ISOBARIC SPIN IN PHOTONUCLEAR REACTIONS

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Abstract: **Present evidcnce for isobaric spin splitting of thc photonuclcar giant dipole resonancc is discussed on some examples. In particular, it is shown that the experiments on** *11***B are inconclusive.**

For ^{*}Zr the ratio of integrated cross sections for the two isospin components is predicted, together with the corresponding ratio for some reaction chan**nels.**

1. Introduction

It is generally believed that the photonuclear reactions provide a good tool **for the invcstigation of the isobaric analogue states in the continuum at** excitations between 10 and 30 MeV. This is because the photonuclear giant **rcsonance is almost entirely due to electric dipole transitions implying an** isobaric spin selection rule $\Delta T = 0$ or 1 (no $T = 0$ to $T = 0$ transitions). How**cver, it turns out that it is not easy to distinguish expcrimcntally thc two types of states, neither is the reaction mechanism well understood.**

In what follows, some basic features concerning the isobaric spin compo· sition of thc photonuclear giant resonance will be discussed, and a few typical experimental examples will be shown for thc purposc of illustration.

2. The energy difference between the centroids o/ thc two types of isobaric spin excitations

Wc shall bc considcring only non-self-conjugate nuclei with isobaric spin of the ground state equal to $T_0 = T_z$. Accordingly, there will be two types of

dipole excitations $T_a = T_0$ *and* $T_a = T_0 + 1$ *. As it is known, a low symmetry of the isobaric-spin wave function is connected with a high symmetry of the spac\! and spin wavc functions, and vicc versa (Hund's rulc). A high symmctry of thc spacc-spin function means that nuclcons comc in average closer to each othcr than in the case of low symmetry. Duc to the attractive eha· ractcr of the nuclear forces one therefore expects thc states of higher T to be located at a higher energy as compared to the states of lower T (for atoms the effcct on energy is just the opposite due to th\! repulsion of Coulomb forces). Empirically this effect results in the symmctry term ot the Weiz·* sücker mass formula. Formally the symmetry effect in one nucleon excitations *can bc incorporated in the Hamiltonian by introducing the Lane term*

$$
\frac{\overrightarrow{4tT}U_4}{A}
$$
,

which was originally used for the charge exchange scattering, where \overrightarrow{T} and \overrightarrow{t} are the isobaric spin operators for the target nucleus and the projectile, *respcctively. For the energy difference between thc two types of states one obtains*

$$
E(T_{\star}) - E(T_{\star}) = \frac{4 U_1}{A} \langle \langle T_{\star} | \vec{T} \vec{T} | T_{\star} \rangle -
$$

$$
-\langle T_{\star} | \vec{T} \vec{T} | T_{\star} \rangle = \frac{4 U_1}{A} (T^{\star} + 1).
$$
 (1)

It is convcnicnt to express the above value with thc differcnce in the nuclear intcraction U of a neutron and an equivalent proton with the nuclcus:

$$
U = \langle nA \mid \frac{4\overrightarrow{i} \overrightarrow{T}}{A} U_1 \mid nA \rangle - \langle pC \mid \frac{4\overrightarrow{i} \overrightarrow{T}}{A} U_1 \mid pC \rangle = T \Big| \frac{4 U_1}{A} \Big| \tag{2}
$$

Finally, wc obtain:

$$
E(T_{\star}) - E(T_{\star}) = \frac{T_{\star} + 1}{T_{\star}} U.
$$
 (3)

Abovc, notation used for the study of chargc exchangc scattering has been adoptcd, I *pC) dcnoting the state of the proton plus the targct nucleus, and I nA > a neutron plus the analogue state of the residual nucleus.*

3. The relative strengths of the two isobaric-spin components

We write the photonuclear absorption cross section for the E1 radiation in the form (Thompson scattering not included):

$$
\sigma_{on}(E1) = \frac{16 \pi^3}{9} \frac{1}{137} (E_n - E_0 \mid \langle \psi_n \mid \mid \sum_{i=1}^4 e_i r_i Y^i (i) \mid \mid \psi_0 \rangle \mid^2
$$
 (4)

where the reduction of the matrix element applies only to the space and spin coordinates. The notation $e_i = \frac{N}{A}$ for protons and $e_i = -\frac{Z}{A}$ for neutrons is used. The transition matrix element can be divided into an isoscalar and an isovector part. The isovector part reads*

$$
\langle \psi_n \mid \sum_i \tau_3(i) \ r_i Y^1(i) \mid \psi_0 \rangle. \tag{5}
$$

