalty rules, the following Radl algorithm is constructed to solve the pairwise sequence alignment problem:

**ALGORITHM: pairwiseAlignment**

\[
[\text{Var score: array}(0..m, \text{array}(0..n, \text{integer})); \text{seq1}: \text{array}(0..m, \text{char}); \text{seq2}: \text{array}(0..n, \text{char}); i, j: \text{integer}];
\{AQ \land AR\}
\]

BEGIN: \( i = 0 \Rightarrow \); \( j = 0 \Leftarrow \);
TERMINATION: \( i = m \land j = n \);
RECUR: Eq. (6);
END.

### 3.2.3 Develop Cycle Invariants

Reference [33] gives a new definition of loop invariant, that is, the predicate that reflects the variation law of all loop variables in the loop body and is true before and after the loop body is executed is called the loop invariant of the loop body. Among them, the loop variable is defined as the variable in the loop body whose value changes continuously as the loop body executes.

From the obtained Radl algorithm, it is not difficult to see that the algorithm has two layers of loops, the variable \( i \) controls the outer loop, the variable \( j \) controls the inner loop, and each loop corresponds to a different loop invariant. Use \( ms \) to store \( \text{maxScore}(i, j) \) value, then all the variables in the loop are \( i, j \) and \( ms \). First analyze the outer loop, the variables that change with the execution of the loop body are \( i \) and \( ms \), and the variable \( j \) has nothing to do with the outer loop, because no matter the outer loop executes at which step, the value of the variable \( j \) before the outer loop body is executed is 0. The value of the loop variable \( ms \) is always \( (\text{MAX cs} : \text{cs} = \text{align}(i, j) : \text{score}(cs)) \), and the range of the loop variable \( i \) is \([0, m]\). According to the change rule of the loop variable, it can be accurately
expressed by the predicate, that is, the loop invariant of the outer loop is obtained:

\[ ms = \text{maxScore}(i, j) = (\text{MAX } cs : cs = \text{align}(i, j) : \text{score}(cs)) \land (0 \leq i \leq m) \]

Then again, by analogy with the outer loop, the loop invariant of the inner loop can be obtained:

\[ ms = \text{maxScore}(i, j) = (\text{MAX } cs : cs = \text{align}(i, j) : \text{score}(cs)) \land (0 \leq j \leq n) \]

### 3.2.4 Synthesis Algorithm Program

According to the obtained recursion relationship, Radl algorithm, and loop invariant, the Apla abstract algorithm program can be easily obtained. Due to space limitations, only the Apla codes of the three main functions are given here. The main codes of the comparison algorithm are as follows:

```plaintext
function rule(var i, j : integer) : integer;
begin
if seq1[i] = seq2[j] → rule := match;
[] seq1[i] ≠ seq2[j] → rule := nmatch;
fi;
end;
function matching(var i, j : integer) : integer;
begin
if (i = 0) ∧ (j = 0) → matching := 0;
[] (i = 0) ∧ (j ≠ 0) → matching := space * j;
[] (j = 0) ∧ (i ≠ 0) → matching := space * i;
[] (i ≠ 0) ∧ (j ≠ 0) →
matching := max(score[i-1, j] + space, \[max(score[i, j-1] + space, score[i-1, j-1] + rule(i-1, j-1))\]);
fi;
end;
procedure maxScore();
var
i, j : integer;
begin
i := 0;
do i ≤ m →
j := 0;
do j ≤ n →
score[i,j] := matching(i,j);
j := j + 1;
od;
i := i + 1;
od;
end;
```

The maximum alignment score can be calculated by calling the maxScore procedure, and the maximum alignment score is score \([m, n]\).

### 4 AUTOMATIC VERIFICATION AND GENERATION OF PAIRWISE SEQUENCE ALIGNMENT ALGORITHM

Based on the previously obtained Apla algorithm for pairwise sequence alignment, this section verifies it formally. After verifying its correctness, Apla is then generated into an executable program using the program generation system of PAR platform.

#### 4.1 Automated Verification of Pairwise Sequence Alignment Algorithms

Constructing a correct program requires mathematical proof [34], because program testing can effectively find the existence of bugs, but it cannot show that there are no bugs in the program. Therefore, to ensure that the above program is completely correct, it needs to be formally verified. In addition, through the program's correctness proof, the understanding of the program can also be deepened. In this paper, Dijkstra's weakest pre-predicate method is used, and the Isabelle theorem prover is used to prove the correctness of the obtained Apla program.

