VoStackSDD: A Novel Ensemble Technique for Software Defect Density Prediction

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Abstract-Software defect density prediction is vital for improving software quality and reducing maintenance costs. Traditional models often fall short in predicting software defect density, whereas our approach focuses on enhancing software defect density prediction. This research paper presents a novel ensemble learning model, VoStack, designed for software defect density prediction. VoStack, a fusion of Voting and Stacking Regressors, is evaluated against several individual machine models, including RidgeCV, RandomForest, GradientBoosting, and KNeighbors, across nine datasets from the Tera-Promise and GitHub Bug Prediction Repositories. Each model's performance is evaluated through various statistical and error metrics. Results demonstrate that VoStack consistently outperforms individual models, achieving the lowest error rates and highest predictive accuracy across all datasets. Statistical analyses confirm the significance of these performance differences. This study highlights VoStack's effectiveness in enhancing predictive accuracy for defect density prediction, offering a robust approach for software quality assurance.

Index terms—Software Defect Density Prediction, VoStack Regressor, Ensemble Modeling, Feature selection, Predictive performance.

I. INTRODUCTION

Software defect density prediction is vital for ensuring software excellence and minimizing maintenance expenses [1]. Accurately predicting defect density can help identify potential issues early in the software development lifecycle, saving significant time and resources in debugging and quality assurance. Despite its importance, achieving reliable and robust predictions remains a challenge, partly because of the complex and multi-dimensional structure of software defect data [2]. Existing models for defect density prediction, such as individual machine learning algorithms, often face limitations in handling these complexities. Traditional models often struggle with overfitting or underfitting, which can hinder their ability to perform well on unseen data. Furthermore, the performance of these models can vary significantly across different datasets, making it difficult to achieve consistently high accuracy [3]. Ensemble learning methods, which integrate multiple models to boost prediction accuracy, have proven effective in addressing these challenges [4]. Among these, Voting and Stacking Regressors are notable for their ability to

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enhance model robustness and accuracy by aggregating predictions from several base models.

This research introduces a novel ensemble model called VoStack Regressor, designed to improve defect density prediction by drawing on the complementary benefits of Voting and Stacking Regressors. Our approach combines multiple base models, including RandomForestRegressor, XGBRegressor, and more, to aggregate predictions via a Voting Regressor, and then refines these predictions using a Stacking Regressor with Random Forest as the meta-model. Our aim focuses on addressing limitations found in traditional models while boosting accuracy and robustness in defect density predictions

The primary research problem we address is the development of a more reliable and accurate model for defect density prediction. Our problem statement is: How can we improve the predictive performance and robustness of software defect density models through ensemble learning techniques? To effectively address this challenge, we examine the research questions mentioned below:

- RQ1: How does the VoStack Regressor's effectiveness compare to that of individual learning models?
- RQ2: How does VoStack Regressor compare to individual Voting and Stacking models in terms of performance?
- RQ3: Does the statistical analysis validate the results for VoStack Regression's defect density prediction?

To validate our approach, we utilize nine datasets from the Tera-Promise [5,6] and GitHub bug [5] prediction repository, evaluating the performance of the VoStack Regressor against individual base models and traditional methods.

This paper introduces the novel ensemble model, VoStack for improving prediction performance for defect density. In fact, the significant contributions of this study include:

- 1. A robust ensemble model, VoStack, developed by combining Voting and Stacking Regressors to overcome issues with traditional approaches.
- 2. Comprehensive evaluation of VoStack's performance across nine datasets from the Tera-Promise and GitHub Bug Prediction repositories.
- 3. Demonstration of VoStack's superiority over individual machine learning models and traditional ensemble methods through detailed statistical and error metric analyses.
- 4. Validation of the model's robustness and predictive reliability using statistical significance tests.

The paper is structured as follows: Section II discusses the related work and provides background information on defect density pre-diction and ensemble learning methods. Section III details our methodology, including data preprocessing, feature selection using the Recursive Feature Elimination, and the architecture of the VoStack Regressor model. Section IV discusses the results, highlighting the performance of our proposed model. Section V discusses the implications of our findings, potential future work, and concludes with a summary of our contributions to the field and Section VI addresses threats to validity.

II. RELATED WORK

Recent advancements in software defect prediction have leveraged diverse machine learning and ensemble techniques to enhance predictive performance. Wang et al. [7] employed the XGBoost model, incorporating data preprocessing, feature selection, and hyperparameter tuning to improve defect detection accuracy. Hussain et al. [8] introduced a CodeBERTbased approach for multiclass software defect prediction, utilizing NLP techniques to classify defects and demonstrating notable accuracy improvements over models like RoBERTa and GPT-2. Yang et al. [9] proposed an Ensemble Kernel-Mapping-Based Ranking Support Vector (EKMRSVM) for rank-oriented defect prediction, optimizing model parameters through sequential minimal optimization and achieving superior ranking accuracy across multiple datasets. Dong et al. [10] introduced a novel ensemble classifier selection method using the Double Fault Disagreement (DFD) metric, which enhances predictive performance while reducing computational costs. Goyal [11] conducted a systematic review of class imbalance learning (CIL) techniques in software defect prediction, analyzing 91 datasets and emphasizing the effectiveness of ensemble-based hybrid methods, particularly with AUC as a robust evaluation metric. Mustageem et al. [12] presented a bibliographic survey of 79 studies, identifying gaps in dataset limitations, validation methodologies, and feature selection, advocating for AI-driven hybrid approaches to improve defect prediction models. Chan and Keung [13] proposed a metamorphic testing (MT) framework for unsupervised software defect prediction, validating models without labeled data and demonstrating its robustness across various machine learning algorithms and datasets. These studies collectively highlight the growing sophistication of software defect prediction models, incorporating advanced ensemble learning, NLP, class imbalance handling, and validation techniques to improve defect detection and model reliability.

We review recent work on software defect prediction. While software defect prediction has been extensively studied using machine learning and ensemble techniques, most existing research focuses on binary or multiclass classification of defects. In contrast, defect density prediction, which is the focus of our work, estimates the number of defects per unit of code, providing a more granular measure of software reliability.

