

THE LOW-LYING STATES OF ^{59}Co IN THE GENERALIZED
SEMIMICROSCOPIC MODEL

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In a previous paper [1] we described the low-lying states of ^{49}Ti , ^{51}Cr and ^{57}Co with the generalized semi-microscopic model (GSMM) [2]. In this model, the states of a nucleus with odd-mass number A are approximated by linear combinations of the states of a hole coupled to an $A+1$ single-closed vibrating core and those of a particle coupled to an $A-1$ vibrating core. We faced certain difficulties in the detailed description of some peculiarities in ^{57}Co , so that it seems worthwhile to perform some calculations on ^{59}Co , the other cobalt isotope for which a reasonable amount of experimental data exist to make sense in comparison with theory. In this case, the basis states are those of a hole in the $1f_{7/2}$ shell coupled to the quadrupole phonons of ^{60}Ni and those of a particle which has available $1f_{5/2}$, $2p_{3/2}$ and $2p_{1/2}$ orbits, coupled to the quadrupole phonons of ^{56}Fe .

We used the following single-particle energies of the protons: $\epsilon(f_{5/2}) - \epsilon(p_{3/2}) = 0.75$ MeV and $\epsilon(p_{1/2}) -$

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TABLE I
 Comparison of experimental $|3\rangle$ and calculated negative-parity states below 2 MeV and spectroscopic factors $(2I+1)S$ in ^{59}Co .

I	Energy (MeV)		$(2I+1)S$	
	Exper.	Calc.	$(^3\text{He},d)$	(α,t)
7/2	0	0	1.36	1.52
3/2	1.10	0.97	0.44	0.32
5/2, 9/2	1.19	1.04		0
3/2	1.29	1.74	1.36	1.04
(1/2)	1.43	1.32	0.74	0.58
$\geq 7/2$	1.46	1.25		0
$\leq 7/2$	1.48			
(7/2)	1.74	1.85		0.002
5/2, 7/2	2.06	1.93		0.57

$-\epsilon(p_{3/2}) = 1.05$ MeV, taken from the experimental energy levels of ^{57}Ni , and $\epsilon(f_{7/2}) - \epsilon(p_{3/2}) = 2.57$ MeV which was estimated from the proton separation energy. The phonon energies were set equal to the energy of the 1_2^+ states of the corresponding vibrators, namely $\hbar\omega(^{58}\text{Fe}) = 0.805$ MeV and $\hbar\omega(^{60}\text{Ni}) = 1.333$ MeV. The corresponding quadrupole deformations were $\beta(^{58}\text{Fe}) = 0.25$ and $\beta(^{60}\text{Ni}) = 0.20$. In addition, the coupling constant of the cluster-field interaction was set equal to 0.9 times the value resulting from the radial wave functions corresponding to a Woods-Saxon potential with spin-orbit coupling. It has been found that the position of the $1_{1/2}$ and $1_{3/2}$ levels is very sensitive to the value of this coupling constant, which is the only free parameter. As for the remaining parameters, the vibrator charges were fixed at $(Z\beta/\sqrt{5})$, and the two usual values of the effective proton charge and gyromagnetic ratios $|1|$ were used.

The calculated energy spectrum and spectroscopic factors compare favourably with the experimental ones [3] (table 1). In particular, the two low-lying $3/2$ and the first $1/2$ states are predicted with the correct nature as far as the experimental data on spectroscopic factors are concerned (see also table 2); the first $3/2$ is mainly collective, whereas the second is predominantly of particle type. Table 3 shows the electromagnetic properties calculated with $e^{\text{eff}} = e$, $g_R = 0$, $g_S^{\text{eff}} = 3.5$. It is seen that they are fairly well described with this model, except the E2 transition probability from the $2_{3/2}$ level to the ground state.

TABLE 2.

Components $\times 10^3$ of the negative-parity states in ^{59}Co below 2 MeV. Each state is indicated by its ordering number and spin. The base vectors are $|\ell_j, NR\rangle$, where ℓ_j labels the single-particle subshell, and N and R indicate the number of phonons and their total angular momentum, respectively. Only amplitudes contributing more than 4% are listed.