Considering the T_{\bullet} and T_{\bullet} components being separated, one obtains

$$
\frac{\left| \langle T_0 + 1 \rangle \sum_i \tau_3(i) r_i Y^{\dagger}(i) | T_0 \rangle \right|^2}{\left| \langle T_0 | \sum_i \tau_3(i) r_i Y^{\dagger}(i) | T_0 \rangle \right|^2} =
$$

$$
\frac{\left(T_0 + 1 \frac{1}{2} T_0 \right)^2}{\left(-T_0 \frac{1}{2} T_0 \right)^2} \frac{\left| \langle T_0 + 1 \rangle \right| \sum_i \tau_3(i) r_i Y^{\dagger}(i) | T_0 \rangle|^2}{\left| \langle T_0 | \sum_i \tau_3(i) r_i Y^{\dagger}(i) | T_0 \rangle \right|^2}
$$
(6)

with

$$
\frac{\begin{pmatrix} T_0 + 1 & 1 & T_0 \\ -T_0 & 0 & T_0 \end{pmatrix}^2}{\begin{pmatrix} T_0 & 1 & T_0 \\ -T_0 & 0 & T_0 \end{pmatrix}^2} = \frac{1}{T_0}.
$$
 (7)

The ratio of the reduced matrix elements

$$
\frac{|\langle T_0 + 1 \parallel \sum_{i} \tau_3(i) r_i Y^1(i) \parallel T_0 \rangle|^2}{\|\langle T_0 \parallel \sum_{i} \tau_3(i) r_i Y^1(i) \parallel T_0 \rangle|^2}
$$
 (8)

^{*} As it will be shown later in the discussion of the nucleus %Zr, the scalar term is considerably smaller.

is model dependent and is expected to vary from 1 (for $T_z = 0$ *) to about 1 ¹⁵⁰(for 20�Pb)'>.*

In a single particlc shell model picture one would expect the ratio of thc transition matrix elemcnts (6) to be equal to zero in a sclfconjugate nuclcus, since no $T = 0$ *to* $T = 0$ *transitions are allowed. On the contrary, in the case*

Fig. 1. Types of single particle dipole excitations. States a) and b) have pure T. isospin, while states c) and d) have mixed isospins T_0 and $T_0 + 1$. For instance, the *state c) can be written as*

$$
\left(\frac{2T_0+1}{2T_0+2}\right)^{1/2} |T_0,T_0\rangle + \left(\frac{1}{2T_0+2}\right)^{1/2} |T_0+1,T_0\rangle.
$$

of ²⁰³Pb there would be no $T_0 = T_0 + 1$ transitions (neglecting the ones in*volving 3 h* ω *)* due to the fact that the excess neutrons in the ²⁰⁵Pb ground *slate completely fili one of the harmonic oscillator lcvels. Therefore, ali dipolc cxcitations are of thc typc a) and b) of Fig. 1, involving only the isobaric spin* $T_{\text{c}} = T_0$. By the above model only a quantitative understanding is provided. *For more rcliable estimates one should use more realistic wave functions.*

4. Experimental evidence

¹'B. — Some experiments have been performed recently with the aim to mcasurc the isospin splitting of the giant dipole resonance in ¹¹B², ³). The ex*pcrimcnts involve thc dctcction of gamma rays emitted after thc photodisinlegration of* **11***B. An apparently negative result***²** *> concerning the existencc of* the T_r component of the giant resonance was discussed by Hayward et al.⁴ *and the experimental data were shown to be inconclusive.*

Patrick et al.3> measured deexcitation gamma rays with a better prccision at S different bremsstrahlung end-point energies, and were able to extract a rough energy dependence of the cross sections to three individual excited

statcs of rcsidual nuclei 1°Be and **10***B. The states involvcd are Lhc 3.59 McV* $(J^{\frac{\pi}{2}} - 2^+, T = 0)$ and the 5.17 MeV $(J^{\frac{\pi}{2}} - 2^+, T = 1)$ states in ¹³B, and the 3.37 *MeV* $(J = 2^+, T = 1)$ state in ¹⁰*Bc* (Figs. 2 and 3). According to the authors, *their cxperimental data show that thc giant dipole resonance of* ¹¹*B consists*