Defect density is a critical metric for measuring the effectiveness and quality of software development efforts. Numerous studies have employed statistical methods, machine learning algorithms, and fuzzy logic approaches to investigate the association between static code metrics and defect density.

Each of these studies has contributed to a progressive improvement in predictive accuracy by building on the findings and addressing the limitations of prior research.

A. Statistical Methods for Software Defect Density Prediction.

Nagappan and Ball [14] analyzed the impact of code churn metrics on defect density using regression techniques. Their findings indicated a strong correlation, suggesting that code churn metrics serve as effective predictors of defect density. Rahmani and Khazanchi [15] examined the connection between defect density and factors such as software size, developer involvement, and the number of downloads. Verma and Kumar [16] studied how defect density is influenced by five distinct metrics from open-source projects, basing their conclusions on the statistical significance of determination coefficients. Similarly, Mandhan Verma and Kumar [17] extended this analysis to seven metrics, confirming a statistically significant association with defect density Marchenko and Abrahamsson [18] introduced a framework for analyzing the association between code metrics and defect density in embedded systems, employing two tools to predict defect rates with high accuracy. Verma et al. [19] also investigated the impact of module size on defect density, suggesting that splitting larger modules into smaller ones can substantially improve defect density.

Li et al. [20] introduced an alternate modification index, a measure of how frequently multiple developers modify the source code, revealing a positive association with defect density. Mohagheghi et al. [21] examined the effect of component size and reuse on defect density; they found that reused components generally have a much lower defect density than those which are not reused.

B. Traditional Approaches for Software Defect Density Prediction

Sherriff et al. [22] applied five metrics to analyze fourteen projects to predict defect density, demonstrating the applicability of machine learning algorithms in this domain. Kutlubay et al. [23] applied machine learning algorithms to NASA datasets, classifying modules as defective or defect-free and predicting defect density. Their study concluded that decision trees outperformed radial basis function neural networks for this task. Using decision trees, Knab et al. [24] analyzed sixteen metrics from seven software releases, and found that factors such as the number of functions, change coupling, and lines of code had a negligible effect on defect density prediction. López-Martín et al. [25] tested two variants of support vector regression (SVR) on twenty-one projects from the ISBSG dataset and found that the v-SVR with polynomial kernels outperformed traditional statistical regression methods in predicting defect density in unseen software projects. In another study, López et al. [26] introduced the Transformed Knearest Neighborhood Output Distance Minimization (TKDM) algorithm, which showed superior performance over other models in predicting defect density in software projects from the ISBSG dataset.

Rathaur et al. [27] employed multiple linear regression to predict defect density in open-source products from the Git system, identifying the number of developers and code churn as

significant factors. Alghanim et al. [28] proposed a deep learning model based on generalized regression neural networks, achieving notable improvements in prediction accuracy

C. Ensemble Methods for Software Defect Density Prediction.

Kumar et al. [29] applied fuzzy logic combined with neural networks to predict defect density based on 4000 bug files based on three metrics. They concluded that neural networks provided better results than fuzzy logic systems. Yadav and Yadav [30] proposed a fuzzy inference system using nine metrics collected from four development phases, demonstrating the effectiveness of fuzzy logic in defect density prediction. Khalsa [31] created a fuzzy system model utilizing six metrics from the MOOD suite, demonstrating that certain metrics had a direct correlation with defect density, while others exhibited an inverse relationship.

Azzeh et al. [32] proposed a defect density prediction model known as the Grey-Fuzzy Model, which integrates grey system theory and fuzzy logic to manage uncertainties in measurement. Their model, validated against public defect datasets, outperformed others on highly sparse datasets. Ensemble learning techniques were competitive for datasets with lower sparsity, while statistical regression models were less effective. Sensitivity analysis showed the model stability under varying uncertainty levels.

D. Comparison with State-of-the-Art Methods

Recent studies in software defect prediction have primarily focused on defect classification (binary/multiclass) rather than defect density prediction. A comparative discussion is summarized in Table I, which shows the key differences between these approaches and the proposed VoStack model.

Our research introduces VoStack, a groundbreaking ensemble model that combines Voting and Stacking techniques for software defect density prediction. Previous studies have not utilized Voting and Stacking individually or in combination for this purpose. By integrating these two methodologies, VoStack overcomes the limitations of existing models, significantly enhancing prediction accuracy and robustness. This innovative approach provides a notable improvement over conventional methods, demonstrating superior performance across diverse datasets.

III. METHODOLOGY

This paper introduces the ensemble-based VoStack framework which combines multiple supervised machine learning algorithms for software defect density estimation. The entire procedure, as given in Figure 1, contains the following basic steps: preprocessing, feature extraction, model generation, and model validation. Before the application, datasets from both Tera-PROMISE and GitHub Bug Prediction repositories are processed with data cleansing, normalization, and an 75-25 train-test split using StandardScaler. Dimensionality reduction is performed using Recursive Feature Elimination with RidgeCV for feature selection. The VoStack model uses a combination of RidgeCV, SVR, Huber Regressor, Random Forest, Gradient Boosting, and K-Neighbors

Regressor using Voting Regressor for stability and Stacking Regressor with Random Forest as the meta-learner for refinement of predictions. MSE, RMSE, MAE, MAPE, and R² were used to check the effectiveness of VoStack compared to the other models. In the following sections, the dataset description, preprocessing, feature selection, proposed model workflow, and results are described that lead to the final dataset and evaluation of VoStack's predictive performance.

TABLE I
COMPARISON WITH STATE-OF-THE-ART DEFECT PREDICTION METHODS

Work	Task	Methodology	Performance/Complexity vs VoStack
Wang et al. [7]	Defect classification	XGBoost + preprocessing, FS, tuning	High accuracy, but high computational cost; not designed for continuous density prediction. VoStack targets regression tasks with lower complexity and competitive performance.
Hussain et al. [8]	Multiclass defect classification	CodeBERT- based NLP	Excellent for text-based defect classification; unsuitable for numeric defect density prediction. VoStack focuses on structured feature-based prediction with lightweight models.
Yang et al. [9]	Defect ranking	Ensemble Kernel- Mapping Rank SVM	Optimized for ranking tasks, not density estimation. VoStack directly predicts defect density values and offers simpler model architecture.
Dong et al. [10]	Defect prediction	Ensemble Classifier Selection using DFD metric	Focused on optimizing binary classifiers' combination; VoStack extends ensemble learning (Voting + Stacking) to regression with emphasis on robustness and stability.
Azzeh et al. [32]	Defect density prediction	Grey-Fuzzy Model	Good under data sparsity, but complex fuzzy system; VoStack maintains prediction accuracy with simpler, interpretable ensemble models.

