

Adiabatic TDHF as a consistent theory for anharmonic collective motion

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Many large amplitude collective phenomena, like anharmonic vibrations, fission etc., can be characterised by one, or a few, collective coordinates  $q=q(t)$ . In microscopic theories of collective motion one links the  $q$ -description to the space of  $A$ -particle coordinates  $x_i$ , using a set of deformed Slater determinants, or BCS states resp.,  $\Phi_q(x_1, \dots, x_A) = \langle x_i | q \rangle$ . With this collective basis  $|q\rangle$  and its dynamic generalisation  $|q, p\rangle$ , where  $p$  is the momentum conjugate to  $q$ , one obtains the (classical) collective Hamiltonian  $\mathcal{H}(q, p) = \langle q, p | \hat{H} | q, p \rangle$ , which is to be requantised in order to give the collective Schrödinger equation. The question of quantisation, although part of a consistent collective theory<sup>1)</sup>, will not be discussed here, because of limited space.

The topic of this contribution is the first point, the proper choice of the collective path  $|q\rangle$ . Usually, it is guessed by assuming a properly deformed shell model (e.g. the Nilsson model). A less ambiguous way is, to solve constrained HF, where  $\hat{H} \rightarrow \hat{H} - \lambda Q_c$ . The constraint  $Q_c$ , however, is still at choice. ATDHF now aims to give a unique prescription for determining the path  $|q\rangle$  and the collective operator  $Q$ . The full derivation<sup>1)</sup>, using TDHF in the limit of small velocities, is rather lengthy. Here, we merely try to make the ATDHF equations plausible.

Starting point is, of course, a constrained HF,

$$\langle q | [a^\dagger a, \hat{H} - \lambda Q_c] | q \rangle = 0 \quad (1)$$

where  $\lambda$  is a Lagrange multiplier, which finally becomes  $\lambda = \partial_q \langle q | \hat{H} | q \rangle$ . For small velocities, one obtains the dynamic extension from linear response to an additional dynamic constraint  $\dot{q}P$ , where  $P = i\partial_q$ . This leads to  $|q, p\rangle = \exp(ip\partial_q) |q\rangle = (1 + ip\partial_q) |q\rangle$ , where the dynamic generator  $Q_d$  is given by the response equation

$$\langle q | [a^\dagger a, [H, Q_d] + iP/M] | q \rangle = 0 \quad (2)$$

and the collective mass is  $M^{-1} = \langle q | [Q_d, [H, Q_d]] | q \rangle$  (the Thouless-Valatin mass). We thus have two collective operators  $Q_c$  and  $Q_d$ . If there is really a decoupling collective mode, one has place for only one operator  $Q$ . We therefore have to require Q-consistency:  $Q_c = Q_d$ . This feeds the dynamic generator  $Q_d$  from eq.(2) as static constraint  $Q_c$  back into eq.(1), leading to a coupled set of equations, which uniquely prescribes a collective

path.

For its explicit construction, one combines eqs.(1) and (2) to one differential equation

$$\partial_q |q\rangle = (1/\lambda) [H, H_{ph}] |q\rangle \quad (3)$$

(where  $A_{ph}$  means the 1p-1h part of an operator A). The solution of eq.(3) requires as initial condition one point  $|q\rangle$  with  $\lambda \neq 0$ , i.e. one point off the HF minimum. At the HF point itself, it may be labelled  $|0\rangle$ , the path has to join an RPA mode. Thus one can initialise the path by choosing one particular RPA mode at  $|0\rangle$  and stepping to the first point off the minimum,  $|\delta q\rangle = (1-i\delta q P)|0\rangle$ , using the RPA momentum P. From  $|\delta q\rangle$  on, eq.(3) is in action. The choice of an initial RPA mode is the only freedom left in the ATDHF scheme. With it one determines the sort of collective motion, one wants to study.

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