Fig. 2. The energy and decay scheme for the reactions ^{<i>i}B (γ, ^{*•}•* γ') involved in the</sup> *experiment of Ref.3>. Figures shown along with thc particle emission lines cqual to the square of coupling coefficients.*

mainly of $T = \frac{1}{2}$ states in the lower energy region and of $T = \frac{3}{2}$ states in *the higher energy region.*

Isospin conservation implies that the $T = 0$ state of ¹⁰B can only be populated from the $T_z = \frac{1}{2}$ component of the giant resonance. From the coupling *coefficients (see Fig. 2) we expect the* $T_> = \frac{3}{2}$ component to populate the

 $T = 1$ ¹⁰B state to a larger extent than the $T = 1$ ¹⁰Be state. In this way one *could justify the comparison only betwccn the partial cross scctions to thc two* ¹⁰**B** states for the purpose of estimation of the extent to which the ¹¹*B giant rcsonance is divided mto two rcgions of different isospin, as it was done by the authors of Ref.*³, It should also be kept in mind that the $T = 1$ *statcs can be populated from the T* **<** *component as well. Therefore a unique* conclusion about the location of the T_s resonance cannot strictly be obtained *from such an experiment.*

The interpretation of Ref.³, according to which the giant resonance is *dividcd into two fairly separate isospin componcnts, is based on the assumr· tion that the T_{_} component should be restricted to the energy region below* about 20 MeV, and the T_s component to the region above this energy. How*evcr, this assumption is by no way justified.*

It is possible to construct a fairly good picture of the total photoabsorp· tion cross section for the nucleus 11*B from the known experimental cross* sections $\sigma(\gamma, p_{\text{total}})^{5}$ and $\sigma(\gamma, n) + \sigma(\gamma, np) + 2 \sigma(\gamma, 2 n)^{6}$ (Fig. 3). It is seen *from Fig. 3 that thcre is practically no radiation strength left for the cnergy rcgion below 20 MeV. The centre of gravity of the giant rcsonancc* $\int E \sigma_{\gamma}$ abs $\int E \int \sigma_{\gamma}$, abs de lies in the vicinity of 25 MeV. We note that the *calculation of Spicer and Fraser***⁷** *>, to which the data of Ref.*31 *werc comparcd, yields an incorrect value of* 21 *MeV for the centre of gravity of thc giant rcsonance in* **11s.**

From the preceding discussion we cxpcct the ratio of the intcgratcd ab· sorption cross sections for the T_{S} and the T_{S} component to have a value of *about 2 or less.*. Without affccting the argumcnts which follow, one can* afford to be fairly generous, and allow any value between $\frac{1}{2}$ and 2 for the ratio of the two integrated cross sections, (theory^{*n*} predicts a value of 1.2 for the ratio of the integrated T_s to the integrated T_s cross section).

In Fig. 3 the absorption cross section for **¹ ¹***B is, for the sake of simplicitv, divided by two vertical lines into three cnergy rcgions of equal intcgratcd cross scctions. Assuming thc two isospin components being scparated wc /ind that the Iower vertical line at 23 MeV would represent the separation linc between the components* T_a *and* T_a *in the case that a value of 2 were taken for the ratio* $R = \int \sigma_{r_a} dE / \int \sigma_{r_c} dE$. For the other limiting case $R = \frac{1}{2}$, the separation line would move to 26.5 MeV. In other words, we can *say that if lhe* **¹ ¹***B giant resonancc were dividcd into hvo separate isospin componcnts, thc scparation !ine would Iic somewhere in the encrgy interval 23 - 26.S MeV, unless the ratio R is far larger from the one expected.*

^{*} There is an indication from the experiments on $^{26}Mg^{8,9,10}$ that the above ratio may be larger than $1/T_0$ for the nuclei with low T_1 . However, this would not alter *thc inconclusiveness of the present experimental data for HB.*

Fig. 3. The upper diagram shows the photoneutron and photoproton cross sections together with the sum of both. The cross sections to three different states of the residual nuclei (lower diagrams) are taken from Ref.³). The vertical lines are drawn so as to separate the summed cross section into three cnergy regions of equal **b integrated cross sections.**

It is seen from Fig. 3 and numerically from Table 1 that the ratio of inte· grated cross sections for the 5.17 MeV state and for the 3.58 McV state is about the same in the higher energy region as in the lower energy region, if

the energy which separates the two regions lies in the interval between 23 MeV and 26.5 MeV.