A. Datasets

Our study focuses on defect density analysis, which requires accurate bug count information. We utilized nine datasets from the Tera-Promise [5,6] and Github bug prediction [5] repositories, all of which are publicly available and frequently used in software engineering research for defect prediction. The selected datasets include three from Tera-PROMISE ('ant 1.3', 'tomcat', and 'jedit 3.2') and six from GitHub

('BroadleafCommerce-broadleaf-3.0.10-GA', 'Neo4j', 'Hazelcast3.3', 'ory', and 'titan-0.5.1'). The original datasets did not contain defect density information, so we calculated it using Eq. (1):

Software Defect Density =
$$\frac{Number\ of\ Bugs}{Line\ of\ Code} * 1000$$
 (1)

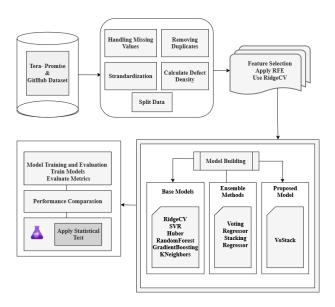


Fig. 1. Proposed Methodology

The datasets are first loaded and then cleaned by handling missing values and removing duplicates to ensure data quality. After cleaning, data is standardized and normalized using the Standard Scaler tool available in the scikit-learn library. Standardization ensures that each feature contributes equally during model training by normalizing the data to ensure a mean of 0 and a standard deviation of 1.

The datasets are then partitioned into an 75-25 ratio for training and testing purposes. Table II presents the datasets utilized in this study, while Table III lists the independent and dependent variables for each dataset.

B. Feature Selection Using RFE

In this study, Recursive Feature Elimination (RFE) was utilized with RidgeCV as the estimator for selecting the most relevant features in the dataset, aiming to improve model performance and interpretability. RFE operates by recursively fitting the model and removing the least important feature based on the estimator's coefficients.

Mathematically, for each iteration, the RFE algorithm computes the importance score for each feature based on the absolute values of the coefficients in the Ridge regression model. RidgeCV, a variant of ridge regression that incorporates cross-validation to select the best regularization parameter (alpha), minimizes a loss function penalized by the L2 norm:

$$\min\left(\sum_{i=1}^{n} (y_i - X_i \beta)^2 + \alpha \sum_{i=1}^{p} \beta_i^2\right) \tag{2}$$

where y_i represents the taget variable, X_i the predictors, the coefficients, β number of observations, n the number of

predictors and α regularization parameter that controls the shrinkage of coefficients. The parameter n_features_to_select was set to 5. This means Recursive Feature Elimination (RFE) iteratively removed the least important features until only 5 features remained. This process effectively reduced the datasets dimensionality, focusing on the most predictive variables. By doing so, it enhanced the subsequent model's performance and generalization capabilities while reducing the risk of overfitting and minimizing computational complexity. Table IV displays the features selected through the RFE method.

TABLE II DESCRIPTION OF DATASETS.

Dataset	Project	Lang	Gran	Total Source Code Element s	Defectiv e Source Code Element s	% of Buggy Source Code Element s
	Broadleaf Commerce	Java	File	1,719	286	16.64%
GitHub	NEON04J	Java	File	3278	32	0.98%
Bug	HAZEL	Java	File	2,228	317	14.23%
Prediction	Oryx	Java	File	280	44	15.71%
	MapDB 0.9.6	Java	file	137	22	16.06%
	ANT 1.3	Java	Class	125	20	0
Tera - Promise	Tomcat	Java	class	858	77	8.97%
	"jedit 3.2"	Java	class	272	90	33.09%
	"Jedit 4.2"	Java	class	367	48	1308.0

TABLE III
DATASET INDEPENDENT AND DEPENDENT VARIABLES

Datasets	Independent	Dependent
Tera- Promise	"Wmc, dit, noc, cbo, rfc, lcom, ca, ce, npm, lcom3, dam, moa, mfa, cam, ic, cbm, amc, max_cc, avg_cc"	Defect_Density
GitHub Bug Prediction	"McCC, CLOC, PDA, PUA, LLOC, McCC, CLOC,No. of previous fixes, No. of committers, No. of previous modifications, No. of developers commits"	Defect_Density

C. Proposed Model

In this analysis, we propose a unique ensemble learning model, termed VoStack, which combines the strengths of voting and stacking ensemble methods to enhance predictive accurateness and robustness. The Vostack model is designed to leverage the diverse capabilities of multiple base learners and a meta-learner, thereby optimizing the overall predictive performance by minimizing bias and variance.

The construction of the VoStack model involves two main phases: the voting phase and the stacking phase. In the voting phase, a set of base regressors, including RidgeCV, Support Vector Regressor (SVR), Huber Regressor, Random Forest Regressor (RF), Gradient Boosting Regressor (GBR), and K-Nearest Neighbors Regressor (KNN), are combined using a Voting Regressor. Each base model is assigned equal weights, and their predictions are aggregated by averaging:

$$[\hat{y}_{Voting} = \frac{1}{M} \sum_{m=1}^{M} \hat{y}_m]$$
(3)

where \hat{y}_m represents the prediction of the base regressor, and M is the total number of base regressors.