	$1_{7/2}$		$1_{3/2}$
$ \text{f}_{7/2}, 00\rangle$	689	$ \text{f}_{7/2}, 12\rangle$	704
$ \text{f}_{7/2}, 12\rangle$	612	$ \text{f}_{7/2}, 22\rangle$	472
$ \text{f}_{7/2}, 24\rangle$	231	$ \text{p}_{3/2}, 00\rangle$	357
$ \text{f}_{7/2}, 20\rangle$	206		
	$1_{9/2}$		$1_{11/2}$
$ \text{f}_{7/2}, 12\rangle$	705	$ \text{f}_{7/2}, 12\rangle$	718
$ \text{f}_{7/2}, 24\rangle$	528	$ \text{f}_{7/2}, 24\rangle$	555
$ \text{f}_{7/2}, 22\rangle$	-358	$ \text{f}_{7/2}, 22\rangle$	262
		$ \text{f}_{7/2}, 36\rangle$	238
	$1_{1/2}$		$2_{3/2}$
$ \text{p}_{3/2}, 12\rangle$	570	$ \text{p}_{3/2}, 12\rangle$	508
$ \text{p}_{1/2}, 00\rangle$	530	$ \text{p}_{3/2}, 00\rangle$	-487
$ \text{f}_{5/2}, 12\rangle$	427	$ \text{f}_{7/2}, 24\rangle$	361
$ \text{f}_{7/2}, 24\rangle$	335	$ \text{f}_{7/2}, 22\rangle$	320
		$ \text{p}_{1/2}, 12\rangle$	312
	$1_{5/2}$		$2_{7/2}$
$ \text{f}_{7/2}, 12\rangle$	635	$ \text{f}_{7/2}, 00\rangle$	535
$ \text{f}_{7/2}, 24\rangle$	497	$ \text{f}_{7/2}, 22\rangle$	486
$ \text{f}_{7/2}, 22\rangle$	385	$ \text{p}_{3/2}, 12\rangle$	303
$ \text{p}_{3/2}, 12\rangle$	269	$ \text{f}_{7/2}, 12\rangle$	-299
$ \text{f}_{7/2}, 33\rangle$	250	$ \text{f}_{7/2}, 20\rangle$	-287
		$ \text{f}_{7/2}, 32\rangle$	-268
		$ \text{f}_{7/2}, 24\rangle$	-220

TABLE 3

Comparison of calculated (first row) and experimental (second row) values of $B(E2)$, $B(M1)$, mixing δ and branching b ratios, electric quadrupole Q and magnetic dipole μ moments, and mean lifetimes τ for some low-lying negative-parity states in ^{59}Co .

Transition	$B(E2)^a$	$B(M1)$	δ^b	b^b
τ_{I_i} τ_{I_f}	[W.u.]	[W.u.]		[%]
$1_{3/2} \rightarrow 1_{7/2}$	15.5 13.0 \pm 2.6			100 100
$1_{9/2} \rightarrow 1_{7/2}$	25.7 12.9 \pm 1.2	0.28	-0.23 -0.25 \pm 0.05	100 100
$1_{11/2} \rightarrow 1_{9/2}$	7.40	0.39	-0.02	12 <10
$1_{11/2} \rightarrow 1_{7/2}$	16.2 6.6 \pm 1.0			88 >90
$1_{1/2} \rightarrow 1_{3/2}$	14.9	0.01	-0.33	100 100
$2_{3/2} \rightarrow 1_{1/2}$	6.84	0.36	-0.04	47 0
$2_{3/2} \rightarrow 1_{3/2}$	15.0	0.02	-0.48	21 7 \pm 4
$2_{3/2} \rightarrow 1_{7/2}$	2.13 17.6 \pm 2.9			32 93 \pm 4
$1_{5/2} \rightarrow 1_{3/2}$	15.8	0.42	-0.12	15 20 \pm 3
$1_{5/2} \rightarrow 1_{7/2}$	3.23	0.26	0.15	85 80 \pm 3

Level	Q	μ	τ^a
τ_I	[eb]	$[\mu_N]$	[ps]
$1_{7/2}$	0.495 0.39 \pm 0.6 ^{c)}	4.177 4.616 \pm 0.009 ^{d)}	
$1_{3/2}$	0.127	3.18	4.6 >2.9

TABLE 3 (continued)

Level τ_I	Q [eb]	μ [μ_N]	τ^a [ps]
$1_{9/2}$	0.251	3.575	0.097 0.05±0.02
$1_{11/2}$	0.392	4.056	1.06 1.1±0.3
$1_{1/2}$		-0.331	67.6
$2_{3/2}$	-0.110	1.61 1.64±0.12 ^{e)}	0.56 0.59±0.02
$1_{5/2}$	0.084	2.55	0.016

a) Ref. [3]. b) K.L. Coop, I.G. Graham and E.W. Titterton, Nucl. Phys. A150 (1970) 346. c) T.R. Fischer, A.R. Polletti and B.A. Watson, Phys. Rev. C8 (1973) 1837.

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