*We, thcrcfore, concludc that within the limits of thc cxpcrimcntal accuracy of Ref.***³** *i thcrc is no cvidcncc for an isospin splitting in the giant resonancc of* **¹¹***B*. On thc contrary, the experimental results suggest a unitorm distri· hution of the T₂ and T₂ <i>radiation strengths over the giant resonance region.* The latter interpretation should be taken with caution as far as the T_c com-*,poncnt is conccrned, since it is not clear how much is thc cross section to the 5.17 MeV (T = 1)* ¹⁰B state affected by the transitions from the T_{\perp} isospin *component of thc giant resonance in* **11***B.*

Table 1

Ratio of integrated cross sections for the states of ¹⁰B with isospin $T = 0$ *and* $T = 1$, in the lower and the higher energy regions

Assumed ratio of integrated photoab- sorption cross sec- tions for the two isospin components	Position of the line of separation, defi- the »lower« ning »higher« the and energy regions	Integrated cross section to the 5.17 MeV $(T=1)$ state Ratio of Integrated cross section to the 3.58 MeV $(T=0)$ state	
$R = \frac{\int \sigma_{r_{\infty}} dE \gamma}{\int \sigma_{r_{\infty}} dE \gamma}$		»Lower« energy region	»Higher« energy region
	23.0 MeV	$1.6 \pm 0.4***$	2.1 ± 0.8
	26.5 MeV	$2.2 + 0.5$	$17 + 0.9$

*MMg. - The isobaric-spin splitting of the photonuclcar giant resonance is dearly dcmonstratcd in the experiment of Wu, Firk and Berman***⁶** *1. fhey stu· died the energy spectra of neutrons resulting from the irradiation of 26Mg with bremsstrahlung gamma rays of two different end-point cnergies. The two isobaric-spin components of the giant dipole resonance have* $T = 1$ and $T_> = 2$. The $T_> = 2$ component cannot decay to the $T = \frac{1}{2}$ ground state *of* ²⁵*Mg* while it can decay to $T = \frac{3}{2}$ states at 7.8 MeV (Fig. 4). In the energy *spectrurn of ncutrons irradiated with the bremsstrahlung of an end-point cnergy o[23.l McV is the upper peak of the giant resonance missing, indi*cating the absence of neutrons decaying from the states above 19 MeV and

^{} Wc nate that considcration of the cross scction to thc 3.37 McV (T = I) '"Bc stale would not affect thc above conclusion.*

*^{**} The errors were obtained from the typical values quoted in Ref.* **¹** *1.*

leaving the residual nucleus ^{25}Mg in its ground state. In fact, the high energy part of the neutron spectrum is similar to the one obtained with an end-point energy of 18.9 MeV. From the difference of the low-energy parts the contribution of neutrons decaying to the $T = \frac{3}{2}$ states of ²⁵Mg is deduced. The difference spectrum seems to agree with the $(\gamma, n)^{9}$ and $(e, e')^{11}$ results.

A relatively large $(\gamma, 2n)$ cross section¹⁰ confirms the experimental results of Wu et al. The $T_{-} = 2$ state of ²⁶Mg decays also into the continuum $T = \frac{3}{2}$ states of ²⁵Mg which in turn decay either through the emission of another neutron into $T = 0$ ²⁴Mg states (violating the isospin selection rule) or through gamma emission into lower states of ²⁵Mg.

Fig. 4. The energy level diagram shows the location of dipole states in "Mg. The results of an (e, e') experiment" are also shown. The energy spectra of photoneutrons are plotted for two different bremsstrahlung end-point

 ^{90}Zr . — Theoretical studies^{t, 12-15} are mainly dealing with the total strength of the two types of isobaric dipole excitations and their energy splitting, while experimentally¹⁶⁻¹⁹ one obtains a sum of cross sections for a few reaction channels only. It is important to study the cross sections for individual reaction channels independently, since they often show a selectivity with respect to the isobaric spin.