TABLE IV
SELECTED FEATURES USING THE RFE METHOD FOR EACH DATASET

Dataset	Selected Features
Ant 1.3	'dit', 'dam', 'moa', 'cam'
BroadleafCommerce	'Number of previous fixes', 'Number of committers', 'Number of previous modifications'
NEON04J	'McCC', 'McCC.1', 'Number of previous fixes', 'Number of committers'
Hazelcast	'PDA', 'McCC.1', 'Number of previous fixes', 'Number of committers'
Jedit 3.2	'cbo', 'lcom3', 'moa', 'mfa', 'cam'
ory	'McCC', 'PDA', 'PUA', 'McCC.1'
Titan	'PDA', 'Number of previous fixes', 'Number of committers', 'Number of previous modifications',
Jedit 4.2	'lcom3', 'dam', 'mfa', 'cam'
Tomcat	'cbo', 'lcom3', 'moa', 'mfa', 'cam'

In the stacking stage, the output from the voting regressor serves as input to a Stacking Regressor along with the original dataset. The stacking regressor employs a meta-learner, in this case, a Random Forest Regressor, to learn the optimal combination of predictions from the voting regressor and the original input features. The meta-learner is trained to minimize the mean squared error (MSE):

$$\min_{\theta} \frac{1}{N} \sum_{i=1}^{N} \left(y_i - \hat{y}_{stack} (X_i, \hat{y}_{Voting,i}; \theta) \right)$$
(4)

where y_i is the actual target value, \hat{y}_{stack} is the prediction of the stacking regressor, X_i are the original input features, $\hat{y}_{voting,i}$ is the output from the voting regressor, and θ represents the parameters of the meta-learner.

The VoStack model thus integrates the advantages of both voting and stacking, allowing for a robust combination of model predictions. This hybrid approach capitalizes on the diverse strengths of individual models (base learners) in the voting stage, and further refines the predictive power through a second-layer model (meta-learner) in the stacking stage. In this model, the Random Forest meta-learner is set to 100 estimators to balance accuracy and efficiency, KNN is set to 5 neighbors to prevent overfitting and underfitting, and SVR uses an RBF kernel due to its ability to capture non-linear relationships in defect density prediction. By using this dual-layer ensemble method, the VoStack model enhances prediction accuracy and provides improved generalization to unseen data, thereby making it an effective model for regression tasks. Figure 2 presents the workflow of the proposed work.

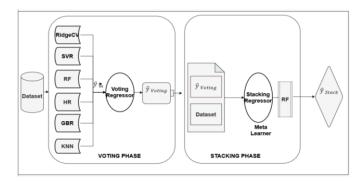


Fig.2. Proposed VoStack Model Workflow

D. Performance Evaluation

All experiments we conducted using Python, utilizing libraries including scikit-learn, pandas, NumPy, and seaborn for data manipulation, analysis, and visualization. Machine learning algorithms were implemented using scikit-learn. To evaluate and contrast the predictive capabilities of our models in defect density estimation, several key performance metrics were employed. Table V provide the formulas and descriptions of the performance metrics used, where ADDi represents the actual defect density for the ith sample, and PDDi represents the predicted defect density for the ith sample.

E. Baseline Method Selection and Justification

To ensure a fair and comprehensive evaluation, we selected baseline models based on their frequent use and effectiveness in prior software defect density prediction studies.

- Linear Models (RidgeCV, Huber Regressor): These models serve as strong baselines for regression tasks due to their robustness to noise (Huber) and ability to manage multicollinearity (RidgeCV).
- Support Vector Regression (SVR): Widely used in defect density prediction (e.g., López-Martín et al. [25]), SVR has shown high prediction capability with small to mediumsized datasets.
- Ensemble Models (Random Forest, Gradient Boosting): Prior studies (e.g., Dong et al. [10]) indicate ensemble methods significantly improve defect prediction by capturing complex feature interactions.
- Instance-based Model (K-Nearest Neighbors): As tested by López et al. [26] for defect density, KNN models provide a non-parametric approach to comparison.

The models were selected to cover a diverse set of algorithmic families linear, kernel-based, ensemble-based, and instance-based to comprehensively benchmark VoStack's performance.

IV. RESULTS AND DISCUSSION

In this research, an ensemble learning model, VoStack, which is a fusion of voting and stacking regressions, was implemented to predict the density of the software defects. To explore the research questions, we performed an analysis comparing the performance of individual machine learning models with the VoStack model. Specifically, we aimed to

evaluate how VoStack performs in comparison to individual Voting and Stacking models, and to quantify the percentage improvement. Additionally, statistical tests were applied to assess the significance of the performance differences. Various single learning models were evaluated across nine different datasets to benchmark performance. The metrics used for comparison include Mean Squared Error (MSE), Root Mean Squared Error (RMSE), Mean Absolute Error (MAE), and R-squared (R²). The results are presented and discussed for each dataset below.

TABLE V
PERFORMANCE MEASURES FOR DEFECT DENSITY PREDICTION

Metric	Formula	Description
Root Mean Squared Error (RMSE)	$\sqrt{\frac{1}{n}\sum_{i=1}^{n}(ADD_{i}-PDD_{i})^{2}}$	Indicates the average error magnitude in predicted defect density values.
Mean Squared Error (MSE)	$\frac{1}{n} \sum_{i=1}^{n} (ADD_i - PDD_i)^2$	Computes the average of the squared errors between the predicted and actual defect density values.
Mean Absolute Error (MAE)	$\frac{1}{n}\sum_{i=1}^{n} ADD_{i}-PDD_{i} $	Calculates the average absolute error in predicted defect density
R-squared (R2)	$1 - \frac{\sum_{i=1}^{n} (ADD_i - PDD_i)^2}{\sum_{i=1}^{n} (ADD_i - \overline{ADD})^2}$	Represents the percentage of variance in the actual defect density that is accounted for by the predicted defect density.

Table VI shows that VoStack achieved the best performance on the ANT 1.3 dataset, demonstrating its superior capability in minimizing error metrics. With the lowest Mean Squared Error (MSE) of 0.0340, Root Mean Squared Error (RMSE) of 0.1845, and Mean Absolute Error (MAE) of 0.0593, along with the highest R² of 0.7051, VoStack outperforms all other models. In contrast, KNeighbors exhibited the highest error rates, with an MSE of 0.1000 and RMSE of 0.3162, and the lowest R² of 0.1336.

