

C5 Antilinear Operators in the Theory of Nuclear StructureF. HERBUT and M. VUJIČIĆ, *Institute "Boris Kidrič", Beograd*

Lately, self-consistent field methods (Hartree-Fock theory and Hartree-Bogolyubov theory) have been applied with great success to the study of nuclear structure. To simplify these variational problems a new mathematical formalism utilizing the algebra of antilinear operators¹⁾ has been developed.

This formalism generated new formulations of the Hartree-Bogolyubov theory in one-particle space²⁾ and quasiparticles space³⁾. This permitted construction of original methods for solving the dynamical equations of the theory, which were based on antilinear symmetries. On the assumption that the pairing operator is a given symmetry operator of the nuclear Hamiltonian, two versions of the dynamical equations were obtained. They consist of two interdependent parts, a Hartree-Fock and a Bardeen-Cooper-Schrieffer part²⁾. To solve both versions canonical forms of antilinear operators were used¹⁾. It was further shown that general complex Hartree-Bogolyubov equations in quasiparticle space can be solved by iterative diagonalization of a real symmetric matrix³⁾. For this purpose an antilinear matrix characteristic for the theory itself was utilized.

These substantial simplifications in solving the dynamical equations should stimulate and enable more ambitious and elaborate computations in nuclear structure theory. Computations of this kind are in progress.

References

- 1) F. Herbut and M. Vujičić, *Journ. Math. Phys.* **8** (1967) 1345;
- 2) F. Herbut and M. Vujičić, *Phys. Rev.* **172** (1968) 1031;
- 3) M. Vujičić and F. Herbut, to be published.

C6 Phenomenological Limit of Semimicroscopic DescriptionL. ŠIPS, *Institute "Ruđer Bošković", Zagreb***C7 On the BCS-Model in Nuclear Theory**J. HENDEKOVIĆ, *Institute "Ruđer Bošković", Zagreb*

The simple vibrational model failed to describe adequately the complex structure of the low-lying spectrum of some spherical vibrational nuclei, such as Sn isotopes. The main problem in the microscopic description of these nuclei arises from the large number of active particles moving in a limited number of orbitals. In some cases satisfactory results can be obtained by

introducing particle excitations coupled to phenomenological phonons¹⁾. The natural limitation of this model lies in the fact that the ground state and phononic excitations are structureless. Thus, in complex situations the Pauli exclusion principle cannot be properly taken into account. The most important pairing correlations and the basic structure parameters of the ground state, namely the occupation probabilities of single particle orbitals, can be expressed simply through the parametrization of the BCS wave function

$$|\bar{0}\rangle = \prod_{\alpha>0} (u_{\alpha} + v_{\alpha} s_{\alpha} c_{\alpha}^{+} c_{-\alpha}^{+}) |0\rangle, \quad s_{\alpha} = (-1)^{j_{\alpha} - m_{\alpha}}.$$

Here c_{α}^{+} are the creation operators of the nucleon in the orbit α , and $\alpha \equiv (a, j_{\alpha}, m_{\alpha})$. v_{α} is the probability amplitude for the occupation of the level α , and $|0\rangle$ is the physical vacuum.

Many extensive calculations in the framework of the BCS-model have recently been performed with considerable success²⁾. Nevertheless, there are many objections to the BCS-model, the most serious referring to its particle number nonconservation. In addition, there are examples of serious disagreement between the results of the shell-model and the BCS-model calculations³⁾. Arguments which might explain this discrepancy are given below.

The following is an intuitive "justification" of the BCS-model in nuclear spectroscopy: The Bogoliubov-Valatin quasi-particle (qp) transformation approximately diagonalizes the strong short-range component of the nucleon-nucleon interaction. The residual interaction between quasiparticles is very much reduced and should be easily diagonalized. The quasiparticle method is then understood as an approximation method in shell-model calculation. Below the above arguments are shown to be incorrect.