At present good experimental data exist for the (γ, n) , $(\gamma, 2n)^{16}$ and (p, n) γ_0 ^{18, 11}) cross sections. Data for other proton channels and the (γ, np) reaction

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are in the process of evaluation^{19, 20}. The (γ, n) cross section consists of a resonance peaking at about 16.5 MeV and some structure at 21 MeV (Fig. 5). The latter is sometimes interpreted as the T_s component of the giant resonance.

Besides the known T_s resonances in the (p, γ_0) reaction²¹ at energies $E_x = 14.4$ and 16.3 MeV there is also some evidence for T, states at excitation energies of about 21 MeV^{18, 17}. However, the ratio R(γ , p_0) = $\int \sigma_{\gamma, p_0} (T) dE$ / $\int \int \sigma_{\sqrt{n}}(T_{\prec}) dE$ is much smaller than $\frac{1}{T_{\rho}}$.

A simplified treatment of the dipole excitations in the nucleus ${}^{\infty}Zr$ will be given here. For convenience protons and neutrons in doubly unoccupied levels

Fig. 5. The energy level diagram for the photonuclear reactions on ${}^{\infty}Zr$. The (γ, ν) cross sections are taken from Ref.¹⁹. The (γ, p_0) cross section is obtained through detailed balance from the inverse reactio

and proton and neutron holes in doubly occupied subshells (i. c. excitations of c-d type of Fig. 1) will be expressed in terms of isoscalar $|s\rangle$ and isovector $|v\rangle$ functions¹⁴⁾

$$
|s\rangle = \frac{1}{\sqrt{2}} (|n^{-1}n\rangle - |p^{-1}p\rangle),
$$

\n
$$
|v\rangle = \frac{1}{\sqrt{2}} (|n^{-1}n\rangle + |p^{-1}p\rangle),
$$

\n
$$
|n^{-1}n\rangle = \frac{1}{\sqrt{2}} (|v\rangle + |s\rangle),
$$

\n
$$
|p^{-1}p\rangle = \frac{1}{\sqrt{2}} (|v\rangle - |s\rangle).
$$

\n(10)

Dipole cxcitations of the c-d type can be written using (4) and (10) as

$$
\left(\frac{N}{A}\left|p^{-1}p\right\rangle+\left|-\frac{Z}{A}\right|\left|n^{-1}n\right\rangle\right|\psi_0\rangle=\left(\left|v\right\rangle-\frac{2\,T_0}{A}\left|s\right\rangle\right)\left|\psi_0\rangle\,,\tag{11}
$$

where ψ_0 stands for the ground state. The c-d type states can be treated separately since they are orthogonal to the states of the a-b type. Expressing the *above product functions in terms of eigenfunctions of total isobaric spin, one obtains*

$$
|\nu\rangle |\psi_0\rangle = \rangle \left(\frac{1}{T_0 + 1}\right)^{\frac{1}{\tau}} |T_0 + 1, T_0\rangle = \frac{T_0}{T_0 + 1}^{\frac{1}{\tau}} |T_0, T_0\rangle
$$
\n(12)

$$
\frac{2 T_0}{A} |s\rangle |\psi_0\rangle = \rangle \frac{2 T_0}{A} |T_1, T_0\rangle.
$$

We neglect the dipole strength contribution due to thc scalar function {sccond line of expressions (12)) which amounts to only about 1⁰/₀ (note the orthogonality of $|s\rangle$ and $|v\rangle$).

Consequently, one finds that for excitations of types c-d (see Fig. 1) there will be a value of 1 to T_0 for the ratio of $T_0 + 1$ to the T_0 dipole strength. It *·should be notcd that for* **⁹⁰***Zr, thc sum of dipole matrix elements of types* a-b (having isobaric spin T_0 only) is slightly greater than the corresponding sum for excitations of types c-d (see e.g.¹⁴) for ⁸³Sr), yielding a value of ≈ 0.08 for the overall ratio of the $T_0 + 1$ to the T_0 dipole strength. For the corresponding ratio of integrated cross sections one obtains $R = \int \sigma(T) dE /$ $\int \int \sigma$ (T₋) dE \approx 0.10.