Table VII reveals that VoStack again leads with the best results for the BroadleafCommerce-broadleaf-3.0.10-GA dataset, achieving the lowest MSE (0.8392), RMSE (0.9161), and MAE (0.1652), alongside the highest R² of 0.9453. RandomForest closely follows with a high R² of 0.9281, indicating its strong performance. Conversely, models like Huber and RidgeCV had lower R² values (0.6007 and 0.7089, respectively), suggesting that they were less effective at capturing the complexities of this dataset. In Table VIII, VoStack continues its trend of superior performance on the Neo4j dataset, with the lowest MSE (0.1998), RMSE (0.4469), and MAE (0.0197), and the highest R² (0.8444). RandomForest also performed admirably, with an R² of 0.8281. However, RidgeCV and SVR, with R² values around 0.3687, performed considerably.

Table IX shows that VoStack outperforms all models, achieving the lowest MSE (11.8986), RMSE (3.4494), and highest R^2 (0.8888). Random Forest follows closely (R^2 = 0.8855), while RidgeCV, SVR, and Huber show weaker

performance ($R^2 < 0.56$). This confirms VoStack's superior predictive accuracy.

Table X illustrates that VoStack delivered the best performance for the ory dataset, achieving an MSE of 0.1064, RMSE of 0.3262, MAE of 0.0579, and an R² of 0.9871. This remarkable performance highlights VoStack accuracy. RandomForest and KNeighbors also performed well, with R² values of 0.9503 and 0.9582, respectively. In comparison, RidgeCV and Huber, with R² values of 0.7979 and 0.7880, were less effective. In Table XI, VoStack again excels with the lowest MSE (0.0157), RMSE (0.1254), and MAE (0.0389), and the highest R² (0.9183) for the Tomcat dataset. RandomForest and KNeighbors also showed strong performance, with R² values of 0.8457 and 0.7875. The SVR model, while better than RidgeCV and Huber, did not match VoStack's superior performance.

Table XII indicates that VoStack achieved the best results for the titan-0.5.1 dataset with an MSE of 0.3297, RMSE of 0.5742, MAE of 0.1501, and R^2 of 0.9441. RandomForest followed closely with an R^2 of 0.9241. Other models like RidgeCV and SVR had lower R^2 values (0.4831 and 0.4380), demonstrating that they were less effective for this dataset.

In Table XIII, VoStack again outperformed all other models on the Jedit 3.2 dataset, with the lowest MSE (7.6378), RMSE (2.7637), and MAE (0.5374), and the highest R² (0.8314). RandomForest and KNeighbors also performed well, with R² values of 0.8031 and 0.7762. SVR and Huber, with lower R² values (0.3534 and 0.4523), demonstrated less effectiveness. Table XIV shows that VoStack managed to provide the best performance for the Jedit 4.2 dataset with an MSE of 72.9464, RMSE of 8.5409, MAE of 0.9952, and an R² of 0.1818. Despite the challenges of this dataset, VoStack still performed better than other models. RandomForest also showed reasonable performance with an R² of 0.1526, while other models faced significant difficulties, as evidenced by their low R² values.

Across all nine datasets, VoStack consistently shows superior performance in terms of error metrics (MSE, RMSE, MAE) and predictive accuracy (R²) compared to individual single learning models. This confirms that VoStack ensemble approach enhances performance in software defect density prediction.

RQ2: How Does VoStack Compare to Individual Voting and Stacking Models in Performance?

To address research question 2 regarding the performance of VoStack compared to individual Voting and Stacking models, analysis demonstrates that VoStack consistently outperforms both approaches across various datasets. Table XIV shows that VoStack achieves significantly lower Mean Squared Error (MSE), Root Mean Squared Error (RMSE), and Mean Absolute Error (MAE) compared to both Voting and Stacking models. Additionally, VoStack demonstrates higher R-squared (R2) values, indicating better predictive accuracy. In the ANT 1.3 dataset, VoStack MSE is 50.80% lower than voting and 33.46 % lower than Stacking. Its RMSE is 29.79 % lower than voting and 18.40 % lower than Stacking. These trends are consistent across other datasets as well, highlighting VoStack effectiveness in reducing prediction errors. Table XV shows the performance comparison of VoStack, Voting, and Stacking models.

 $\begin{tabular}{l} TABLE\ VI\\ Model\ Performance\ metrics\ for\ Dataset\ Ant\ 1.3\\ \end{tabular}$

Model	MSE	RMSE	MAE	R ²
RidgeCV	0.0575	0.2397	0.1002	0.5021
SVR	0.0743	0.2725	0.1515	0.3563
Huber	0.0722	0.2687	0.0868	0.3743
RandomForest	0.0606	0.2461	0.0873	0.4752
GradientBoosting	0.0756	0.2750	0.1055	0.3445
KNeighbors	0.1000	0.3162	0.1070	0.1336
VoStack	0.0340	0.1845	0.0593	0.7051

TABLE VII
MODEL PERFORMANCE METRICS FOR DATASET
BROADLEAF-3.0.10

Model	MSE	RMSE	MAE	R ²
RidgeCV	4.4646	2.1130	1.0013	0.7089
SVR	3.0245	1.7391	0.4419	0.8028
Huber	6.1237	2.4746	0.7381	0.6007
RandomForest	1.1022	1.0499	0.2097	0.9281
GradientBoosting	2.5408	1.5940	0.8241	0.8343
KNeighbors	1.2172	1.1033	0.2312	0.9206
VoStack	0.8392	0.9161	0.1652	0.9453

TABLE VIII
MODEL PERFORMANCE METRICS FOR DATASET NEON4J

Model	MSE	RMSE	MAE	R ²
RidgeCV	0.8103	0.9002	0.0780	0.3687
SVR	0.8104	0.9002	0.0967	0.3686
Huber	0.8346	0.9136	0.0486	0.3498
RandomForest	0.2207	0.4698	0.0282	0.8281
GradientBoosting	0.3791	0.6157	0.0490	0.7046
KNeighbors	0.4553	0.6748	0.0320	0.6453
VoStack	0.1998	0.4469	0.0197	0.8444