A simple model of two levels with spacing ε and one kind of particles interacting through the pairing force of strength G is analysed. The first level with $j=13/2$ is occupied in the normal state, the second one with $j=15/2$ is empty. Fig. 1 compares the structure of the shell-model seniority zero ground state wave function, expressed in the particle-hole representation (P), and that of the very same wave function, expressed in terms of quasiparticles (Q). The number n refers to the n particle pairs and n hole pairs in the first case, or to the $4n$ and $(4n-2)$ qp excitation modes in the second case. Total weight (probability) of the components of a given type is drawn as a function of n for several ε/G . The features of Fig. 1 are:

a) The weight of the BCS ground state $|\bar{0}\rangle$, (value of Q for $n=0$) in the shell-model ground state is very small in both cases.

b) The weight of components with a large number of quasiparticles is not negligible, and is sometimes even dominant.

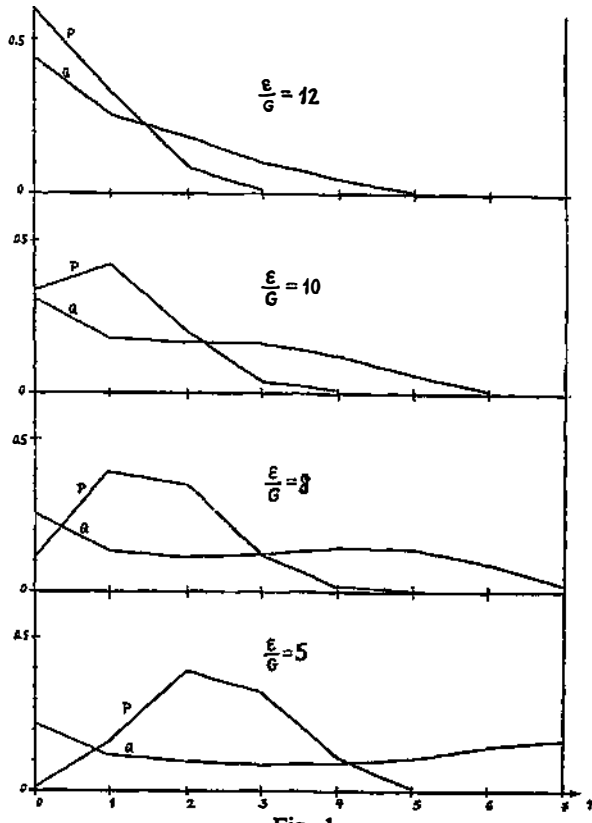


Fig. 1

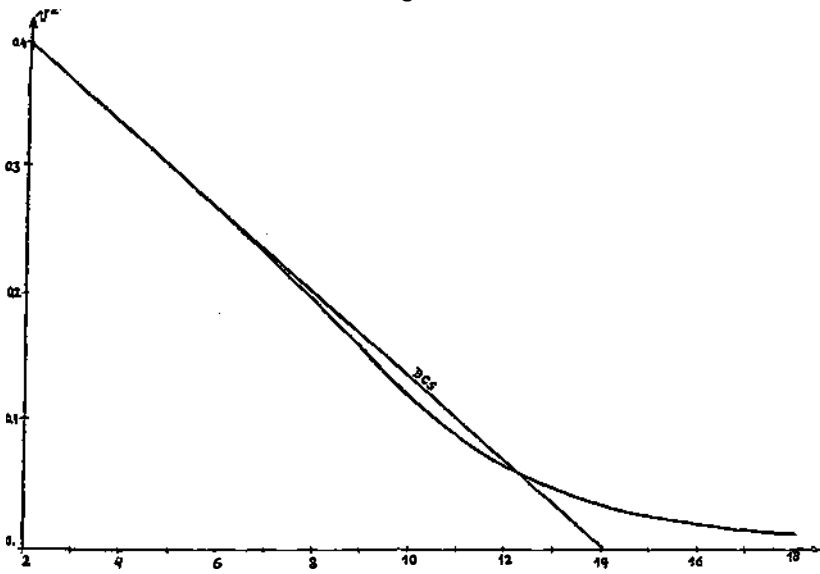


Fig. 2