108 KERNEL

Before proceeding to the treatment of individua! reaction channels we writc the ralio of integrated cross sections for the hvo isospin components in tcrms of partial widths

$$
R(\gamma, p_i) = \frac{\int \sigma^* (\gamma, p_i) dE}{\int \sigma^*(\gamma, p_i) dE} = \frac{\int \sigma_i (T_*) dE \cdot \frac{\Gamma^* n}{\Gamma^*_{i}}}{\int \sigma_i (T_*) dE \cdot \frac{\Gamma^* n_i}{\Gamma^*_{i}}} , \qquad \Gamma_i = \Gamma_{i} + \Gamma_{i} \qquad (13)
$$

for proton channels, and equivalently for neutron channels. With the subscript i we denote a set of channels belonging to the same particle level and the same hole subshell. Labels p and n apply to protons and neutrons, respec· tively. The use of a ratio of cross sections for a reaction channel is convenicnt bccausc there is a number of factors in the partial widths which is common Cor neutron and proton channels of the same i, and may also be common for channels with different isobaric spin and same i.

⁹⁰*Zr* (γ , p_0) ⁸⁹*Y*. Since the spin of the residual nucleus is $\frac{1}{2}$, only *s* and *d*

*proton channcls are accessiblc through this reaction. The excitations are of '*the type c-d for which the ratio $\int \sigma_i(T) dE / \int \sigma_i(T) dE$ is ≈ 0.25 (using $E(T_+) = 17$ MeV and $E(T_+) = 21.5$ MeV). Due to the large number of open *proton channels, one expects* $\Gamma^*_{\ell} / \Gamma^*_{\ell} \approx 1$. We shall assume that the dipole *statcs decay statistically and that thc ratio of parlial widths can bc replacccl by the ratio of transmission coefficient sums* $\Gamma_{ri}/\Gamma_i = \sum T_{ri}/\sum T_i$ *(the sum ·includcs ali the channels with the label i). Using the same formulac for transmission coefficients and level densities as in ref.*^{1*7*} we obtain $\Gamma_{ri}/\Gamma_i \approx 0.2$ *resulting in a value of about 1.2 for R (y, p***¹** *). However, i includes ali channels with 1/2⁻ proton holes and s and <i>d* protons (channels with ^{\$9}Y in its ground *state represent just one of the possibilitics). Due to the higher excitation* encrgy there are more proton channels available for the T_s resonance than *for the T. one. Using the same statistical arguments as before we find* $R(\gamma, p_0) \approx \frac{1}{40} R(\gamma, p_i) \approx 0.04$. A rough comparison to the experiment can be made by considering the marked areas on fig. 5 as possible T_z resonances *from which one would obtain R* $(\gamma, p_0) \approx 0.06$. In evaluating the experimental *value of R* (γ , p_0) only the (γ , p_0) cross section above $E_x \approx 13$ MeV was taken

 $^{90}Zr(\gamma, n)$ $^{89}Zr(T = 11/2)$. The threshold for this reaction is at 20.0 MeV *(Fig. 5). Taking into account the transmission coefficients and the value for* $E(T_s)$ of 21.5 MeV one gets for the reaction (γ, n) to the $T = 11/2$ state about the same number of open channels as for the reaction (γ, p_0) . There are only *isospin coupling coefficients which are different for the two reactions. As a* consequence we expect the T_z part of the integrated (γ , *n*) cross section to be

into account since in the lower energy region neutron channels are not open.

about (2 T_0 + 1) times larger than its (γ , p_0) counterpart. The later being of the *order of magnitude of 100 kcV · mb it yields for the integrated photoneutron cross section to the* $T = 11/2$ *state a value of about 1 McV · mb which is not* large enough to explain the structure in (γ, n) experimental data¹⁶ in the *energy region of 20 - 23 MeV. It is notcd that nuclci �* **⁹***Y,* **⁹¹***Zr, 91Zr and -»zr ,show Iess structurc in thc rcgion of excitations betwcen 20 and 23 MeV* although the thrcsholds for isospin allowed neutron decays^{*} of the T_r reso*nance are lower than in the case of* **⁹⁰***Zr. We, thereforc, conclude that the structure appearing at 20 - 23 MeV in photoneutron cross section for ⁹⁰_Zr must mainly be of some other origin. Also, an interpretation in terms of a quadrupole resonance would be difficult to relate to the experimental angular distribution (see Ref.***¹⁷¹***for angular distributions).*

