

THE NUMERICAL ESTIMATES OF ENERGY AND SOFT-MODE PARAMETERS OF
ADA-ADP ANTIFERROELECTRIC SOLUTIONS ON THE BASIS OF DIELECTRIC
MEASUREMENTS⁺

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Abstract: The dielectric measurement data are used
for numerical estimates of energy and
soft-mode parameters of ADA-ADP solid solutions

It is very well known ^{1,2} that solid antiferroelectric
ADA-ADP solutions possess both the chemical stability and optimal
physical properties in a wide (working) temperature interval,
which is of great interest in various technical applications.
Such solutions, but of low concentration x (one of the components,
say As), as analysed by various experimental techniques, could
also give some new information to yield deeper insight into the
nature of ferro- and antiferroelectric critical phenomena inclu-
ding the softening, problems of universality and central peaks.

On the basis of dielectric measurements (the maximal
perpendicular permeability of a free ADA-ADP solution, i.e. the
Curie-Weiss temperature $T_0(x)$ and the constant $C(x)$ and their
simple interpretation in the frame of the pseudospin model ^{3,4}
(extended to the proton-phonon coupling ^{5,6}), in a previous work
of authors ⁷, the energy parameters of this model ($J_{q_0}(x)$ -
the Fourier transformed effective inter-sublattice Ising con-
stant, taken at the edge of the Brillouin-zone, q_0 , and $2\Omega(x)$ -

⁺ The experiments have been carried out in Laboratoire de Physique
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the proton tunneling energy) as well as the corresponding soft-mode parameters⁸ are numerically estimated (in MFA⁵⁻¹⁰) for several concentrations. In these calculations the following formulae are used^{7*}:

(a) The pseudospin-model parameters⁵⁻¹⁰

$$J_{q_0}(x) = 2k_B T_c(x); \quad T_c(x) = T_0(x) + 54 [^\circ K] \quad (1)$$

(The difference between the critical point $T_c(x)$, and $T_0(x)$ has been found⁷ as nearly independent of x and in accordance with the theoretical predictions^{5,6})

$$2\Omega(x) = 8\mu \left[\frac{N k_B b(x) l/2}{C(x)} \right] \quad (2)$$

where $\mu = e^* l \sim 10^{-18}$ esu - the proton pseudo-dipole, l being the distance between the double-well potential minima at hydrogen bond¹¹ and $N \sim 5^{10} \times 10^{21}$ [proton/cm³] - the total number of protons per unit volume.

(b) The soft - mode parameters⁸

$$\lambda(x) = \frac{[2\Omega(x)]^2}{T_c(x)} [\text{cm}^{-2} \text{K}^{-1}] \quad (3)$$

$$\rho(x) = \frac{1}{6} 2\Omega(x) J_{q_0}(x) [\text{cm}^{-2}] \quad (4)$$

$(\omega_q^2 = \lambda(T - T_c) + \rho \sum_{\alpha=x,y,z} (q - q_{0\alpha})^2$ - the soft-mode

behaviour in an antiferroelectric).

The numerical results for all four parameters, for six characteristic concentrations, are listed in the table enclosed.

As a brief comment one can see a nonlinear dependence in $\lambda(x)$ (a minimum about $x \sim 0,120-0,400$) which has no any experimental evidence nor theoretical explanation so far.

*) Some errors in ref. 7 are corrected and a more convenient notation is used.

x	$T_c(x) [^{\circ}K]$	$T_o [^{\circ}K]$	$c(x) [^{\circ}K]$	$b(x) [^{\circ}K^2]$	$J_{q_o}(x) [cm^{-1}]$	$2\Omega(x) [cm^{-1}]$	$\lambda(x) [cm^{-2} \cdot ^{\circ}K^{-1}]$	$\rho(x) [cm^{-2}]$
0,000	145,86	91,86	4,000	13,397	402,5	48,52	16,14	3,255,2
0,048	148,66	94,86	4,040	14,183	410,3	49,67	16,60	3,396,7
0,118	154,16	100,16	4,080	15,330	425,5	51,39	17,13	3,644,0
0,390	172,96	118,96	4,550	19,784	477,4	52,28	15,80	4,398,0
0,615	186,76	132,76	4,750	23,469	515,5	58,93	18,59	5,062,0
1,000	218,96	168,96	5,650	29,774	604,3	60,86	16,92	6,130,0

The above table can be interpolated for every possible x too.

Therefore, it enables one to predict simply all important physical properties of these materials as used in various applications. Otherwise the estimates obtained could provide a good orientational fit in more precise combined neutron scattering and roentgenographic experiments dealing with the influence of the component concentration on the rather complex critical effects in such mixed antiferroelectrics.

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