#### 4.1.1 Automated Verification Strategy

Based on the obtained recurrence relation and loop invariant, the correctness of the Apla abstract algorithm program can be verified. There are many ways to prove the correctness of the program, because the Floyd inductive assertion method [36] and the Hoare axiom system method [37] are very difficult to write appropriate intermediate assertions, and Dijkstra's weakest pre-predicate method is defined by the weakest pre-predicate \(WP\) to write intermediate assertions [34, 35], which is more practical. Use \(S\) for statements and \(R\) for post-assertion of \(S\). Then the execution of \(S\) starts from any state and must terminate within a finite time, and the termination state satisfies \(R\). The predicate \(WP(\text{"}S\text{"}, R)\) represents the set of these states and is called the weakest pre-predicate. Therefore, this paper chooses Dijkstra’s weakest pre-predicate method to prove the correctness of the Apla program. Dijkstra’s weakest pre-predicate method to prove the correctness of the loop statement needs to meet five conditions:

1. \(Q \Rightarrow \rho\);
2. \(\rho \land C_i \Rightarrow WP(\text{"}S_i\text{"}, \rho)\), \(1 \leq i \leq n\);
3. \(\rho \land \neg \text{Guard} \Rightarrow R\);
4. \(\rho \land \text{Guard} \Rightarrow \tau > 0\);
5. \(\rho \land C_i \Rightarrow WP(\text{"}\tau_i := \tau; S_i\text{"}, \tau_i < \tau)\), \(1 \leq i \leq n\).

Among them, \(Q\) is the pre-predicate, \(R\) is the post-predicate, \(\rho\) is the loop invariant, \(\tau\) is the bound function, \(C_i\) and \(S_i\) are the loop conditional branch statement and its corresponding loop body respectively, Guard is the disjunction of all branches \(C_i\).

Input the conditions of the proving program into Isabelle in Isabelle’s grammar and prove it using the automatic proof strategy it provides.

#### 4.1.2 Verification Process

Create a new theory seqalign for the formal proof of the Apla program in this article. The theory name needs to be consistent with the file name. Since the Main theory contains the list type used in this article, it is only necessary to use import to import the Main parent theory. The recurrence relation for maxScore and the rule function used are translated into the language used in Isabelle, as shown in Fig. 2.

The main body of the pairwise sequence alignment algorithm program constructed in this paper is a double-layer loop. The recurrence relation and penalty rules in the loop are strictly derived, so it is only necessary to prove the correctness of the double-layer loop. To prove the five
Theorems of the loop statement in Dijkstra's weakest pre-predicate method, finding the loop invariant \( I \) and the bound function \( r \) of the loop statement is the key. The loop invariant in the Apla program has been solved in Section 2. In addition, it is obvious that the bound functions corresponding to the double-layer loop can be \( m - i + 1 \) and \( n - j + 1 \) respectively. The values of the parts of the theorem are substituted into them, expressed in the syntax of Isabelle, and entered into the created seqalign theory, and are expressed as follows:

\[
\begin{align*}
\text{for } i = 1 \text{ to } m - 1 \\
\text{and } j = 1 \text{ to } n - 1.
\end{align*}
\]

In addition, it is obvious that the bound functions corresponding to the double-layer loop can be \( m - i + 1 \) and \( n - j + 1 \) respectively. The values of the parts of the theorem are substituted into them, expressed in the syntax of Isabelle, and entered into the created seqalign theory, and are expressed as follows:

\[
\begin{align*}
\text{for } i = 1 \text{ to } m - 1 \\
\text{and } j = 1 \text{ to } n - 1.
\end{align*}
\]

Isabelle is given below, as in Fig. 3.

The above five lemmas can be automatically verified directly by the auto strategy. Add apply auto after each lemma, and the proof state as shown in Fig. 4 has all changed to "No subgoals!", indicating that the theorem is proved to be correct. Finally, end with done the proof of each lemma. Since the proof of the inner loop is the same as the proof of the outer loop, there is no proof statement for the inner loop. The above proof shows that the loop invariant is before and after the loop execution and the loop body. All are true, and the Apla program finally generated in this article is indeed correct.

4.2 Executable Program Generation

The pairwise sequence alignment algorithm is formally constructed and its correctness is verified. Based on the previous algorithm, we show the generation effect of the algorithm through the Apla -> C++ program generation system on the PAR platform.