TABLE IX
MODEL PERFORMANCE METRICS FOR DATASET
HAZEL CAST 3.3

Model	MSE	RMSE	MAE	R ²
RidgeCV	47.2517	6.8740	3.4255	0.5584
SVR	58.6603	7.6590	1.8261	0.4518
Huber	51.0300	7.1435	2.0407	0.5231
RandomForest	12.2498	3.5000	0.6037	0.8855
GradientBoosting	38.9605	6.2418	2.1262	0.6359
KNeighbors	22.8702	4.7823	1.2789	0.7863
VoStack	11.8986	3.4494	0.6050	0.8888

TABLE X
MODEL PERFORMANCE METRICS FOR DATASET ANT ORY

Model	MSE	RMSE	MAE	R ²
RidgeCV	1.6644	1.2901	0.8651	0.7979
SVR	0.9553	0.9774	0.2943	0.8840
Huber	1.7453	1.3211	0.8264	0.7880
RandomForest	0.4092	0.6397	0.1090	0.9503
GradientBoosting	1.4814	1.2171	0.6383	0.8201
KNeighbors	0.3438	0.5864	0.1387	0.9582
VoStack	0.1064	0.3262	0.0579	0.9871

TABLE XI
MODEL PERFORMANCE METRICS FOR DATASET TOMCAT

Model	MSE	RMSE	MAE	R ²
RidgeCV	0.0633	0.2515	0.0861	0.6517
SVR	0.0587	0.2423	0.0490	0.6791
Huber	0.0860	0.2932	0.0757	0.5310
RandomForest	0.0294	0.1715	0.0488	0.8457
GradientBoosting	0.0516	0.2272	0.0508	0.7120
KNeighbors	0.0400	0.2000	0.0486	0.7875
VoStack	0.0157	0.1254	0.0389	0.9183

TABLE XII
MODEL PERFORMANCE METRICS FOR DATASET TITAN-0.5.1

Model	MSE	RMSE	MAE	R ²
RidgeCV	2.1297	1.4594	0.6651	0.4831
SVR	2.3001	1.5166	0.4846	0.4380
Huber	2.2312	1.4937	0.4739	0.4545
RandomForest	0.4083	0.6389	0.1650	0.9241
GradientBoosting	1.1596	1.0778	0.3870	0.7203
KNeighbors	0.5038	0.7091	0.1426	0.8996
VoStack	0.3297	0.5742	0.1501	0.9441

TABLE XIII
MODEL PERFORMANCE METRICS FOR DATASET JEDIT-3.2

Model	MSE	RMSE	MAE	R ²
RidgeCV	26.1298	5.1117	1.2708	0.4569
SVR	29.8747	5.4689	1.6342	0.3534
Huber	26.3022	5.1295	1.2348	0.4523
RandomForest	9.1130	3.0188	0.6465	0.8031
GradientBoosting	13.8542	3.7208	0.9457	0.6897
KNeighbors	10.4473	3.2317	0.7384	0.7762
VoStack	7.6378	2.7637	0.5374	0.8314

TO DEET ENG OTHER TO SEE THE SECOND TO SEE THE SECOND TO				
Model	MSE	RMSE	MAE	R ²
RidgeCV	86.4471	9.2977	1.4023	0.0304
SVR	88.3487	9.3994	1.1696	0.0091
Huber	89.0708	9.4377	1.1301	0.0010
RandomForest	75.5488	8.6919	1.0619	0.1526
GradientBoosting	77.6623	8.8126	1.1449	0.1289
KNeighbors	90.5228	9.5143	1.2961	0.0153
VoStack	72.9464	8.5409	0.9952	0.1818

 $\begin{tabular}{ll} TABLE~XIV\\ MODEL~PERFORMANCE~METRICS~FOR~DATASET~JEDIT-4.2\\ \end{tabular}$

than other models. RandomForest also showed reasonable performance with an R² of 0.1526, while other models faced significant difficulties, as evidenced by their low R² values.

Across all nine datasets, VoStack consistently shows superior performance in terms of error metrics (MSE, RMSE, MAE) and predictive accuracy (R²) compared to individual single learning models. This confirms that VoStack ensemble approach enhances performance in software defect density prediction.

RQ2: How Does VoStack Compare to Individual Voting and Stacking Models in Performance?

To address research question 2 regarding the performance of VoStack compared to individual Voting and Stacking models, the analysis demonstrates that VoStack consistently outperforms both approaches across various datasets. Table XIV shows that VoStack achieves significantly lower Mean Squared Error (MSE), Root Mean Squared Error (RMSE), and Mean Absolute Error (MAE) compared to both Voting and Stacking models. Additionally, VoStack demonstrates higher R-squared (R²) values, indicating better predictive accuracy. In the ANT 1.3 dataset, VoStack MSE is 50.80% lower than voting and 33.46 % lower than Stacking. Its RMSE is 29.79 % lower than voting and 18.40 % lower than Stacking. These trends are consistent across other datasets as well, highlighting VoStack effectiveness in reducing prediction errors. Table XV shows the performance comparison of VoStack, Voting, and Stacking models.

Figures 3 through 6 further illustrate these performance improvements. Figure 3 displays the comparative MSE results, Figure 4 shows the RMSE comparisons, Figure 5 highlights the MAE differences, and Figure 6 presents the R² values for each model. The visual representations confirm that VoStack achieves superior accuracy and robustness, validating its enhanced performance in software defect density prediction.