 ^{90}Zr (γ , 2n) ⁸⁸Zr *and* ^{90}Zr (γ , *np*) ⁸⁸Y. The cross sections for these reactions *could also contain some* T_{S} *strength. In the case of* $(\gamma, 2n)$ *a neutron would* be emitted from the T_{c} dipole state leaving the residual nucleus ^{*}Y in a $T = 11/2$ state. This process would be followed by either gamma-ray or iso*spin forbidden neutron cmission (proton channels in* **⁸⁹***Zr are essentially closed at excitations of 1 or 2 MeV above the threshold). It is, however typical for the* $(\gamma, 2n)$ *cross section not to drop to zero even when isotopic spin* allowed $(\gamma, n + p)$ channels become open. It is concluded that the giant resonance high energy tail is composed of the $T₂$ component with a superposi*tion of* T_{S} states, in a similar fashion as the two known T_{S} resonances are superimposed on a $T₂$ continum in the lower energy region. For the (γ, np) *reaction***¹⁹***1 a very low cross section is obtained in agreement with small transmission coefficients.*

Other (γ, p) *channels.* Unless the T_{γ} resonance lies considerably higher *than 21.5 MeV we would not expect it to decay through any othcr neutron channels apart from the ones mentioned earlier. Therefore we expect the corresponding T* component to decay through *d* and *g* proton channels leav*ing the nucleus* ⁸⁹*Y in its excited states. Therefore it would be intercsting to*

measure the gamma-ray activity of the isomeric state 0.91 MeV $(I^{\pi} = 9/2^+,$ *
* $I^{\pi} = 16c$ *) in ⁸⁹V, formed during the irradiation of ⁹⁰⁷r with bremsstrablung* $\tau_{1/2}$ = 16s) in ⁸⁹*Y*, formed during the irradiation of ⁹⁰Zr with bremsstrahlung *gamma rays of different end-point energies. In this way a summed cross section could be cxtracted which would bc roughly proportional to the total high momentum proton cross section and which should include the maiin part of the T* **>** *dipole strength.*

We draw the following conclusions about the T0 + I component of the giant dipole resonance in ${}^{\circ}\mathcal{Z}r$:

 $-$ the total integrated cross section for the T_s component should be about 10 times larger than its T_z counterpart,

^{*} Here the sum of $\sigma(\gamma, n)$, $\sigma(\gamma, np)$ and $\sigma(\gamma, 2n)$ should be considered since the threshold for the last two reactions is mostly rather low.

- $-$ the integrated (γ, n) cross section for the excitations of the T_z type *should have a small value of the order of 1 MeV · mb.*
- $-$ the $(\gamma, 2n)$ cross section is mainly of the T_{c} type. The T_{c} resonance *extends to high energies. T. states are superimposed on its high-energy tail, and*
- *thc 1·. resonancc decays mainly through high momentum proton chan· ncls leaving thc nucleus 89Y in its excited states. It could be detected by measuring thc activity o(the first excited isomeric state of* **⁶⁹***Y obtained* by the irradiation of the nucleus ^{\$2}*Xr* with gamma rays of difterent end-*·point encrgies.*

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IZOBARNI SPIN V FOTOJEDRSKIH REAKCIJAH

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V se bina

V prvem delu sta na kratko povzeti splošna ocena razmerja jakosti obeh izotopsko-spinskih komponent fotojedrske dipolne veleresonance in ocena nujnega energijskega razmaka.

Za razumevanje meritev je potreben študij posameznih reakcijskih kanalov, kajti nekateri kanali kažejo močno izospinsko selektivnost.

Posebej so obravnavana nekatera jedra. Pokazano je, da se iz dosedanjih meritev na IIB ne da sklepati na izospinski razcep pri tem jedru. Podrobneje je obravnavano jedro ⁹⁰Zr. Ocenjen je delež posameznih izospinskih kompo*nent v dipolni veleresonanci, kakor tuđi v posameznih reakcijskih kanalih. Te ocene se z dosedanjimi meritvami ujemajo.*