To facilitate the viewing of the best alignment method, based on the Apla program of the aforementioned pairwise sequence alignment algorithm, we store the matching of each step of the best alignment method and add the process of outputting the best alignment method. When calculating the maximum alignment score for coordinates \((i, j)\), the coordinates before the last match are determined. Therefore, if you want to get the best alignment, you only need to save the last match when calculating the maximum score for each coordinate. Here, a two-dimensional array path is used to save it. The value range of the elements in the array is \([0, 1, 2, 3]\). The above four values for path \([i, j]\) represent the initial state of the comparison, seq2 \([i]\) and Gap matching, seq1 \([i]\) and gap matching, and seq2 \([i]\) match or mismatch. Therefore, the matching function can be changed as follows:

\[
\text{function matching}(\text{var } i, j : \text{integer}) : \text{integer};
\]

\[
\begin{align*}
\text{begin} \\
\text{if } (i = 0) \land (j = 0) \rightarrow \text{path}[i, j] := 0; \\
\text{matching} := 0; \\
\text{space} := 1; \\
\text{if } (i = 0) \land (j = 0) \rightarrow \text{path}[i, j] := 1; \\
\text{matching} := 0; \\
\text{space} := 1; \\
\text{if } (i = 0) \land (j = 0) \rightarrow \text{path}[i, j] := 2; \\
\text{matching} := 0; \\
\text{space} := 1; \\
\text{end;}
\end{align*}
\]

After determining the value of the path array, traverse forward from the coordinates \((n, n)\) until the initial state of the comparison, and store each matching method into the stack, and finally the best alignment method can be obtained by outputting the top elements of the stack in turn. Due to space limitations, the code of the output process is omitted here.

4.3 Pairwise Sequence Alignment Algorithm C++ program running result

For the following two sequences:

\[
\begin{align*}
\text{CGGACCCCTCAGGGCCCGAGGGTC} \\
\text{CGGACCACCTGCTCAAGAGT}
\end{align*}
\]

The max score is 6.
The two sequences involved in the matching are read from the text, and then the results of the pairwise sequence alignment are output to the text file where, "#" means empty space. For the sake of space, only a simple example of the C++ program is given here, as shown in Fig. 5.

```cpp
int rule(const Int B1, const Int B2) {
    int ReturnValue;
    if (seq1[i] == seq2[i]) {
        ReturnValue = match;
    } else if (seq1[i] != seq2[i]) {
        ReturnValue = mismatch;
    }
    return (ReturnValue);
}
```

Figure 6 Generated C++ code for the rule and matching functions

5 CONCLUSION

In this paper, based on the PAR method, we adopt the formal method to obtain the recurrence relation for the general case from the Radl formal specification of the pairwise sequence alignment problem in biological sequence analysis. The special case is analyzed, and the Apla algorithm is obtained by adding a recursive condition to the recursive formula. Further, the correctness of the pairwise sequence alignment algorithm generated in this paper is ensured by the verification of theorem prover Isabelle. Finally, the C++ program generation system of PAR platform is used to generate the executable code from the Apla program.

The main contributions of this paper are as follows:

1. This paper uses the PAR method to start from the problem specification, constructs a pairwise sequence alignment algorithm in biological sequence analysis, formally proves the correctness of the constructed algorithm, and finally generates an executable program, which effectively guarantees its high trustworthiness.

2. This construction method demonstrates the amazing idea of the algorithm, and also shows the clear logic behind this idea. The work in this paper not only shows the design idea of the pairwise sequence alignment algorithm, but also adds special case values to the recurrence relations derived in the general case, which brings great convenience to generate the algorithm program and makes the design of the algorithm easier.

3. The formal method is applied in the field of bioinformatics. As an instance, a pairwise sequence alignment algorithm is successfully constructed, which illustrates the effectiveness and practicability of the method.

4. In the field of sequence analysis in bioinformatics, many problems are similar and sequences have many common features, so the work in this paper can provide an example for the formal construction of typical algorithms in the field of complex bioinformatics.

An important idea of the PAR approach is to convert as much creative work as possible into non-creative work, so that the otherwise difficult process of algorithm design becomes a step-by-step task. In this paper, the algorithm is constructed with the help of the PAR platform C++ program generation system and theorem prover Isabelle, which minimizes manual work. The next step is to further investigate methods for generating Apla programs from recursive relations and loop invariants, and to transform more creative work in the construction of algorithms into mechanical work. What's more, we will work on establishing the specification library. By putting some common types and operations into the specification library, the establishment of the specification and the derivation of the recursive relation can be made more convenient.

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