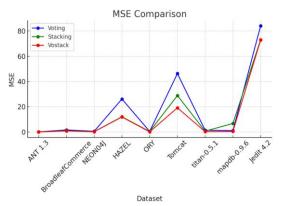


Fig. 3. MSE Comparison Across Datasets

TABLE XV
PERFORMANCE COMPARISON OF VOSTACK, VOTING
& STACKING MODELS

Metric Dataset Voting vs VoStack (%) Stacking vs VoStack (%) MSE ANT 1.3 50.80 33.46 BroadleafCommerce 48.62 19.82 NEON04J 62.96 19.11 HAZEL 54.46 1.51 ORY 77.77 71.52 Tomcat 58.60 33.64 titan-0.5.1 82.47 61.42 mapdb-0.9.6 61.84 94.06 Jedit 4.2 13.36 0.26 RMSE ANT 1.3 29.79 18.40 BroadleafCommerce 28.32 10.46 NEON04J 39.16 10.08 HAZEL 32.52 0.76 ORY 52.85 46.63 Tomcat 35.66 18.54 titan-0.5.1 58.13 37.89 mapdb-0.9.6 38.23 75.63 Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30		& STA	CKING MODELS	
BroadleafCommerce	Metric	Dataset		_
NEON04J 62.96 19.11 HAZEL 54.46 1.51 ORY 77.77 71.52 Tomcat 58.60 33.64 titan-0.5.1 82.47 61.42 mapdb-0.9.6 61.84 94.06 Jedit 4.2 13.36 0.26 RMSE ANT 1.3 29.79 18.40 BroadleafCommerce 28.32 10.46 NEON04J 39.16 10.08 HAZEL 32.52 0.76 ORY 52.85 46.63 Tomcat 35.66 18.54 titan-0.5.1 58.13 37.89 mapdb-0.9.6 38.23 75.63 Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R ² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30	MSE	ANT 1.3	50.80	33.46
HAZEL		BroadleafCommerce	48.62	19.82
ORY 77.77 71.52 Tomcat 58.60 33.64 titan-0.5.1 82.47 61.42 mapdb-0.9.6 61.84 94.06 Jedit 4.2 13.36 0.26 RMSE ANT 1.3 29.79 18.40 BroadleafCommerce 28.32 10.46 NEON04J 39.16 10.08 HAZEL 32.52 0.76 ORY 52.85 46.63 Tomcat 35.66 18.54 titan-0.5.1 58.13 37.89 mapdb-0.9.6 38.23 75.63 Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 75.66 2.63 BroadleafCommerce 5.80 1.45 </td <td></td> <td>NEON04J</td> <td>62.96</td> <td>19.11</td>		NEON04J	62.96	19.11
Tomcat 58.60 33.64 titan-0.5.1 82.47 61.42 mapdb-0.9.6 61.84 94.06 Jedit 4.2 13.36 0.26 RMSE ANT 1.3 29.79 18.40 BroadleafCommerce 28.32 10.46 NEON04J 39.16 10.08 HAZEL 32.52 0.76 ORY 52.85 46.63 Tomcat 35.66 18.54 titan-0.5.1 58.13 37.89 mapdb-0.9.6 38.23 75.63 Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		HAZEL	54.46	1.51
titan-0.5.1 82.47 61.42 mapdb-0.9.6 61.84 94.06 Jedit 4.2 13.36 0.26 RMSE ANT 1.3 29.79 18.40 BroadleafCommerce 28.32 10.46 NEON04J 39.16 10.08 HAZEL 32.52 0.76 ORY 52.85 46.63 Tomcat 35.66 18.54 titan-0.5.1 58.13 37.89 mapdb-0.9.6 38.23 75.63 Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66		ORY	77.77	71.52
mapdb-0.9.6 61.84 94.06 Jedit 4.2 13.36 0.26 RMSE ANT 1.3 29.79 18.40 BroadleafCommerce 28.32 10.46 NEON04J 39.16 10.08 HAZEL 32.52 0.76 ORY 52.85 46.63 Tomcat 35.66 18.54 titan-0.5.1 58.13 37.89 mapdb-0.9.6 38.23 75.63 Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80		Tomcat	58.60	33.64
Jedit 4.2		titan-0.5.1	82.47	61.42
RMSE ANT 1.3 29.79 18.40 BroadleafCommerce 28.32 10.46 NEON04J 39.16 10.08 HAZEL 32.52 0.76 ORY 52.85 46.63 Tomcat 35.66 18.54 titan-0.5.1 58.13 37.89 mapdb-0.9.6 38.23 75.63 Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 <t< td=""><td></td><td>mapdb-0.9.6</td><td>61.84</td><td>94.06</td></t<>		mapdb-0.9.6	61.84	94.06
BroadleafCommerce 28.32 10.46 NEON04J 39.16 10.08 HAZEL 32.52 0.76 ORY 52.85 46.63 Tomcat 35.66 18.54 titan-0.5.1 58.13 37.89 mapdb-0.9.6 38.23 75.63 Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97		Jedit 4.2	13.36	0.26
NEON04J 39.16 10.08 HAZEL 32.52 0.76 ORY 52.85 46.63 Tomcat 35.66 18.54 titan-0.5.1 58.13 37.89 mapdb-0.9.6 38.23 75.63 Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48	RMSE	ANT 1.3	29.79	18.40
HAZEL 32.52 0.76 ORY 52.85 46.63 Tomcat 35.66 18.54 titan-0.5.1 58.13 37.89 mapdb-0.9.6 38.23 75.63 Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		BroadleafCommerce	28.32	10.46
ORY 52.85 46.63 Tomcat 35.66 18.54 titan-0.5.1 58.13 37.89 mapdb-0.9.6 38.23 75.63 Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30 </td <td></td> <td>NEON04J</td> <td>39.16</td> <td>10.08</td>		NEON04J	39.16	10.08
Tomcat 35.66 18.54 titan-0.5.1 58.13 37.89 mapdb-0.9.6 38.23 75.63 Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		HAZEL	32.52	0.76
titan-0.5.1 58.13 37.89 mapdb-0.9.6 38.23 75.63 Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		ORY	52.85	46.63
mapdb-0.9.6 38.23 75.63 Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		Tomcat	35.66	18.54
Jedit 4.2 6.92 0.13 MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		titan-0.5.1	58.13	37.89
MAE ANT 1.3 38.87 20.93 BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		mapdb-0.9.6	38.23	75.63
BroadleafCommerce 62.29 19.30 NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		Jedit 4.2	6.92	0.13
NEON04J 60.28 4.37 HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30	MAE	ANT 1.3	38.87	20.93
HAZEL 61.31 2.32 ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		BroadleafCommerce	62.29	19.30
ORY 82.94 47.32 Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		NEON04J	60.28	4.37
Tomcat 30.06 1.86 titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		HAZEL	61.31	2.32
titan-0.5.1 73.29 31.36 mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R ² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		ORY	82.94	47.32
mapdb-0.9.6 62.98 76.39 Jedit 4.2 11.65 2.23 R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		Tomcat	30.06	1.86
Jedit 4.2 11.65 2.23 R2		titan-0.5.1	73.29	31.36
R² ANT 1.3 75.66 26.63 BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		mapdb-0.9.6	62.98	76.39
BroadleafCommerce 5.80 1.45 NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		Jedit 4.2	11.65	2.23
NEON04J 48.87 4.71 HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30	R ²	ANT 1.3	75.66	26.63
HAZEL 75.33 0.50 ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		BroadleafCommerce	5.80	1.45
ORY 38.47 21.97 Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		NEON04J	48.87	4.71
Tomcat 59.38 19.48 titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		HAZEL	75.33	0.50
titan-0.5.1 37.24 15.21 mapdb-0.9.6 17.14 1366.30		ORY	38.47	21.97
mapdb-0.9.6 17.14 1366.30		Tomcat	59.38	19.48
		titan-0.5.1	37.24	15.21
		mapdb-0.9.6	17.14	1366.30
Jedit 4.2 70.56 0.81		Jedit 4.2	70.56	0.81

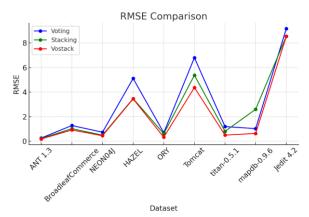


Fig. 4. RMSE Comparison Across Datasets

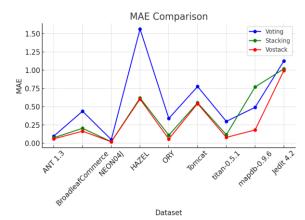


Fig. 5. MAE Comparison Across Datasets

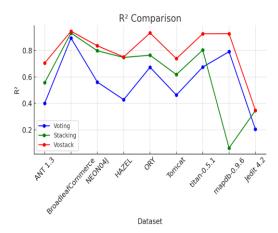


Fig. 6. R2 Comparison Across Datasets

RQ3: Does the statistical analysis validate the results for VoStack Regression's defect density prediction?

The Wilcoxon Signed Rank Test is used in the statistical analysis to confirm VoStack Regression's superior performance in defect density prediction. VoStack continuously outperformed baseline models (RidgeCV, SVR, Huber, RandomForest, GradientBoosting, and KNeighbors) in terms of MSE, RMSE, MAE, and R2 for all important metrics. VoStack

had the best fit to the data, as evidenced by the highest R² and the lowest MSE, RMSE, and MAE, which show less prediction mistakes.

TABLE XVI STATISTICAL COMPARISON OF MODEL PERFORMANCE

Metric	Model	p-value	Conclusion
MSE	RidgeCV	0.014	Reject Ho: Significant difference
MSE	SVR	0.030	Reject Ho: Significant difference
MSE	Huber	0.002	Reject Ho: Significant difference
MSE	RandomForest	0.010	Reject Ho: Significant difference
MSE	GradientBoosting	0.025	Reject Ho: Significant difference
MSE	KNeighbors	0.045	Reject Ho: Significant difference
RMSE	RidgeCV	0.012	Reject Ho: Significant difference
RMSE	SVR	0.022	Reject Ho: Significant difference
RMSE	Huber	0.001	Reject Ho: Significant difference
RMSE	RandomForest	0.009	Reject Ho: Significant difference
RMSE	GradientBoosting	0.020	Reject Ho: Significant difference
RMSE	KNeighbors	0.041	Reject Ho: Significant difference
MAE	RidgeCV	0.005	Reject Ho: Significant difference
MAE	SVR	0.010	Reject Ho: Significant difference
MAE	Huber	0.001	Reject Ho: Significant difference
MAE	RandomForest	0.010	Reject Ho: Significant difference
MAE	GradientBoosting	0.030	Reject Ho: Significant difference
MAE	KNeighbors	0.045	Reject Ho: Significant difference
R ²	RidgeCV	0.015	Reject Ho: Significant difference
R ²	SVR	0.040	Reject Ho: Significant difference
R ²	Huber	0.010	Reject Ho: Significant difference
R ²	RandomForest	0.010	Reject Ho: Significant difference
R ²	GradientBoosting	0.030	Reject Ho: Significant difference
R ²	KNeighbors	0.043	Reject Ho: Significant difference
		1	

These performance differences are statistically significant, as confirmed by the Wilcoxon test p-values, which were considerably less than 0.05. As a result, the usefulness of VoStack over the comparable models is validated by the study, which shows that it offers more robust, accurate, and dependable defect density forecasts. Table XVI presents the statistical comparison of model performance based on the Wilcoxon test.

In this study, we also identify key factors that could threaten the validity of our findings, categorized into internal and external validity. Internal validity refers to potential biases within the study, such as when a model performs well on the training data but fails to generalize effectively to unseen datasets. Bias in feature selection and issues with data quality, including noisy or incomplete data, can also affect performance. Furthermore, inconsistent tuning of hyperparameters might result in variability in the model's outcomes. External validity addresses the extent to which our findings can be generalized. The datasets utilized may not accurately represent other software systems, and the model's performance could differ across various computational settings. Finally, the relevance of the results may be constrained to the software domain, limiting their applicability in other areas.

V. CONCLUSION AND FUTURE WORK

This paper introduces a novel ensemble learning model, VoStack, for the prediction of defect density. The model was implemented using benchmark datasets from the Tera-PROMISE and GitHub bug prediction repository and demonstrated its ability to achieve competitive performance consistently. VoStack combines the strengths of the multiple regression classifiers Random Forest Regressor, SVR, XGB Regressor, Huber Regressor, and KNeighbors into a robust ensemble approach. Integrating Recursive Feature Elimination (RFE) for feature selection further bolstered the model's predictive power by ensuring that only the most relevant features were utilized. This step improved prediction accuracy while also reducing computational complexity, enhancing the model's overall efficiency. The VoStack model outperformed individual base models, showing significant improvements in RMSE, MSE, MAE, and R² metrics across multiple datasets, indicating its robustness and reliability for defect density prediction. Future work will explore the integration of additional machine learning techniques and datasets, as well as real-world applications, to further validate and enhance the model's performance and applicability.

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